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To the Graduate Council:

I am submitting herewith a thesis written by Abdulrahman M. Enani entitled "A Neural Network for Collaborative Forecasting." I have examined the final electronic copy of this thesis for form and content and recommend that it be accepted in partial fulfillment of the requirements for the degree of Master of Science, with a major in Industrial Engineering.

Xueping Li, Major Professor

We have read this thesis and recommend its acceptance:

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(Original signatures are on file with official student records.)

A Neural Network for Collaborative Forecasting

A Thesis Presented for the
Master of Science
Degree
The University of Tennessee, Knoxville

Abdulrahman M. Enani
December 2016

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ABSTRACT

As the supply chain activities' backbone, demand forecasting must be accurate. This paper proposes an artificial neural network forecasting model, which integrates and synchronizes shared information, such as sales or consumption rate among different partners, to improve the forecasting's accuracy. This information sharing is part of the collaborative planning, forecasting and replenishment (CPFR) model, which is a supply chain model aiming to enhance the supply chain's efficiency by jointly planning and forecasting between two or more supply chain partners that will be used as the base for production and replenishment activities. The model is validated using a tuna product sales data, and the combination of individual forecasts resulted in better demand forecasting accuracy for the supply chain. This improvement will lead to reduced costs associated with the forecast's overestimation or underestimation.

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CHAPTER ONE

INTRODUCTION AND GENERAL INFORMATION

Supply chains are widening and becoming more complicated since businesses (e.g., manufacturers, retailers, pharmacies, and health providers) have suppliers globally. Having said that, lead times are also getting longer because of increased distances and are putting more pressure on businesses to have accurate forecast systems. Demand forecasting results in either overestimation or underestimation. Overestimation can lead to overstock, adding up costs, including holding costs, dumping costs for perishable items, and return costs. Underestimation leads to loss of potential sales and as a result less revenue. To overcome these problems, companies are developing new ways and models for forecasting and managing their inventories. One of the models is called Vendor-Managed Inventory, which Walmart initiated. With this model, suppliers are responsible for managing their products at Walmart's stores and have access to sales data. As a result, Walmart can achieve close to 100% order fulfilment on merchandise [1]. Another innovation in the supply chain field is the Collaborative Planning, Forecasting and Replenishment (CPFR) model, which is "an evolving business practice that seeks to reduce supply chain costs by promoting greater integration, visibility, and cooperation between trading partners' supply chain" [2]. CPFR involves four main collaborative activities: Strategy & Planning, Demand & Supply Management, Execution, and Analysis. Toiviainen and Hansen have divided these activities into eight tasks, which are listed in Table 1.1 [3].

This paper focuses on collaborative forecasting and how to get a forecast that satisfies the partners in terms of better accuracy. In collaborative forecasting, the partners conduct their forecast individually using point of sales (POS) data shared with them. Then the forecasts are combined using the proposed model.

Table 1.1. Tasks under Collaborative Planning, Forecasting and Replenishment (CPFR)

Collaborative Activities	Collaborative Tasks
Strategy and Planning	1. Collaboration Arrangement
	2. Joint Business Plan
Demand and Supply Management	3. Sales Forecasting
	4. Order Planning/Forecasting
Execution	5. Order Generation
	6. Order Fulfillment
Analysis	7. Exception Management
	8. Performance Assessment

Tremendous work has been done in the area of supply chain management (SCM). Rouse defined *supply chain management* as “the oversight of materials, information, and finances as they move in a process from supplier to manufacturer to wholesaler to retailer to consumer. Supply chain management involves coordinating and integrating these flows both within and among companies” [4]. Rouse’s definition identifies three main flows in any supply chain: products or materials flow, information flow, and finances flow. Many types of information can be shared among partners of a supply chain. In their article “Information Sharing in Supply Chain Management,” Lotfi, Mukhtar, Sahran, and Zadeh mentioned some of the types of shared information including inventory information, order information, sales data, sales forecasting, exploitation information about new products, and product ability on formation [5]. These authors have also investigated the benefits of information sharing within supply chains and summarized them along with the sources as shown in Table 1.2. This study proves how sharing two types of information, sales data and forecasts, can improve the forecast’s accuracy. This improvement can lead to better customer satisfaction products will be available, and reduce the cost of holding extra inventory resulting from over estimation will be reduced. To benefit from the shared information, we are going to combine the forecasts.

Table 1.2. Information Sharing Benefits

No.	Benefits	Sources
1	Inventory reduction and efficient inventory management	[6, 7, 8, 9]
2	Cost reduction	[6, 7, 9, 10]
3	Increased visibility (significant reduction of uncertainties)	[9, 10, 11, 12, 13]
4	Significant reduction or complete elimination of bullwhip effect	[9, 11, 15, 16]
5	Improved resource utilization	[6, 9]
6	Increased productivity, organizational efficiency, and improved services	[6, 9, 10, 14]
7	Building and strengthening social bonds	[9, 10, 17]
8	Early problem detection	[9, 16, 18]
9	Quick response	[9, 16]
10	Reduced cycle time from order to delivery	[10]
11	Better tracing and tracking	[10]
12	Earlier time to market	[9]
13	Expanded network	[9]
14	Optimized capacity utilization	[9]

Forecast Combination

When more than one forecast for the same event is available, most businessmen and statisticians try to find which one is better (or best). In 1969, Bates and Granger developed the idea of combining forecasts. They showed how the combination improved forecast accuracy and was better than either forecast separately in terms of a better mean squared forecast error. The easiest way to do the combination is to drive the forecasts' average (assigning identical weights to individual forecasts). In his article "Combining Forecasts: A Review and Annotated Bibliography," Clemen mentioned how he increased the forecast's accuracy by combining multiple forecasts, whether the forecasts are econometric or extrapolation, judgmental or statistical. According to Clemen, huge accuracy improvements can be made by averaging the forecasts. [19]

Based on the literature review, combining forecasts has been shown to be useful, cost-effective, and beneficial. Conducting a survey to determine how often firms combine forecasts, Dalrymple found that 40% of the firms frequently or usually combine forecasts. [20] This finding indicates that combining forecasts is becoming popular. Many methods can be used to find the weights for combining

forecasts. Blair, Leonard, and Elsheimer identified the following nine methods for determining the weights: [21]

1. Simple average
2. User-defined weights
3. Rank weights
4. Ranked user weights
5. Root mean squared error (RMSE) weights
6. Corrected Akaike's information criterion (AICC) weights
7. Ordinary least squares (OLS) weights
8. Restricted least squares weights
9. Least absolute deviation (LAD) weights

Other methods for finding weights are available.

For example, some researchers suggested conducting a linear regression to find the combination weights. Bayesian approaches have also been used in finding the best combination. Adhikari, and Agrawal suggested using the artificial neural network for combining multiple time-series forecasts. [22] Thus, many options are available for combining forecasts; however, a problem arises in determining each forecast's weight. In this paper, the artificial neural network is used because it can estimate any continuous function. Another advantage of neural networks is that a linear relationship between outputs and inputs does not have to be assumed; instead, it can approximate nonlinear functions.

CHAPTER TWO

PROBLEM DEFINITION

2.1. Problem Statement

One of the major tasks for any inventory controller is to predict upcoming sales. This task may help determine how much to order from the suppliers and when, how much inventory should be kept in distribution centers to feed stores, and how much to keep in retail stores. Demand forecast is the foundation of supply chain planning. Forecasts are always associated with some error, but are good indicators of demand. Short-term forecasts are usually more accurate than long-term forecasts. Indeed, the standard deviation of error relative to the mean is larger with long-term forecasts. In addition, disaggregate forecasts are less accurate than aggregate ones. One of any retailer's nightmares is being out of stock, especially when quickly moving items because lack of stock means loss of potential sales. Being out of stock is also critical for imported items, especially those with long lead times (i.e., the time between ordering an item and receiving it). Over predicting is also an issue but not as big as being out of stock because this problem can be corrected with price markdowns. Thus, forecasting is important, and its accuracy can affect a company's revenues because it adds costs associated with inventory, ordering, transportation, and labor for shipping and receiving. Many forecasting models can be used to predict sales for any product of interest. The key is finding the best model with the highest accuracy to represent a product. In combining different forecast data using the neural network, the problem is finding the weight each forecast contributes to the final forecast.

2.2. Problem Formulation

2.2.1 Parameters

The following parameters (i.e., data needed) must be defined before solving the problem:

- i : Suppliers index
- t : Weeks index
- A_t : Actual sales in week t
- F_t : Company's internal sales forecast for week t
- X_{it} : Collected sales forecast from supplier i for week t
- Y_t : Combined sales forecast for week t using neural network
- T : Number of historical data available
- I : Total number of suppliers available for the product of interest.

2.2.2 Objective Function:

The two main objective functions are identified below:

- Finding the weight for each forecast to contribute to the combined forecast that will have the minimum error

$$\text{Min} \left(\frac{1}{T} \sum_{t=1}^T \frac{|A_t - f(F_t, X_{it})|}{A_t} \right) * 100 \quad (1)$$

Given that

$$Y_t = f(F_t, X_{it}) \quad (2)$$

- Choosing the forecast that has the minimum error from the competing ones: company's internal forecast, suppliers' forecast, and the combined neural network forecast.

$$\text{Company's Error} = \left(\frac{1}{T} \sum_{t=1}^T \frac{|A_t - F_t|}{A_t} \right) * 100 \quad (3)$$

$$\text{Supplier's Error} = \left(\frac{1}{T} \sum_{t=1}^T \frac{|A_t - X_{it}|}{A_t} \right) * 100 \quad \text{for } i = 1, \dots, I \quad (4)$$

$$\textit{Combined Forecast Error} = \left(\frac{1}{T} \sum_{t=1}^T \frac{|A_t - Y_t|}{A_t} \right) * 100 \quad (5)$$

CHAPTER THREE

METHODOLOGY

Most companies worldwide are conservative when sharing data with their suppliers. Some are afraid of losing their business (e.g., car dealers think if they share the demand data, manufacturers would bypass them and sell the cars themselves). To get a better deal, others don't share sales data. For example, when I was working for one of the biggest retailers in Saudi Arabia as an inventory controller, buyers didn't want me to share the actual sales data with the suppliers in order to get discounted goods.

To encourage these companies to share their sales or consumption data with their suppliers, a tangible benefit must be provided. The proposed method shows how sharing sales or consumption data with the supply chain's key players can improve the forecast's accuracy, which is the heart of any business's planning process. The artificial neural network is used to combine forecasts because it can estimate not only any continuous function but also nonlinear data. Below are the steps for the proposed method:

1. Gather historical sales or consumption data for the product of interest.
2. Share the data with key supply chain players, such as manufacturers or suppliers.
3. Have the players conduct individual forecasts based on the gathered data using their own forecast model. Thus, internal and external forecasts will be available.
4. Construct the collaborative neural network using the actual data as the target variable and the individual forecasts as the input. For conducting the neural network, Alyuda Forecaster XL, which is add-in software within Excel can be used. One of this software's best features is that neural networks can be generated while retaining all the data-operation tools in

Excel. In fact, it is “the only forecasting Excel add-in with an automatic neural network architecture and parameters selection.” [23] One advantage of the program is that the user doesn’t need to be an expert in artificial intelligence or statistics to generate neural networks.

5. Compare the neural network’s output with each forecast based on three different criteria: Mean Absolute Deviation (MAD), Mean Square Errors (MSE), and Mean Absolute Percentage Error (MAPE).
6. Conduct the forecast using the best model.

Steps 3, 4, and 5 are explained below.

3.1. Step 3: Individual Forecasts

3.1.1 Internal Forecast

For the internal forecast, a Matlab Module was created to choose the best- fitting ARMA model for the date for which we are interested in generating a forecast. First, the model reads the data. In our case, it reads the data from an Excel sheet, but it can be adjusted to read from other files. Second, it generates three graphs for the data: time-series distribution curve, autocorrelation function (ACF), and partial autocorrelation function (PACF).

Autocorrelation is the linear dependence of a variable with itself at two points in time. For stationary processes, autocorrelation between any two observations depends on the time lag k between them.

- Autocovariance is defined by

$$Cov(y_t, y_{t-k}) = \frac{Y_k}{Y_0} \text{ for all lags } k = 0, \pm 1, \pm 2, \dots \quad (6)$$

- Autocorrelation is defined by

$$\rho_k = Corr(y_t, y_{t-k}) = \frac{Cov(y_t, y_{t-k})}{Y_0} = \frac{Y_k}{Y_0} \quad k = 0, \pm 1, \pm 2, \dots \quad (7)$$

- Partial autocorrelation is the autocorrelation between y_t and y_{t-k} after removing any linear dependence on $y_1, y_2, \dots, y_{t-h+1}$. The partial lag-k autocorrelation is denoted $\hat{\rho}_{k,k}$. The denominator γ_0 is the lag 0 covariance, i.e., the unconditional variance of the process. A plot of ρ_k against non-negative values of k gives the autocorrelation function. Note that $\rho_0 = 1$ by definition.

To estimate the theoretical autocorrelation and partial autocorrelation, we use the sample autocorrelation and sample partial autocorrelation, which are important statistics. They are used as qualitative model selection tools to compare with known theoretical autocorrelation functions. For an observed series y_1, y_2, \dots, y_t , denote the sample mean \bar{y} . The sample lag – k autocorrelation is given by

$$\hat{\rho}_k = \frac{\sum_{t=k+1}^T (y_t - \bar{y})(y_{t-k} - \bar{y})}{\sum_{t=1}^T (y_t - \bar{y})^2} \quad (8)$$

The standard error for testing the significance of a single lag – k autocorrelation, $\hat{\rho}_k$, is approximately

$$SE_{\rho} = \sqrt{\frac{1}{T} (1 + 2 \sum_{i=1}^{k-1} \rho_i^2)} \quad (9)$$

When we use (autocorr), a matlab-built ifn function to plot the sample autocorrelation function (also known as the correlogram), approximate 95% confidence intervals are drawn at $\pm 2SE_{\rho}$.

The sample lag – k partial autocorrelation is the estimated lag – k coefficient in an AR model containing k lags, $\hat{\theta}_{k,k}$. The standard error for testing the significance of a single lag – k partial autocorrelation is approximately $1/\sqrt{T - 1}$.

Third, the module fits different ARMA(p, q) models and calculates the likelihood for each of them. The user can decide on the maximum for both p and q . Fourth,

the module calculates two different model-selection criteria: Akaike's information criterion (AIC) and Bozdogan's consistent AIC (CAIC).

The Akaike information criterion (AIC) is an unknown constant, which can be determined and used to measure statistical models' relative quality for a particular set of data. Given several different models for a certain data, AIC estimates each model's quality, relative to that of the other models. Therefore, AIC provides a means for model selection and is approximated by

$$\text{AIC} = -2\log L(\hat{\theta}) + 2k \quad (10)$$

where

- $L(\hat{\theta})$ is the maximized likelihood function, $\hat{\theta}$ is the MLE of, and k is the number of free parameters in the model.
- In AIC, the compromise occurs between the maximized log likelihood, i.e., $-2\log L(\hat{\theta})$ (the lack of fit component) and the number of free parameters estimated within the model (the penalty component); the latter is a measure of complexity or the compensation for the bias in the lack of fit when the maximum likelihood estimators are used.
- The model with minimum AIC value is chosen as the best model to fit the data.

Bozdogan's consistent AIC (CAIC) is also a model selection criterion developed by Bozdogan in 1987. It is similar to AIC, but the difference is in the penalty term. CAIC resolves issues related to AIC's second term (e.g., the consistency similar to SBC). To make AIC consistent, the multiplier of the number of free parameters in the penalty term (i.e., AIC's second term) depends on the sample size. Thus, CAIC is defined in equation 11, and the model with minimum CAIC value is chosen as the best model to fit the data.

$$CAIC = -2\log L(\hat{\theta}) + k(\log(n)+1) \quad (11)$$

Fourth, based on the criterion's minimum, the module generates an ARMA model and finds the its parameter estimates. Finally, it forecasts the number of periods the user defines and creates a plot for the actual data versus the forecasted data.

3.1.2 External Forecast

For generating the external forecasts, proForecaster, an add-in application within Excel, was used. proForecaster was developed for business users who create educated predictions quickly and without statistical training. It uses state-of-the-art statistical forecasting methods and neural network technology to accurately predict the future [24]. One of this application's best features is that it can generate many sophisticated forecasting models within the Excel environment. Table 3.1 shows this product's features.

Table 3.1. ProForecaster Application Features

Feature	Benefit
Forecasting Wizard	Make predictions quickly without needing statistical know-how
15 Statistical Forecasting Models plus Neural Network Technology and a Hybrid Forecasting Model	Accurately predict historical data
Expert Forecasting Engine	Make all technical decisions so that non-statisticians can produce sophisticated predictions
Regression Wizard to forecast cross-sectional data and time-series data through explanatory variables	Make regression analysis at a fly and determine how variables influence the target variable
Advanced Reporting generated in an Excel worksheet	Create the prediction results in Excel and easily insert them into the corporate layout
Forecasting up to 1,000,000 time series in one run.	Create forecasts simultaneously for different time series

(pro BS, 2016)

Forecasting Steps

Step 1: Select data in Excel

Data can be chosen by columns or rows, and there is an option to select if the data contain a header. Another option can be selected for seasonality. A screenshot of this step is presented in Figure 3.1.

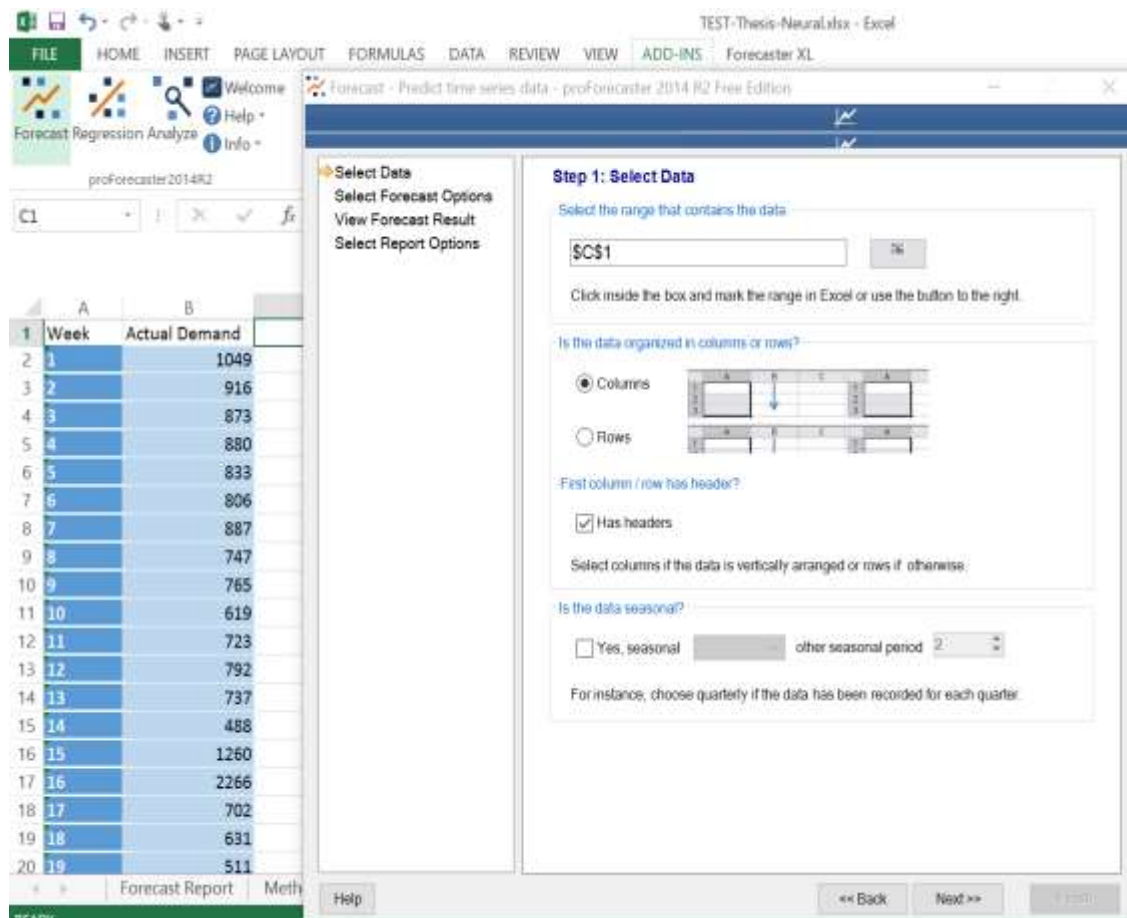


Figure 3.1. Screenshot for Data Selection in Excel

Step 2: Select Forecast Options

In this step, we can choose the preferred forecasting methods as well as the ranking method (e.g., MAD, RMSE, MAPE, or expert rank) that will check the goodness of fit on validation data. The number of periods to predict can also be selected in this step. A screenshot of this step appears in Figure 3.2.

Step 3: View the forecasting results

In this step the models' results can be seen for each forecasting method selected. A graphic of the actual versus the fitted model along with the forecast is provided. Also included is a box containing the parameter estimates for the forecasting method chosen and a summary containing the accuracy. A screenshot of this step is presented in Figure 3.3.

Step 4: Select Report Options

This step's purpose is to determine what to include in the report in terms of forecasting methods' statistics and forecasting charts. The option is also available to show the predictions for either the best model or the best three models. A screenshot of this step is shown in Figure 3.4. Figures 3.5 and 3.6 are screenshots of the generated reports.

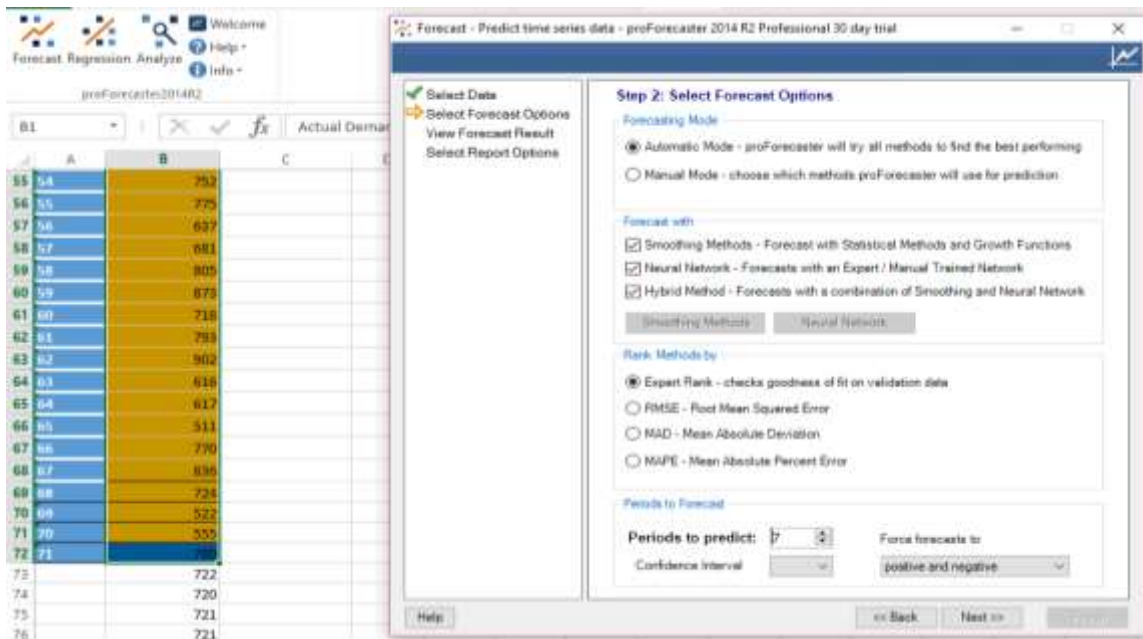


Figure 3.2. Screenshot for Selecting Forecast Options in Excel

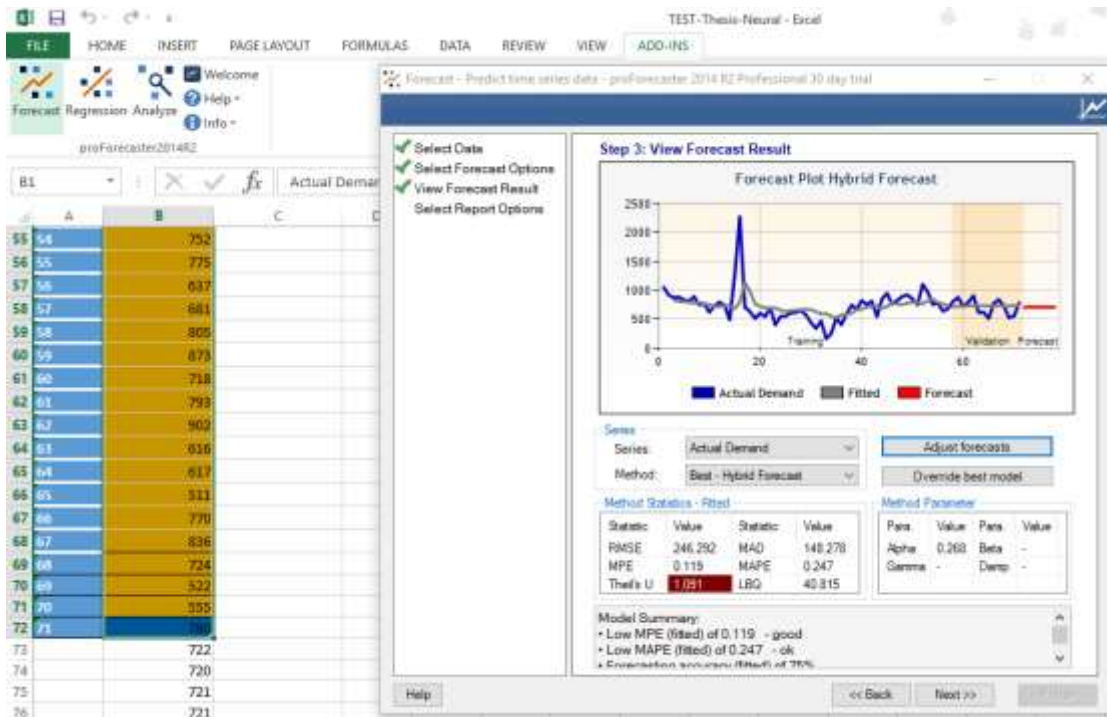


Figure 3.3. Screenshot for Forecast Results in Excel

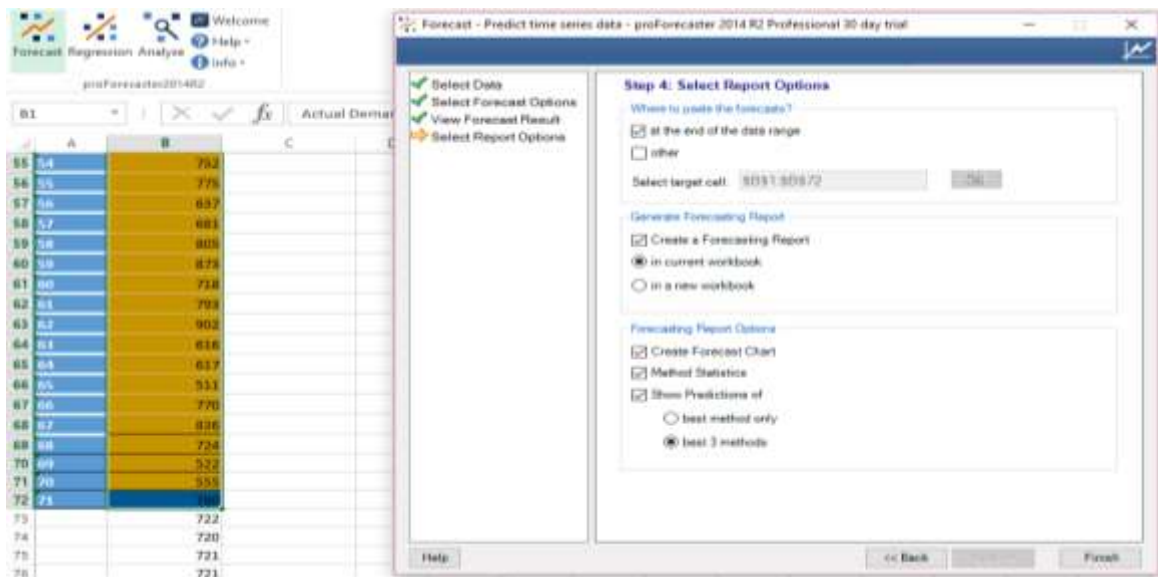


Figure 3.4. Screenshot for Report Option Selection in Excel

Method Statistics												
Series	Method	MAE	RMSE	MAPE	MAPI	MAPE	MAPE	MAPE	MAPE	MAPE	MAPE	MAPE
Actual Der Expert Neural Net	1	264.177	105.986	0.295	0.146	1.455	95.4095	-	-	-	-	-
Actual Der Hybrid Forecast	2	245.976	150.25	0.252	0.124	1.096	42.2411	0.54	-	-	-	-
Actual Der Linear Exponential Smoothing	3	253.968	161.198	0.252	0.105	0.989	39.7357	0.286	0	-	-	-
Actual Der Single Exponential Smoothing	4	253.968	161.198	0.252	0.105	0.989	39.7357	0.286	-	-	-	-
Actual Der Linear Growth	5	262.934	170.163	0.298	0.14	1.405	87.0092	763.161	-1.09232	-	-	0
Actual Der Moving Average	6	285.461	167.318	0.247	0.076	1.042	57.3791	-	-	-	-	-
Actual Der Damped Exponential Smoothing	7	325.085	188.883	0.297	0.049	1.191	46.3556	1	0.503	-	-	0.719
Actual Der Triple Exponential Smoothing	8	310.32	175.977	0.266	0.082	1.048	41.3618	0.085	-	-	-	-
Actual Der Quadratic Growth	9	255.545	159.375	0.272	0.126	1.304	81.993	0	-12.6795	0.16482	-	-
Actual Der Double Moving Average	10	334.186	214.315	0.326	0.06	1.32	86.4072	-	-	-	-	-
Actual Der Polynomial Growth	11	245.734	136.706	0.211	0.111	1.228	60.3951	-	-	-	-	-

Figure 3.5. Screenshot for the Forecast Statistics Report by ProForecaster

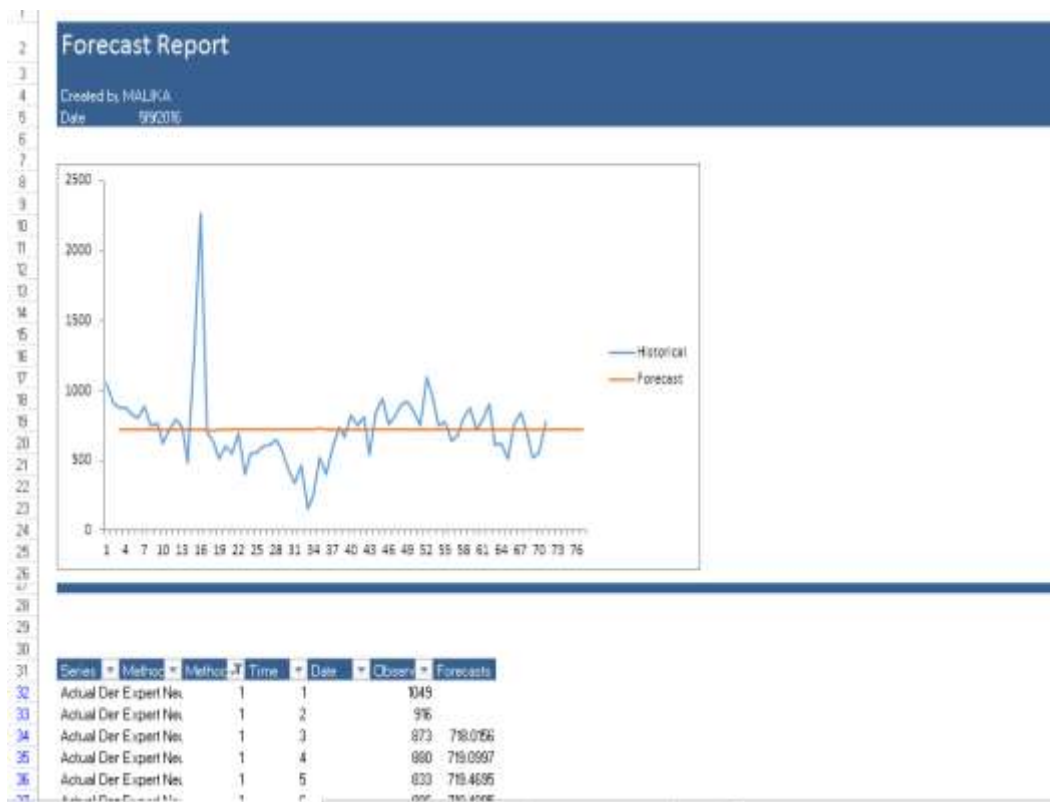


Figure 3.6. Screenshot for the Periodical Forecast Report by ProForecaster

3.2. Step 4: Constructing the Collaborative Neural Network

Below are the steps for creating a neural network Using Alyuda Forecaster XL:

Step 1: Load all data into an Excel sheet: the actual data as well as the internal forecast and the external forecasts.

Step 2: Click the Create Network button.



Step 3: After the button is clicked, a box (as shown in Figure 3.7) appears, and you can select your data. Choose both forecasts (i.e., internal and external) as the input data. Then choose the actual data as the target.

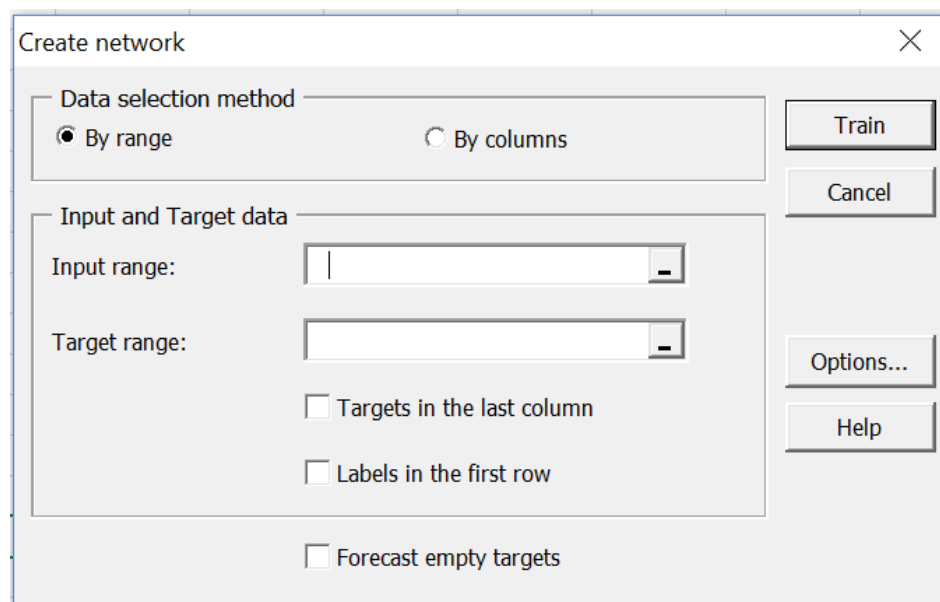



Figure 3.7. Network Creation Using Alyuda Forecaster XL

Step 4: Hit the Train button, which is shown in Figure 7to generate a performance report containing the following: actual versus forecast graph, deviation graph, input importance, input importance table, and actual versus forecasted table.

Step 5: Once you have created the network, you can start forecasting using the network by clicking the Forecast  button. Then a box as shown in Figure 3.8 will appear, and you can choose your input data and where you want the forecast to be stored.

Step 6: Hit the Forecast button, which is shown in Figure 3.8. Once you hit that button, the forecast will be stored in the chosen cells.

3.3. Step 5: Comparing Individual Forecasts

As mentioned earlier, three different criteria are used—Mean Absolute Deviation (MAD), Mean Square Errors (MSE), and Mean Absolute Percentage Error (MAPE)—to compare the neural network's output with each forecast. Below are definitions for each criterion.

3.3.1 Mean Absolute Deviation (MAD)

MAD is used to measure the difference between the values in a data set and the mean. The absolute value prevents the differences with positive sign from cancelling the ones with negative sign [25]. The MAD function can be expressed as

$$MAD = \frac{1}{n} \sum_{i=1}^n |x_i - \bar{x}| \quad (12)$$

3.3.2 Mean Square Errors (MSE)

The mean squared error is one of the most important criteria used for measuring the accuracy of an estimator or a predictor. It is useful for transmitting the concepts of accuracy, bias, and precision in statistical approximation. To use the mean squared error, a target of estimation is needed as well as a predictor that is a function of the data. [26]. The MSE function can be expressed as

$$MSE = \frac{1}{n} \sum_{i=1}^n (x_i - \bar{x})^2 \quad (13)$$

3.3.3 Mean Absolute Percentage Error (MAPE)

The MAPE measures how big the error is in terms of a percentage. Many organizations focus primarily on the MAPE when assessing forecast accuracy. According to Stellwagen (the vice president and co-founder of Business Forecast Systems, Inc. (BFS) and co-author of the Forecast Pro software product line), most people like to think in percentage terms; thus, the MAPE is easy to understand when the user doesn't know anything about the size of the demand of a certain product. For example, telling someone who doesn't know a product's demand size that we are off by 10% is easier to understand than saying "we are off by 2000 cases" [27]. The MAPE function can be expressed as

$$MAPE = \left(\frac{1}{n} \frac{|\text{Actual} - \text{Forecast}|}{|\text{Actual}|} \right) * 100 \quad (14)$$

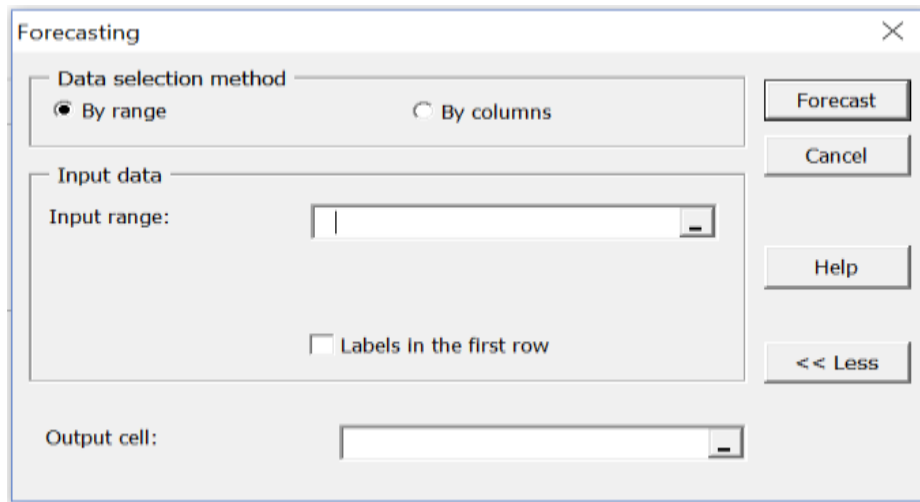


Figure 3.8. Forecasting Step Using Alyuda Forecaster XL

CHAPTER FOUR

CASE STUDY

4.1. Data Gathering

Sales data for a tuna product was gathered from Panda, one of the largest supermarket chains in Saudi Arabia. The product's weekly sales data from January of 2012 till June of 2013 is shown in Table 4.1. The sales data's distribution curve is represented in Figure 4.1. The first 71 weeks were used to find the best model. The sales data for weeks 72 to 77 were used to compare the forecasted sales generated from the neural network combination model.

Table 4.1. Sales Data for the Tuna Product

Week	Actual Qty Sold	Week	Actual Qty Sold	Week	Actual Qty Sold	Week	Actual Qty Sold
1	1049	21	545	41	751	61	793
2	916	22	695	42	810	62	902
3	873	23	398	43	543	63	616
4	880	24	545	44	850	64	617
5	833	25	553	45	943	65	511
6	806	26	602	46	758	66	770
7	887	27	614	47	821	67	836
8	747	28	649	48	891	68	724
9	765	29	573	49	918	69	522
10	619	30	440	50	846	70	555
11	723	31	337	51	749	71	780
12	792	32	466	52	1099	72	612
13	737	33	159	53	969	73	508
14	488	34	250	54	752	74	546
15	1260	35	524	55	775	75	765
16	2266	36	401	56	637	76	657
17	702	37	590	57	681	77	578
18	631	38	739	58	805		
19	511	39	671	59	873		
20	601	40	818	60	718		

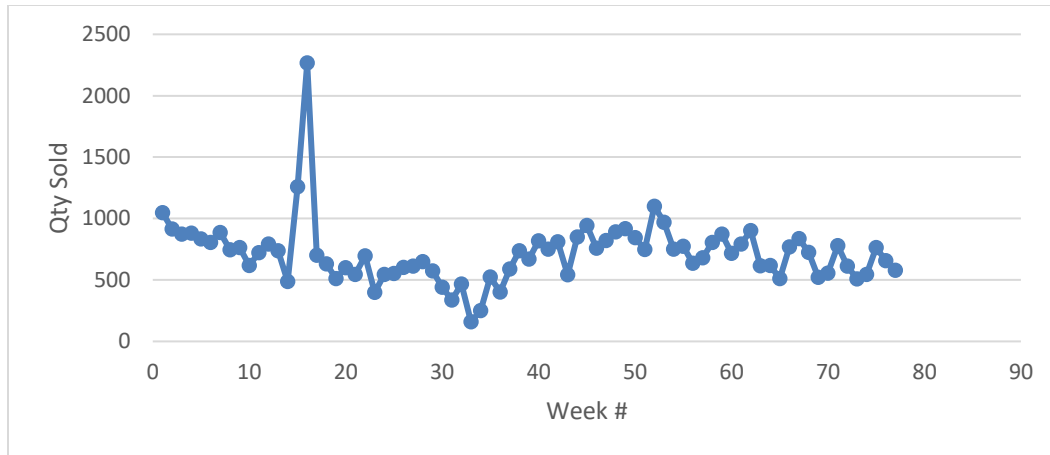


Figure 4.1. Distribution Curve of the Gathered Data (Tuna Sales)

4.2. Conducting Individual Forecasts

4.2.1 Internal Forecast

For generating a forecast for Panda, a Matlab module was created to find the best ARMA model for the sales data. For selecting the best ARMA model, the module used two information criteria: Akaike's Information Criterion (AIC), and Bozdogan's Consistent AIC (CAIC). The best- fitting ARMA model was AR(1). The parameter estimates are shown in Table 4.2. The module also plots samples ACF and PACF, which are used as qualitative model selection tools to compare. Samples ACF and PACF plots are shown in Figure 4.2.

4.2.2 External Forecast

For generating the external forecasts, proForecaster, an add-in application within Excel was used. The best three models the application proposed were used as the external forecast. The external and internal forecasts, including weeks 3 through 71, are shown in Table 4.3.

Table 4.2. Best-fitted ARMA Model for Sales Data

ARIMA(1,0,0) Model				
Conditional Probability Distribution: Gaussian				
		Standard	t	
Parameter	Value	Error	Statistic	
Constant	399.413	67.0738	5.95483	
AR{1}	0.450475	0.0513621	8.77057	
Variance	56548.1	4313.09	13.1108	

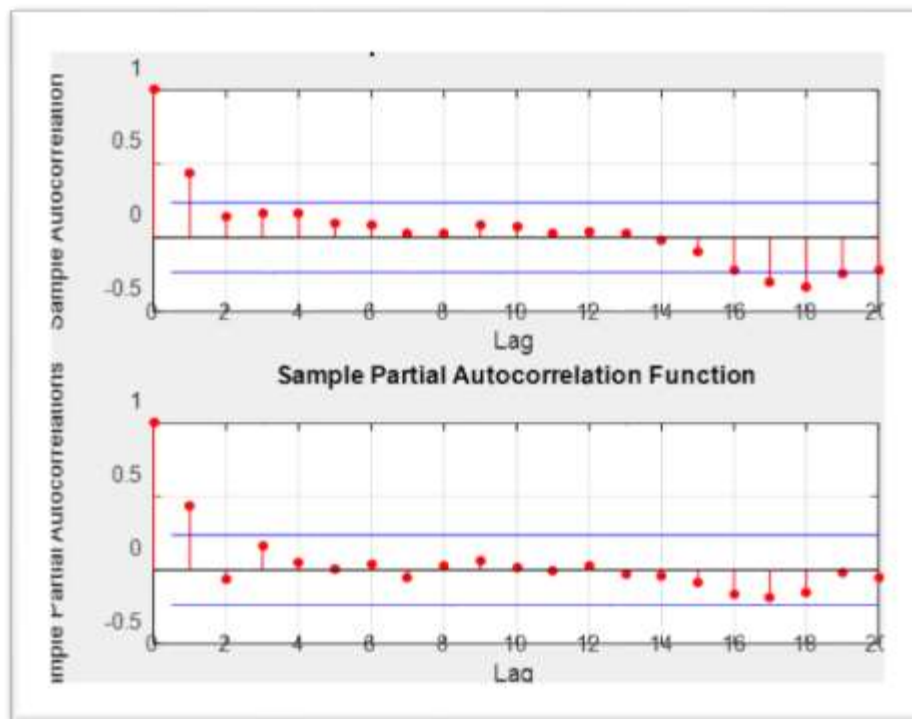


Figure 4.2. ACF and PACF Plots for the Sales Data

Table 4.3. Internal and External Forecasts Generated

Week	Actual Demand	Internal Forecast	External Forecasts Using proForecaster ADD-IN		
		AR1	External Forecast #1	External Forecast #2	External Forecast #3
3	873	812.05	824.93	718.02	916.00
4	880	792.68	818.78	719.10	903.70
5	833	795.83	815.29	719.47	896.92
6	806	774.66	805.39	719.41	878.64
7	887	762.50	794.37	719.82	857.87
8	747	798.98	798.97	720.06	866.20
9	765	735.92	780.24	719.35	832.11
10	619	744.03	770.46	720.61	812.91
11	723	678.26	740.44	720.47	757.46
12	792	725.11	735.75	721.84	747.60
13	737	756.19	742.14	720.83	760.30
14	488	731.41	738.26	720.20	753.64
15	1260	619.24	697.49	720.77	677.66
16	2266	967.01	788.42	722.93	844.21
17	702	1420.19	1005.50	717.48	1250.84
18	631	715.65	918.05	711.65	1093.87
19	511	683.66	850.90	721.06	961.49
20	601	629.61	781.65	721.79	832.65
21	545	670.15	746.41	722.95	766.40
22	695	644.92	711.82	722.07	703.08
23	398	712.49	710.80	722.57	700.77
24	545	578.70	663.41	721.20	614.18
25	553	644.92	654.07	724.12	594.39
26	602	648.53	646.99	722.63	582.55
27	614	670.60	649.95	722.53	588.12
28	649	676.00	653.72	722.04	595.52
29	573	691.77	661.92	721.91	610.81
30	440	657.53	655.93	721.59	600.00
31	337	597.62	631.59	722.39	554.24
32	466	551.22	598.68	723.79	492.11
33	159	609.33	595.11	724.79	484.64
34	250	471.04	544.27	723.61	391.51
35	524	512.03	523.86	726.74	351.04
36	401	635.46	550.07	725.66	400.50
37	590	580.05	548.88	722.90	400.65
38	739	665.19	578.66	724.07	454.80
39	671	732.31	621.66	722.11	536.08
40	818	701.68	641.84	720.70	574.67
41	751	767.90	679.70	721.31	644.26
42	810	737.72	695.57	719.96	674.79
43	543	764.30	716.73	720.57	713.46
44	850	644.02	690.17	720.06	664.71
45	943	782.32	719.93	722.54	717.70
46	758	824.21	753.40	719.67	782.14
47	821	740.87	749.30	718.86	775.23
48	891	769.25	757.12	720.50	788.32
49	918	800.79	772.72	719.93	817.69
50	846	812.95	787.93	719.32	846.38
51	749	780.51	787.76	719.08	846.27
52	1099	736.82	773.03	719.71	818.45
53	969	894.48	816.74	720.55	898.69
54	752	835.92	826.27	717.65	918.80
55	775	738.17	800.97	718.64	871.09
56	637	748.53	787.01	720.56	843.61
57	681	686.37	755.01	720.37	784.52
58	805	706.19	739.62	721.68	754.91
59	873	762.05	747.15	721.22	769.24
60	718	792.68	762.65	720.07	798.91
61	793	722.85	749.87	719.47	775.77
62	902	756.64	753.18	720.88	780.70
63	616	805.74	771.59	720.17	815.39
64	617	676.91	740.36	719.22	758.37
65	511	677.36	719.76	721.90	717.93
66	770	629.61	687.81	721.93	658.75
67	836	746.28	705.43	722.88	690.57
68	724	776.01	726.75	720.39	732.16
69	522	725.56	725.22	719.80	729.83
70	555	634.56	693.62	720.88	670.39
71	780	649.43	676.70	722.86	637.39

4.3. Conducting the Neural Network Forecasting Model

Once all the individual forecasts are obtained, they can be used to find the best neural network for predicting actual sales. To find the best network, Alyuda forecaster XL, a forecasting Excel add-in based on neural networks, is used. The forecasted sales using the neural network are presented in Table 4.4, while the actual versus the forecasted sales using the network are shown in Figure 4.3. As illustrated in Figure 4.4, the neural network diagram has 4 inputs (1 internal forecast and 3 external forecasts), 9 hidden neurons, and 1 output that is the forecast. The input data used in the neural network is divided into two sets: the learning set (83% of the data) and the testing set (17% of the data).

4.4. Comparing the Outputs

Once the forecast is generated from all the models, a comparison is conducted based on three criteria: Mean Absolute Deviation (MAD), Mean Square Errors (MSE), and Mean Absolute Percentage Error (MAPE) to determine the best-fitting model for the data. Table 4.5 shows each forecasting model's errors. The forecasting combination is the best-fitting model since it has the minimum criteria. For calculating errors, the testing set was used.

4.5. Conducting the Forecast

Based on the previous step, the best-fitting model is the neural network combination model; thus, it was used to predict future forecasts (weeks 72 to

77). The results are presented in Table 4.6. The calculated Mean Absolute Percentage Error (MAPE) for the upcoming 6 weeks was found to be **18.47%**, showing how effective the neural network combination model is. The neural network combination was better than the individual forecasts; however, the other two combining methods (i.e., linear regression combination and simple average combination) are suggested in the literature.

Table 4.4. Forecasted Sales Using the Neural Network Combination

Week	Neural Network Forecast Combination	Week	Neural Network Forecast Combination	Week	Neural Network Forecast Combination
3	790.83	26	533.35	49	752.14
4	757.75	27	615.83	50	731.28
5	726.07	28	635.83	51	870.41
6	827.64	29	687.81	52	1114.00
7	891.32	30	349.39	53	1009.66
8	724.42	31	408.34	54	743.61
9	990.58	32	480.14	55	839.92
10	1097.94	33	247.38	56	1002.03
11	657.14	34	919.37	57	678.02
12	770.00	35	436.20	58	745.73
13	678.66	36	607.44	59	814.56
14	450.19	37	620.87	60	780.64
15	771.61	38	822.29	61	406.18
16	2140.14	39	619.71	62	911.21
17	693.23	40	808.39	63	739.60
18	583.75	41	765.53	64	653.17
19	792.42	42	740.51	65	628.02
20	575.78	43	819.05	66	621.61
21	636.32	44	738.96	67	803.29
22	654.11	45	821.93	68	803.22
23	798.08	46	730.94	69	382.47
24	172.28	47	857.74	70	707.61
25	452.75	48	845.43	71	760.32

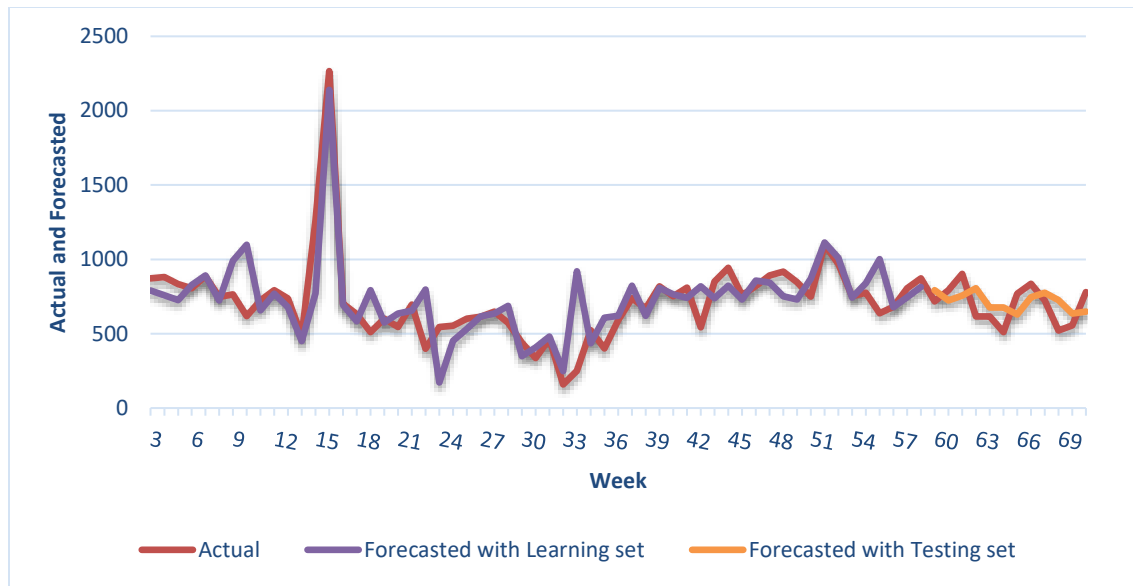


Figure 4.3. Actual vs. Forecasted Sales Using the Neural Network Model

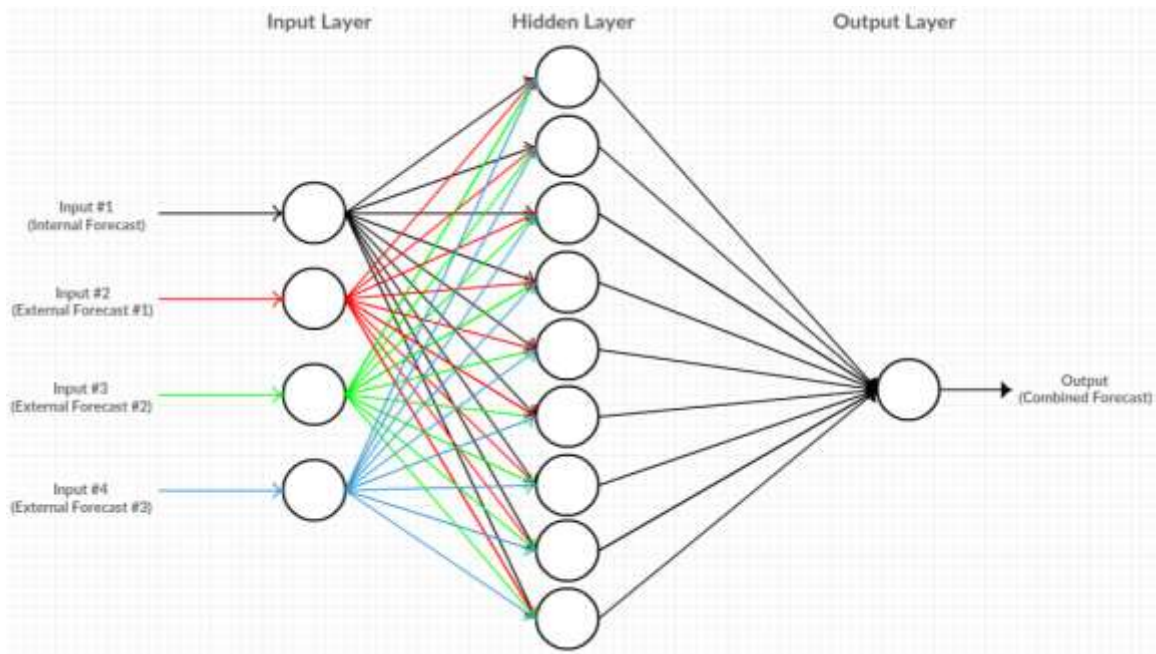


Figure 4.4. Neural Network Diagram for the Sales Data

Table 4.5. Comparison of Forecasting Models Using MAD, MSE, and MAPE

Forecast Model	MAD	MSE	MAPE
AR1	143.27	56565.46	23.87
External Forecast #1	150.25	60504.03	25.19
External Forecast #2	165.99	69789.59	29.45
External Forecast #3	161.20	64499.73	25.22
Neural Network Combination	108.97	21369.39	16.52
Linear Regression Combination	142.69	55768.24	23.68
Simple Average Combination	146.70	58403.77	24.68

Table 4.6. Forecast for the Upcoming Six Weeks

Week	Actual Demand	Neural Network Forecast Combination
72	873	739.95
73	880	742.88
74	833	707.33
75	806	663.37
76	887	628.90
77	747	611.50

CHAPTER FIVE

CONCLUSION AND RECOMMENDATIONS

5.1 Conclusion

This study explored the importance of demand forecasting and how its accuracy can impact a supply chain's profitability. Overestimation leads to overstock and added costs (e.g., holding cost, dumping cost for perishable items, and return cost). Underestimation leads to loss of potential sales and as a result less revenue. Then the following innovations in the supply chain were discussed: Vendor Managed Inventory (VMI), and Collaborative, Planning, Forecasting, and Replenishment (CPFR). CPFR aims to enhance the supply chain's efficiency by having a joint plan and by forecasting between two or more supply chain partners that will be used as the basis for production and replenishment activities. Next information sharing in the supply chain, including the types and benefits of shared information, was discussed. Also discussed was the process of combining forecasts and how it can improve forecast accuracy in terms of a better mean squared error. Then, a neural network forecasting model was proposed, which combines different forecasting models generated by different key players in a supply chain. Finally, a case study was presented to test the model. The results show that sharing point-of-sales data with key suppliers and having a combined forecast improved the accuracy and was better than each making individual forecast. These findings indicate that this model is effective for collaborative forecasting, an essential part of the collaborative planning, forecasting and replenishment (CPFR) model.

5.2 Recommendations for Future Research

In this study, different software packages were used to find the forecast: Matlab for the internal forecast and Alyuda forecaster XL for the neural network.

Designing a program that can do both activities without having to shift between software packages is recommended. Furthermore, the model presented in this study was tested on a food retailing company's sales data; however, it could be tested on other fields.

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APPENDIX

ARMA Fitting Matlab Module

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```
%USAGE: ARMA_Fitting_Enani

% Created by Abdulrahman Enani
%      Department of Industrial and Systems Engineering
%      The University of Tennessee
%      Knoxville, TN, 37996, USA

clear all;
clc;
clf;
close all
%Load or enter the time series data set
```

Import the data

```
[~, ~, raw] = xlsread('C:\Users\abood\Desktop\UTK- materials\Thesis\Sales-Tuna-  
Sys.xlsx','Sales Data','B2:B78');
```

Create output variable

```
Data = reshape([raw{:}],size(raw));
```

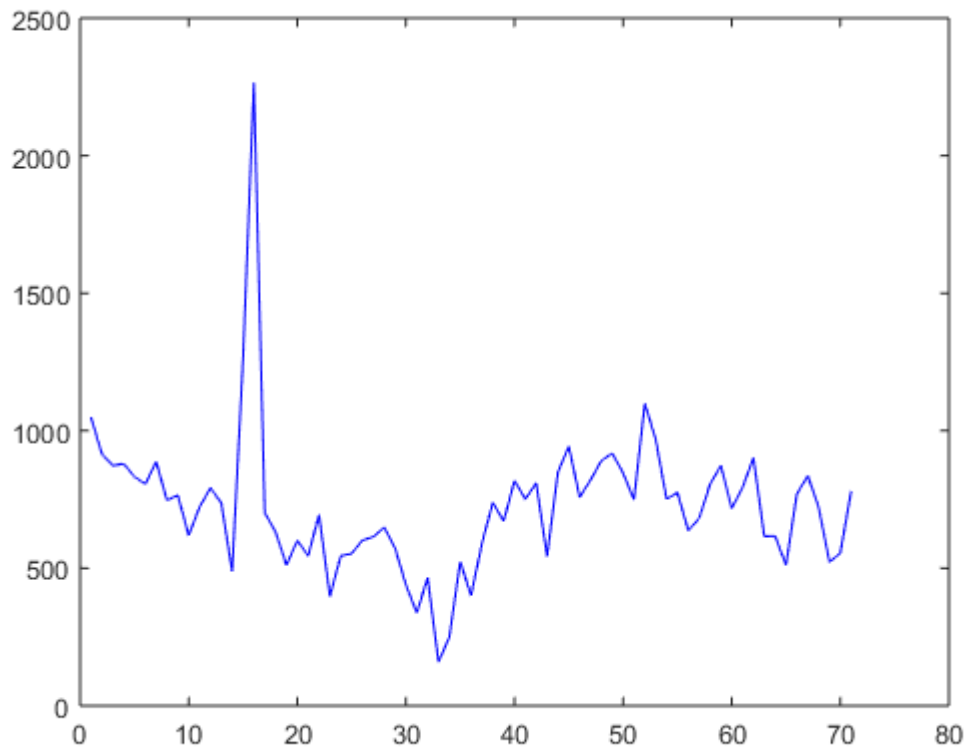
Clear temporary variables

```
clearvars raw;
```

Plot the time series

```
Y = Data(1:71);
```

```
figure (1)  
plot(Y, 'b')  
xlim([0,80])
```



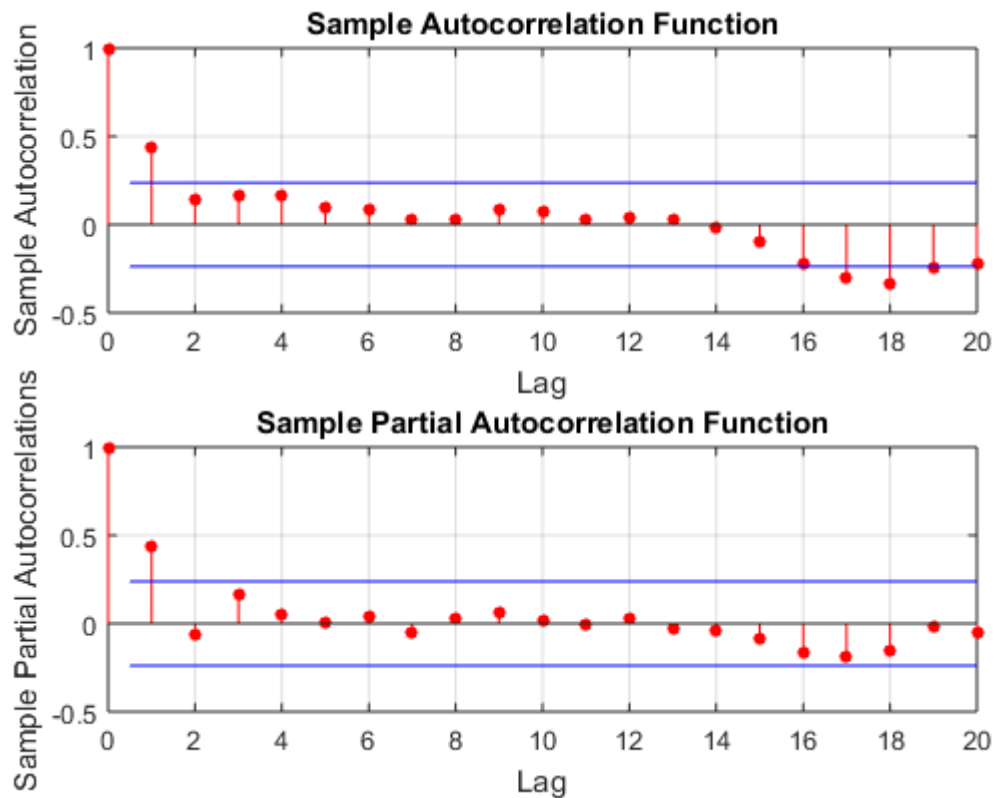
Plot the sample autocorrelation function (ACF) and the partial autocorrelation function (PACF)

```
%for the simulated data.
```

```
figure (2)  
subplot(2,1,1)  
autocorr(Y)  
subplot(2,1,2)  
parcorr(Y)
```

```
%Note that both the sample ACF and PACF decay relatively slowly.  
%This is consistent with an ARMA model. The ARMA lags cannot be selected
```

%solely by looking at the ACF and PACF, but it seems no more than four AR or MA terms %are needed.



Fit ARMA(p,q) models

%To determine the best lags, we fit several models with different lag choices. Here,
 %we fit all combinations of $p = 0, \dots, 4$ and $q = 0, \dots, 4$ (a total of 32 models). Then we
 store
 %the loglikelihood objective function values for each model fit and number of
 coefficients for
 %each fitted model.

```
pMax=4;
qMax=4;
LOGL = zeros(pMax+1,qMax+1); %Initialize
PQ=zeros(pMax+1,qMax+1);

for p = 0:pMax
    for q = 0:qMax

        Md1 = arima(p,0,q);
        [EstMd1,EstParamcov,logL] = estimate(Md1,Y,'print',false);
        LOGL(p+1,q+1)=logL;
```

```

        PQ(p+1,q+1)=p+q;
    end
end

```

Calculate the model-selection criteria

```

%Calculate the model-selection criteria. Number of parameters for ARMA(p,q)
%model is p+q+1.

```

```

LOGL = reshape(LOGL, (pMax+1)*(qMax+1),1);...
    %Elements taken column wise

PQ=reshape(PQ, (pMax+1)*(qMax+1),1);

disp('AIC Computation')

n=length(Y);
[aic,~]=aic_caic(LOGL,PQ+1,n); %numParams=PQ+1

AIC=reshape(aic,pMax+1,qMax+1)
minAIC=min(aic)
[bestP,bestQ]=find(AIC==minAIC)

disp('SBC/BIC Computation')

[~,caic]=aic_caic(LOGL,PQ+1,n);

CAIC=reshape(caic,pMax+1,qMax+1)
minCAIC=min(caic)
[bestP,bestQ]=find(CAIC==minCAIC)

```

AIC Computation

AIC =

```

    995.2194    982.1339    983.7173    985.5674    986.1617
    981.6530    983.3951    982.1344    984.0613    985.8734
    983.3777    985.3407    987.1572    982.0896    987.8046
    983.3165    983.8736    985.8413    988.1631    985.5012
    985.0178    985.5839    988.5228    990.1652    985.0309

```

minAIC =

```

    981.6530
bestP =

```

2

```
bestQ =
```

```
1
```

```
SBC/BIC Computation
```

```
CAIC =
```

```
1.0e+03 *
```

0.9985	0.9887	0.9935	0.9986	1.0025
0.9882	0.9932	0.9952	1.0004	1.0054
0.9932	0.9984	1.0035	1.0017	1.0106
0.9964	1.0002	1.0054	1.0110	1.0116
1.0013	1.0052	1.0114	1.0163	1.0144

```
minCAIC =
```

```
988.1783
```

```
bestP =
```

```
2
```

```
bestQ =
```

```
1
```

Fitting the best model

```
Md1 = arima(bestP-1,0,bestQ-1);  
EstMd1=estimate(Md1,Y);  
[res,~,logL]=infer(EstMd1,Y);  
  
stdr = res/sqrt(EstMd1.Variance);
```

```
figure (3)
```

```
subplot(2,2,1)  
plot(stdr)  
title('Standardized Residuals')  
subplot(2,2,2)  
hist(stdr)  
title('Standardized Residuals')  
subplot(2,2,3)  
autocorr(stdr)  
subplot(2,2,4)  
parcorr(stdr)
```



```
fit = estimate(Mdl,Y);
```

ARIMA(1,0,0) Model:

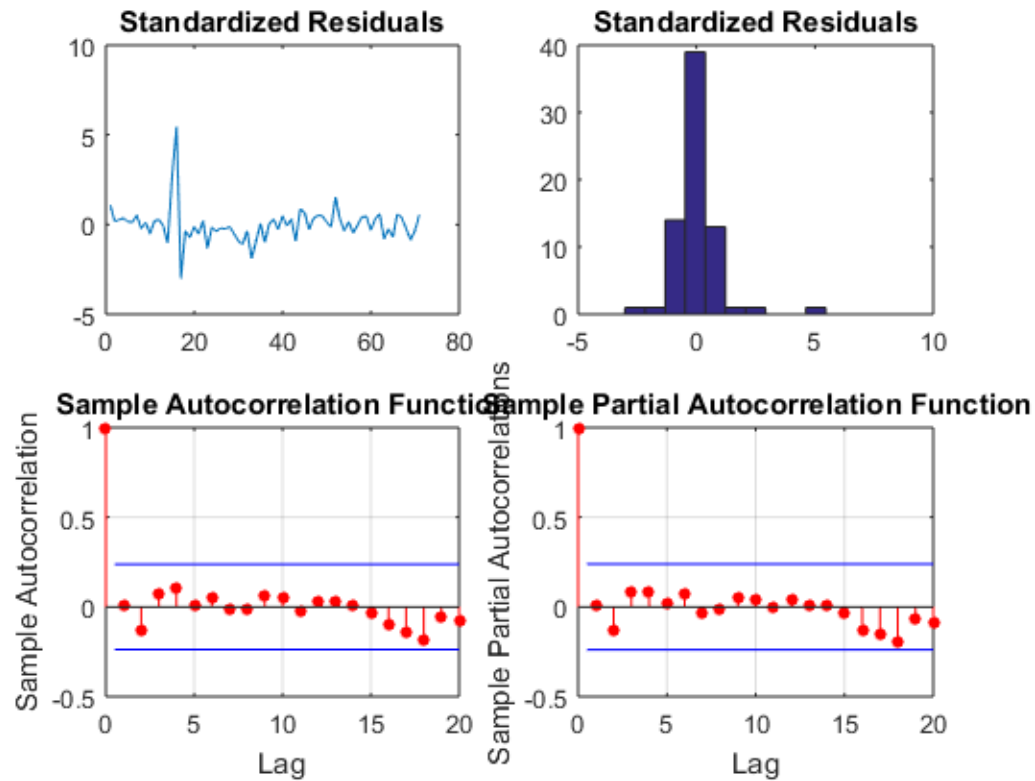
Conditional Probability Distribution: Gaussian

Parameter	Value	Standard Error	t Statistic
Constant	399.413	67.0738	5.95483
AR{1}	0.450475	0.0513621	8.77057
Variance	56548.1	4313.09	13.1108

ARIMA(1,0,0) Model:

Conditional Probability Distribution: Gaussian

Parameter	Value	Standard Error	t Statistic
Constant	399.413	67.0738	5.95483
AR{1}	0.450475	0.0513621	8.77057
Variance	56548.1	4313.09	13.1108



Finding the future forecast using the best model

%Finding the future forecast using the best model (6 coming weeks)

```
[yF,yMSE] = forecast(fit,6,'Y0',Y);
```

```
upper = yF + 1.96*sqrt(yMSE);
```

```
lower = yF - 1.96*sqrt(yMSE);
```

```
figure
```

```
lw1= plot(Y,'color',[.75,.75,.75]);
```

```
hold on
```

```
plot((Y-res),'r','Linewidth',2);
```

```
hold on
```

```
h1 = plot(n+1:n+6,yF,'r','Linewidth',2);
```

```
h2 = plot(n+1:n+6,upper,'k--','Linewidth',1.5);
```

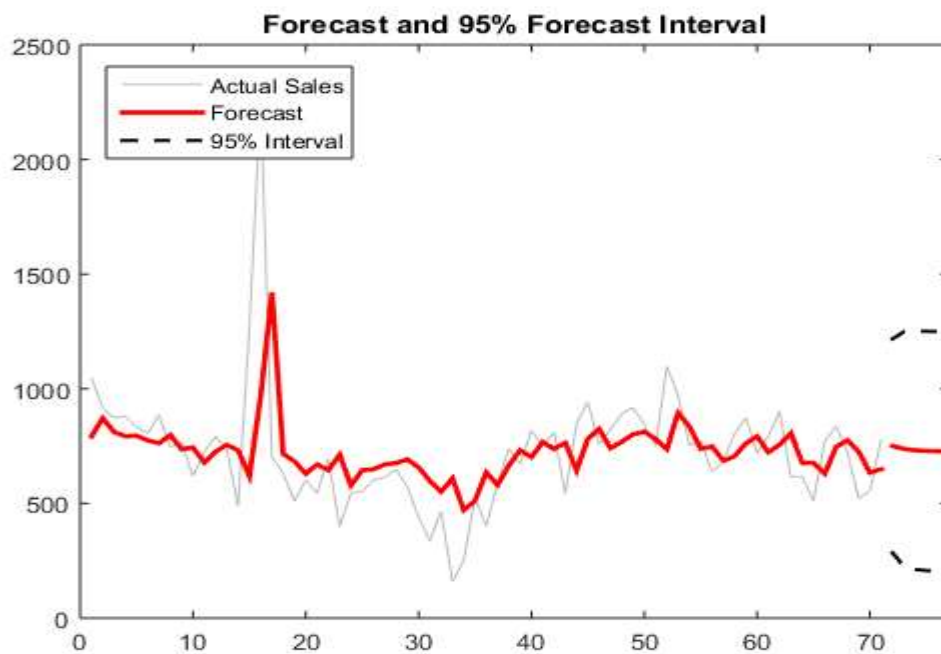
```
plot(n+1:n+6,lower,'k--','Linewidth',1.5)
```

```
xlim([0,n+6])
```

```
title('Forecast and 95% Forecast Interval')
```

```
legend([lw1,h1,h2],'Actual Sales','Forecast','95% Interval','Location','Northwest')
```

```
hold off
```



Observations of the fitted model

```
AR1= Y(3:71)-res(3:71);
```

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VITA

Abdulrahman Enani was born in Philadelphia, PA. He spent his childhood in Jeddah, a city located in the western region of Saudi Arabia. In 2007, he was admitted to King Abdulaziz University's Industrial Engineering program and received his bachelor's degree in 2012. Then he worked as an inventory controller for Panda, one of the largest retailing companies in Saudi Arabia. In 2014, he moved back to the U.S. to study Industrial Engineering at the University of Tennessee, Knoxville, where he received his master's degree in 2016. In his spare time, he enjoys cooking for friends, playing football, and lifting weights at the gym.