

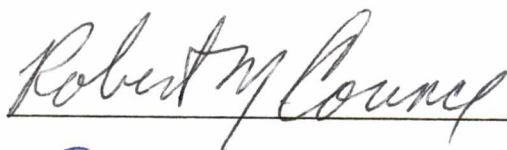
To the Graduate Council:

I am submitting herewith a thesis written by Lawrence Paul MacIntyre entitled "Process Control of a Continuous Uranyl Nitrate Evaporator." I have examined the final copy of this thesis for form and content and recommend that it be accepted in partial fulfillment of the requirements for the degree of Master of Science, with a major in Chemical Engineering.

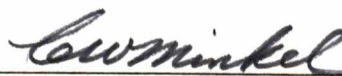


Charles F. Moore, Major Professor

We have read this thesis
and recommend its acceptance:



Accepted for the Council:



The Graduate School

PROCESS CONTROL FOR A CONTINUOUS
URANYL NITRATE EVAPORATOR

A Thesis
Presented for the
Master of Science
Degree
The University of Tennessee, Knoxville

Lawrence Paul MacIntyre

March 1984

DEDICATION

This thesis is dedicated to my wife, Patricia Ann
MacIntyre.

ACKNOWLEDGEMENTS

The author wishes to express his gratitude to all of the people who aided him in this research. He would like to thank Dr. Charles F. Moore and Dr. Stephen F. Peterson for their aid and support. He wishes to acknowledge Dr. R. M. Counce for his work on the simplified dissociation model used in this work, and Dr. Duane D. Bruns and Dr. R. M. Counce for serving on his committee.

Special recognition is given to Jeffrey D. Draper for his plotting programs which have figured greatly in this work. Finally, thanks are given to T. J. Abraham and James E. Hackney for their insights and assistance.

ABSTRACT

A continuous uranyl nitrate evaporator at the Savannah River Plant (SRP) in Aiken, South Carolina was the subject of this work. A rigorous mathematical model of the evaporator was developed. A difference equation form of the model was then constructed and used for control studies.

Relative gain analysis was done on the system in order to identify any promising multivariable control schemes. Several alternate control schemes were modeled, tuned, and compared against the scheme presently in use at SRP.

As the pneumatic specific gravity instrumentation at SRP is very noisy, the noise was simulated and used in the second phase of the control study. In this phase, alternate tuning methods and filters were investigated and compared.

Finally, recommendations were made as to what method could best be used to control the evaporator.

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LIST OF SYMBOLS

SYMBOL	MEANING
B	- Bottoms Flow Rate, lb/hr
C	- Uranium Concentration, g/liter
C(t)	- Manipulated Variable
C _p	- Heat Capacity, BTU/lb/°F
C _{p_f}	- Heat Capacity of Feed, BTU/lb/°F
F	- Feed Flow Rate, lb/hr
F _s	- Steam Flow Rate, lb/hr
H	- Height of Liquid in Evaporator, inches
H ₀	- Height of Weir Above Bottom in Evaporator, inches
K _a	- Equilibrium Constant
K _h	- Valve Constant for Bottoms Flow, lb/hr/in
K _{hat}	- Valve Constant for Hackman Hat Flow, lb/hr/in
M	- Mass of Liquid in Evaporator, lb
N	- Dead Time, hr
N _a	- Normality of Acid in Evaporator
P _a	- Equilibrium Vapor Pressure of Acid, inches water
P _c	- Pressure in Condenser, inches water
P _e	- Pressure at Liquid Surface in Evaporator, inches water
P _w	- Equilibrium Vapor Pressure of Water, inches water

R	-	Gas Constant
T	-	Temperature of Liquid in Evaporator, $^{\circ}\text{F}$
T_f	-	Temperature of Feed, $^{\circ}\text{F}$
V	-	Vapor Flow Rate, lb/hr
X	-	Output of Difference Equation
X_{ss}	-	Value of X at Steady State
a	-	Difference Equation Constant
b	-	Difference Equation Constant
dH	-	Heat of Reaction
h	-	Height of Liquid in Hackman Hat, inches
n	-	Integer Dead Time
t	-	Time, hours
x_a	-	Analytical Mole Fraction of Acid
x_s	-	Analytical Mole Fraction of Salt
x_w	-	Analytical Mole Fraction of Water
x'_a	-	Mole Fraction of Undissociated Acid
x'_w	-	Mole Fraction of Undissociated Water
x'_{a+}	-	Mole Fraction of Hydrogen Ion
x'_-	-	Mole Fraction of Nitrate Ion
α	-	Extent of Dissociation
β	-	Tuning Constant
γ'_a	-	Activity Coefficient of Undissociated Acid
γ'_w	-	Activity Coefficient of Undissociated Water
θ	-	Dead Time, hours

λ_s	-	Heat of Vaporization of Steam, BTU/lb
λ_v	-	Heat of Vaporization of Vapor, BTU/lb
ρ	-	Specific Gravity of Liquid in Evaporator
τ	-	Time Constant, hours

CHAPTER I

BACKGROUND

An evaporator used to concentrate aqueous uranyl nitrate solutions at the Savannah River Plant (SRP) in Aiken, S.C. was the subject of this investigation. The evaporator control study was chosen over several projects after taking into consideration the complexity and usefulness of the various projects to the company. This study is part of a large project to automate the Uranium-Plutonium processing facility at SRP. It was the aim of this project to choose the best control strategy for the evaporator. The primary control objective is to control the composition of the concentrate. It is necessary to ensure that no radioactivity escapes into the condenser. It is also desired to conserve energy where practical. Instrumentation is also a concern here, as the process solutions are highly radioactive, and the equipment must be operated remotely. From this, it follows that servicing faulty components is difficult. Therefore, instrumentation must be chosen that is particularly trouble-free.

A survey was made of related literature to find what direction past modelers had taken and what control methods had been tried and which methods worked best. A computer

database search for related literature was made using the Department of Energy (DOE) Energy Database, the Lockheed Engineering Database, and the DOE Central Inventory of Models. The Applied Science and Technology Index from 1965 - 1982, as well as the entire Computer and Control Abstracts were also searched for related articles.

1.1 BACON AND HOWE

David Bacon of Queens University and Gerald Howe of Millhaven Fibres published a control study of a falling film evaporator at Chemcell Ltd (1). In the original control scheme, as shown in Figure 1, the recycle was under flow control, the steam flow was under liquid temperature control, and the liquid flow rate was under liquid level control. All controllers were independent and all setpoints were constant. The Auto-Correlation factor and the Box-Pierce statistic (a white noise comparison) were used to evaluate control of the evaporator.

A purely empirical model incorporating instrument noise was developed. The primary control variable was chosen as the liquid flow rate. It was determined that the liquid temperature and the liquid level were the only input variables that exhibited significant effects on the liquid flow rate. Under the present configuration, the

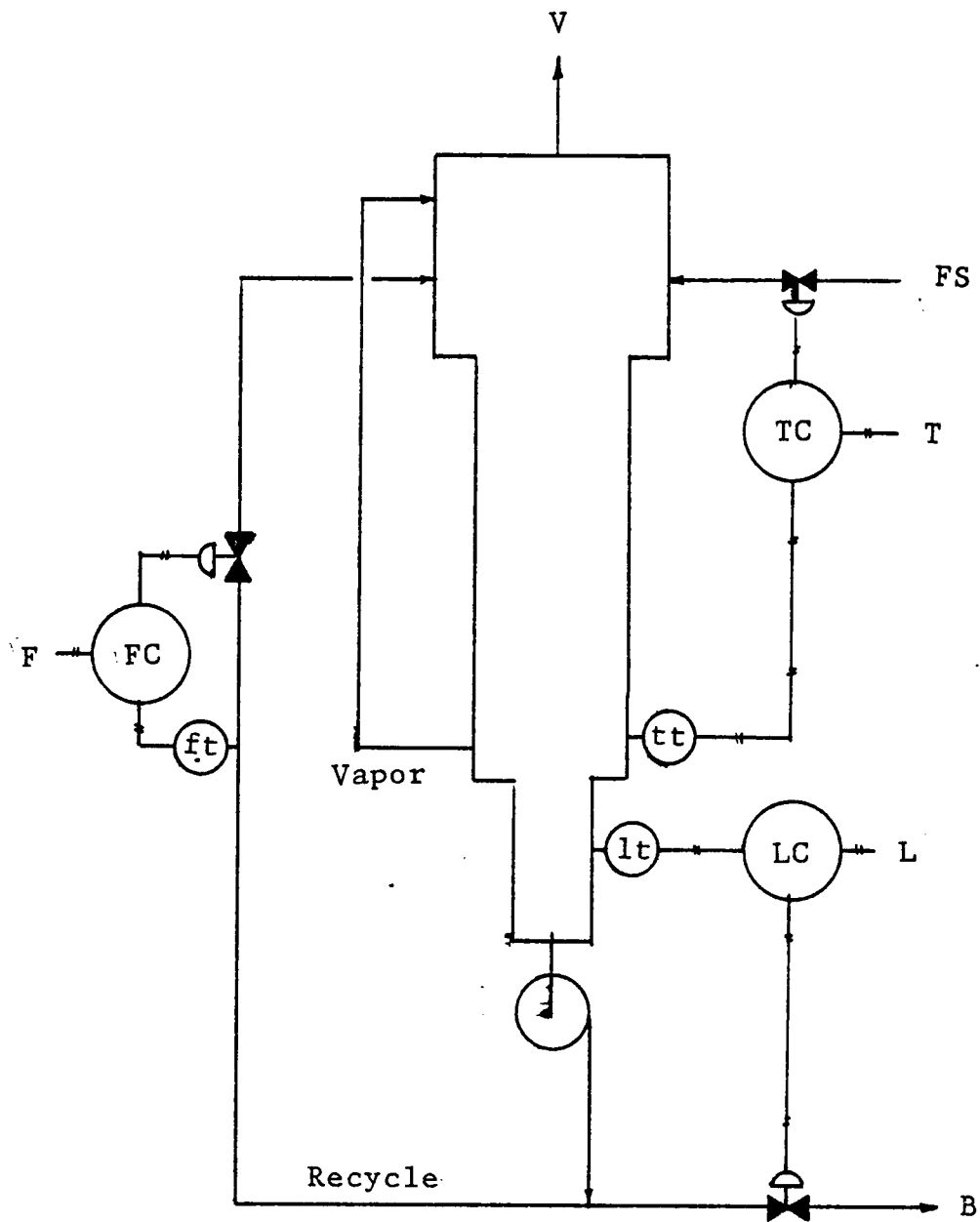


Figure 1. Falling Film Evaporator at Queens University

liquid level could only be affected by using the liquid flow rate. This meant that the liquid temperature had to be used to control the liquid flow rate. This was possible, since the liquid temperature could be used to control the liquid composition, which could, in turn, control the liquid flow rate.

It was also determined that the recycle flow rate was the only monitored variable which could be used to control the temperature. Thus, the proposed control scheme was

1. To leave the existing level control as it was.
2. To use the existing temperature control as a "slave" loop, with liquid flow rate as the "master" control.
3. To use the existing recycle flow control as a "slave" loop, with the deviation from the temperature setpoint used as the "master" loop.

The set point of the master loop was to be zero. A forty-fold improvement in variance was predicted from the stochastic model using the additional control, but no actual test data was reported.

1.2 HARVEY AND FOWLER

D. J. Harvey and J. R. Fowler, of Diamond Shamrock Corporation published a study performed on a quadruple effect chlorine-caustic evaporator (2). A schematic of the

evaporator is shown in Figure 2. The original control scheme consisted of proportional plus integral (PI) level control on the feed, PI level control on the primary vessel steam flow, PI secondary vessel level control on the primary vessel bottoms flow, and proportional plus integral plus derivative (PID) product composition control on the secondary vessel bottoms flow (product flow).

Momentum, heat, and mass balances were incorporated into a mathematical model of the evaporator. The Bernoulli equation was used to describe flow, with friction losses being described by the definition of the friction factor. Electrical flow analogies were used so that Kirchoff's Law could be applied to find all flow rates throughout the system. Experimentally determined pump curves were solved simultaneously with Bernoulli's equation by a trial-and-error process. For situations where flashing might take place due to pressure drops, an approximation between incompressible and critical flows was employed. Corporate data was used for physical property calculations. Fourth-order Runge-Kutta integration was used throughout the model.

The first result of the simulation was that several pump impellers were found to be improperly sized, so that situation was corrected first. Disturbance inputs were evaluated as to their effects, and the seriousness of

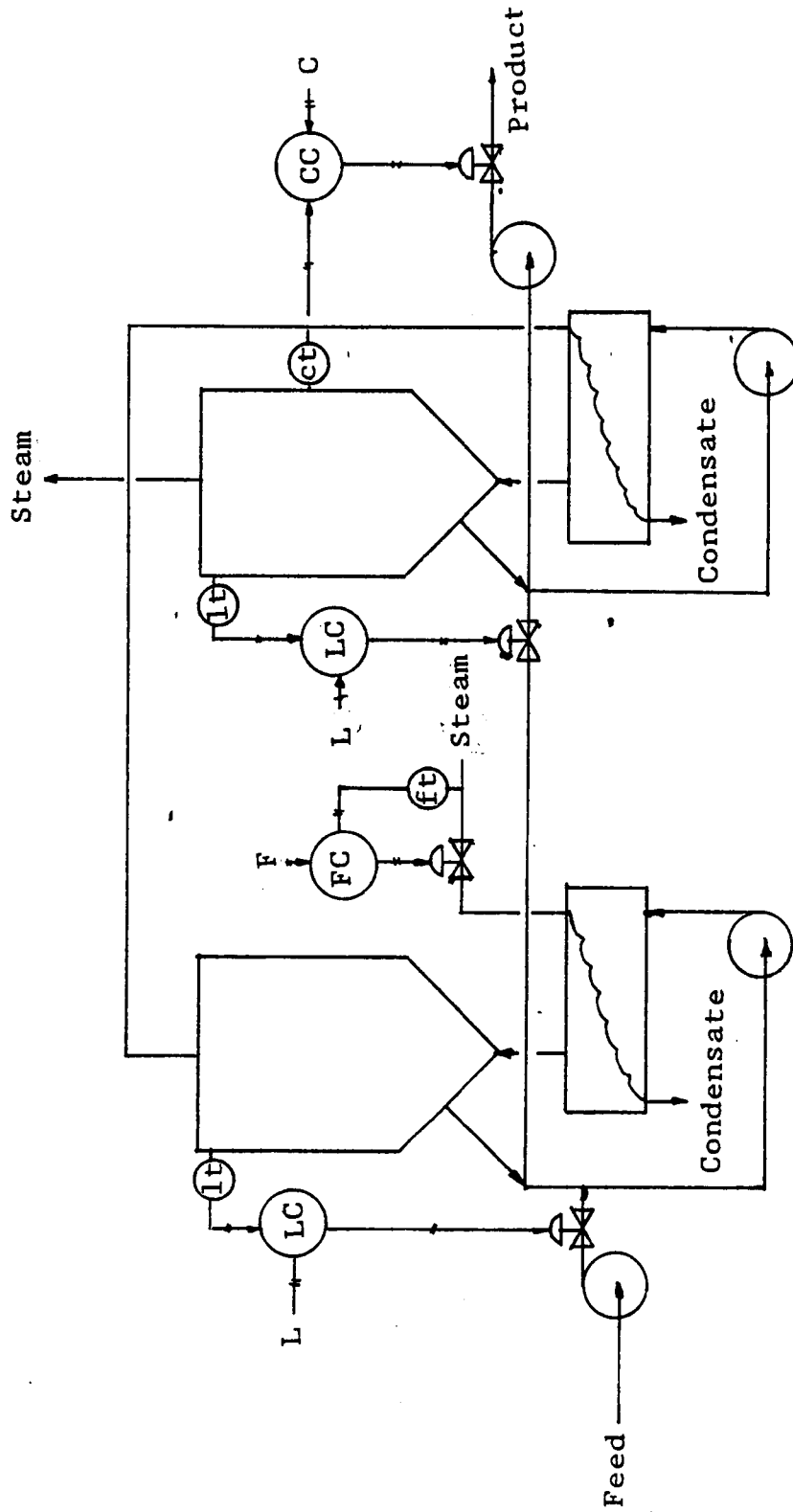


Figure 2. Quadruple-Effect Evaporator at Diamond Shamrock

those effects. Feed locations were determined, and controller modes were selected. Unsteady state operations, such as startup, shutdown, and fly-washing were also studied.

1.3 CHEN, CARTER, MILLER, AND WHEATON

Investigators at the University of Florida reported that computer control of a simulated three effect, four stage citrus juice evaporator yielded energy savings of 17% (3). Product yield was improved, also, as burning of the juice (which results in down time for cleaning of equipment, as well as discarded product) was avoided.

1.4 KLEINPETER AND WEAVER

J. A. Kleinpeter and R. E. C. Weaver, both of Tulane University, present a model of the flash separator shown in Figure 3, along with a recommended control strategy (4,5). The model is quite involved, as it incorporates the Whitman Film Theory along with mass and energy balances. Ideal behavior of liquids and vapors was assumed, as was perfect mixing. Equations of state were used for densities, fugacities, and enthalpies. A fourth-order Runge-Kutta numerical integration was used to solve the resulting equations.

The model was then rewritten in linearized form,

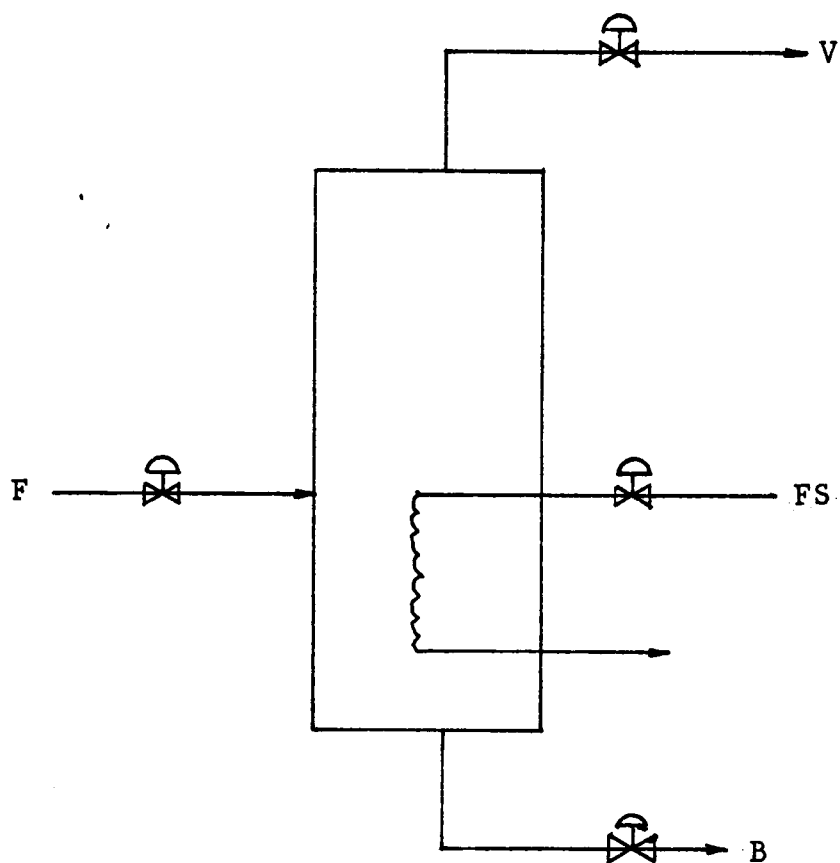


Figure 3. Flash Separator of Kleinpeter and Weaver

retaining only the first-order terms in the Taylor series expansion of each non-linearity. LaPlace transformation of the resulting linear equations was undertaken and the model then yielded a vector-matrix equation, namely

$$s * y(s) = A * x(s) + B * y(s)$$

where $x(s)$ represents both control inputs and disturbance inputs, $y(s)$ represents all state variables, and A and B are constants.

The controller was formed as

$$x(s) = F_1 * x(s) + F_2 * D(s) + F_3 * y(s) + F_4 * C(s) + F_4 * R(s)$$

where $x(s)$ represents the manipulated inputs, $D(s)$ represents the disturbance inputs, $y(s)$ represents the controlled state variables, $C(s)$ represents all other state variables, $R(s)$ represents the setpoint vector, F_1 decouples the manipulated inputs, F_2 is a feedforward term to compensate for the disturbance inputs, F_3 decouples the non-controlled state variables from the controlled state variables, and F_4 decouples the controlled state variables. It is noted that the resulting controller incorporates no dynamic elements.

The proposed controller was then compared for level, pressure, and temperature control against Ziegler-Nichols tuned PID controllers. It was found that for disturbance tuning, the PID controllers performed almost as well as

the structural analysis control. However, when compared for set point changes, or servo control, the PID controllers produced considerable disturbances in the non-monitored state variables, although they did control the control state variables well.

When structural analysis was attempted for composition control, it was found that the matrix A was singular, due to implicit coupling. The time domain description was utilized, and a similar procedure was performed to develop a control strategy. It was found that best control was obtained by deleting F_3 from the controller. Good disturbance control was available, but the servo control performance was not as good as that of the multiloop controller.

1.5 NEWELL, FISHER, AND SEBORG

R. B. Newell, D. G. Fisher, and D. E. Seborg, all of the University of Alberta, have published a series of papers on modeling of a double-effect evaporator and subsequent control studies (6,7,8). Each effect was subdivided into five subsystems; steam chest, heat transfer surface, solution holdup, vapor space, and heat capacity of the evaporator itself. Density and enthalpy balances were written for the steam chest and the vapor space. A lumped-parameter heat balance was used to

describe the heat transfer surface, as well as the heat capacity of the equipment. Mass, solute, and energy balances were written for the solution holdup. Boiling dynamics were ignored and vapor-liquid equilibrium was assumed. Physical properties were calculated using empirical relationships, and the flow equations for the entire system were written. CSMP was used to write the simulation.

The resulting tenth-order nonlinear model (10NL) was then linearized numerically, yielding a tenth-order linear model (10L) of the form

$$\dot{x} = A * x + B * u$$

$$v = C * x$$

Some of the faster relationships were made steady-state to yield two additional models, 5NL and 5L. Further reductions were undertaken, resulting in three more models, 3LR, 3LD, and 2LD. It was found that the lower order models not only deviated from experimental data in their dynamic behavior, but that they also exhibited significant steady state offset. However, the lower-order models might find application for cases where the neglected relationships are unimportant. For example, liquid holdup might not be an important consideration if an additional level control system is applied to the evaporator.

Conventional multiloop control, predictive control, feedforward control, and optimal multivariable feedback control were evaluated with the multivariable control performing best and the multiloop control giving the poorest control. The other two methods fell in the order presented above.

The multiloop control system utilized product composition control on the feed, and cascaded level-flow loops on both evaporator vessels as shown in Figure 4. The feedforward control system utilized a control law of the form

$$u(iT) = K_{fb} * x(iT) + K_{ff} * d(iT)$$

where u represents the control vector, K_{fb} represents the feedback control matrix, K_{ff} represents the feedforward control matrix, x represents the state vector, d represents the load vector, and iT represents the particular point in time.

The multivariable controller took the form

$$u(iT) = K_{fb} * x(iT) + K_m * y_m(iT) + K_{sp} * y_{sp}(iT) + K_{ff} * d(iT)$$

where K_m represents a matrix of constants, y_m represents the model results, K_{sp} represents a matrix of constants, and y_{sp} represents the setpoint.

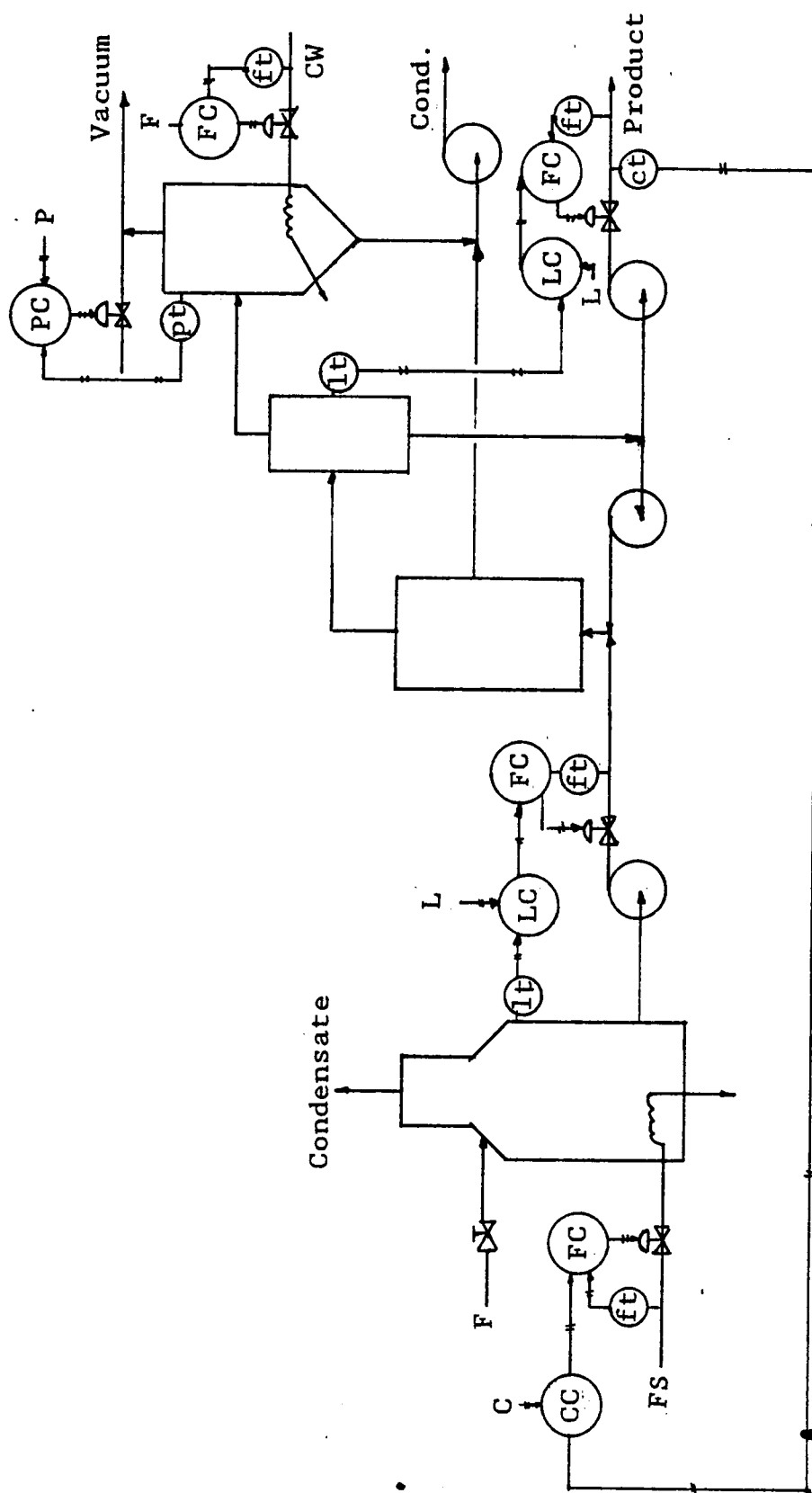


Figure 4. Evaporator at University of Alberta

CHAPTER II

DESCRIPTION OF EVAPORATOR

The continuous evaporator is a thermosiphon type evaporator with an outboard reboiler. Feed is controlled by a Hackman Hat flow controller. The evaporator is shown in Figure 5 and the Hackman Hat is shown in Figure 6. The hat is simply a baffled vessel with an orifice at its bottom. Flow into the hat is under level control. With a constant level in the vessel, there is a constant flow into the evaporator from the hat. Feed from the hat enters the evaporator at the bottom of the reboiler. The liquid flows up through the tube side of the reboiler, through a large duct to the de-entrainment column. A smaller duct connects the de-entrainment column to the bottom of the reboiler.

Liquid exits the evaporator by gravity flow through a weir on the side of the de-entrainment column. Vapor flows up through a demisting tray into the condenser. The two demisting trays are dry bubble cap trays that drain through a downcomer into the column. The scrubbing tray is a bubble cap tray that maintains an inch of water for scrubbing entrained particulates from the vapor stream, and also drains through a downcomer into the column.

The vapor flows up through the center of the

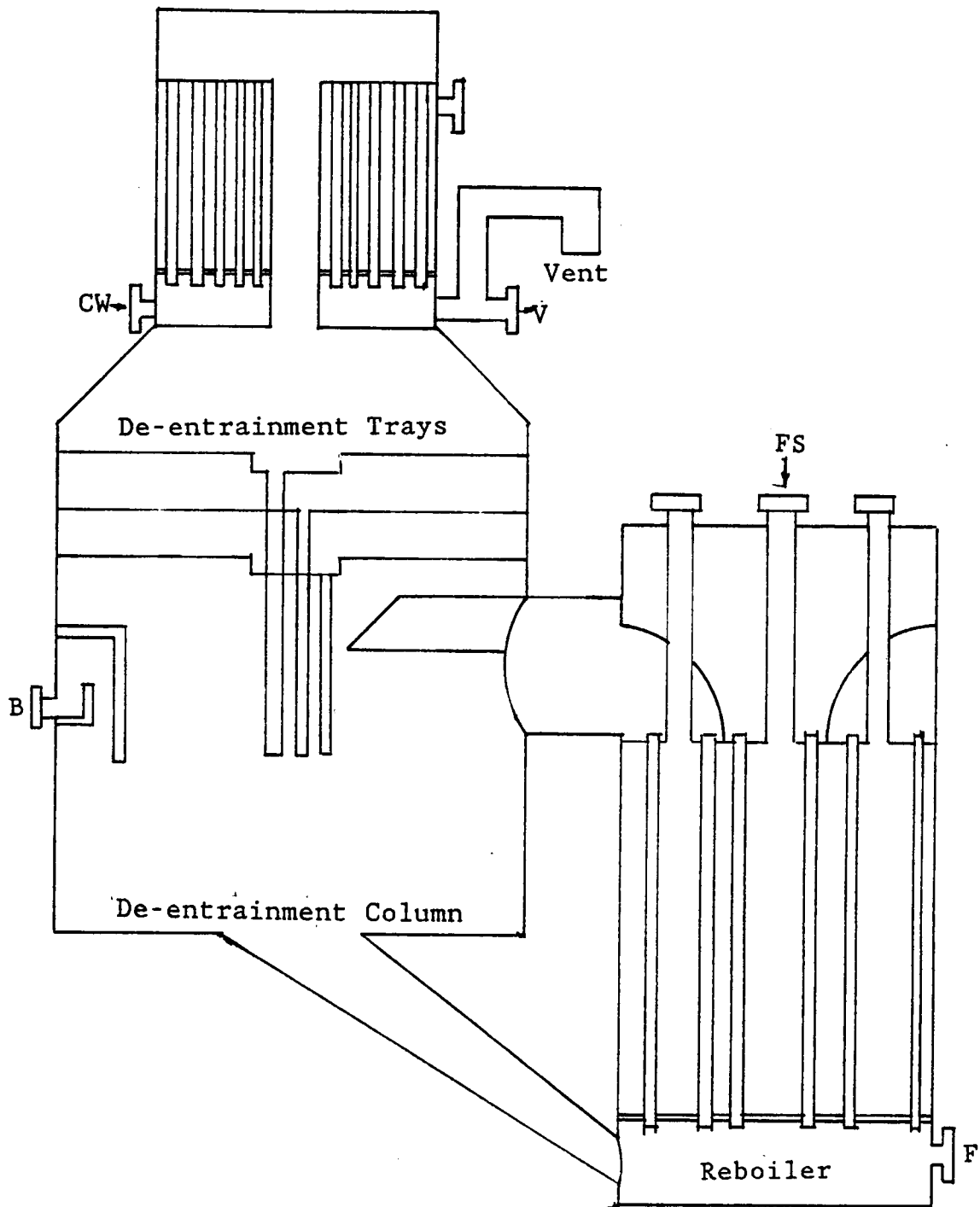


Figure 5. Continuous Evaporator at SRP

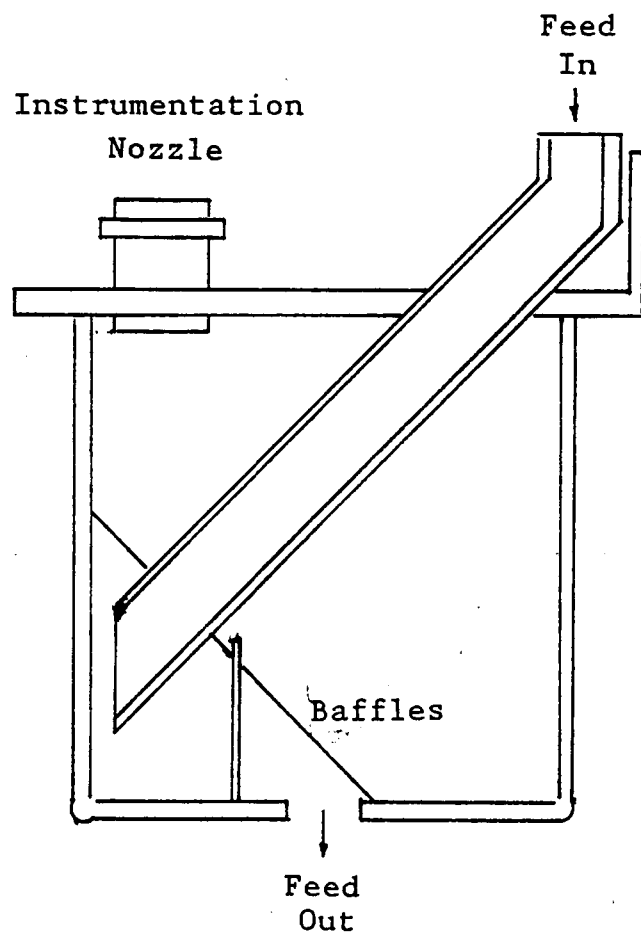


Figure 6. Continuous Evaporator Feed Connection
(Hackman Hat)

condenser and down through the tube side. The resulting liquid flows out by gravity flow. The liquid line is connected to the process vent, which is maintained at approximately one inch of water below atmospheric pressure. An overflow line is provided beyond the vent connection.

The evaporator is intended to concentrate uranyl nitrate solutions for further processing. Since a large percentage of steam use at SRP is in evaporation and DuPont experience is that advanced control techniques can typically save 10% on steam use, the evaporator is a logical candidate for this study. It was also felt that the project would be worthwhile for the knowledge gained about the process. Also, the controller now on the evaporator performs poorly, exhibiting oscillatory behavior.

CHAPTER III

MODEL DEVELOPMENT

Since the evaporator is production equipment on a tight schedule, it is unavailable for testing. Therefore the construction of a rigorous mathematical model was necessary. The bases of the model are differential mass and energy balances, as follows.

3.1 MASS BALANCE

The mass balance was formulated as

$$F - B - V = dM/dt$$

where F is the feed flow rate, expressed in lb/hr, B is the bottoms flow rate, expressed in lb/hr, V is the vapor flow rate, expressed in lb/hr, and M is the mass of the solution in the evaporator, expressed in lbs.

Perfect mixing was assumed for the liquid in the evaporator for use in composition calculations. This is a good assumption because the thermosiphon action between the de-entrainment column and the reboiler vessel provides excellent mixing.

3.2 ENERGY BALANCE

The energy balance was written in the following form:

$$F * T_f * C_{p_f} + F_s * \lambda_s - V * \lambda_v - B * T * C_p = M * C_p * dT/dt$$

where T_f is the feed temperature, expressed in degrees fahrenheit, C_{p_f} is the heat capacity of the feed, expressed in BTU/lb/°F, F is the steam rate, expressed in lb/hr, λ_s is the latent heat of vaporization of the steam, expressed in BTU/lb, λ_v is the latent heat of vaporization of the vapor, expressed in BTU/lb, T is the temperature of the liquid in the evaporator, expressed in degrees fahrenheit, and C_p is the heat capacity of the liquid in the evaporator.

3.3 VAPOR - LIQUID EQUILIBRIUM

The vapor-liquid equilibrium was calculated using equations developed for the $Mg(NO_3)_2 - HNO_3 - H_2O$ system by Thompson, Derby, Stalzer, Counce, Jubin, and Barker (9). They investigated three potential models: a full dissociation model, a simplified model, and a pseudobinary model. It was determined that the simplified dissociation model gave best agreement with experimental data. Therefore, the evaporator model included the simplified dissociation model. While it is true that the evaporator

is used for the $\text{UO}_2(\text{NO}_3)_2 - \text{HNO}_3 - \text{H}_2\text{O}$ system, this model is the best available, and should serve satisfactorily.

Dissociation

The simplified dissociation model predicts that the nitric acid will not fully dissociate, and expresses the equilibrium as

$$K_a = (X'_{a+} * x'_{-})/x'_a$$

where X'_{a+} is the mole fraction of the hydrogen ion, X'_{-} is the mole fraction of the nitrate ion, and X'_a is the mole fraction of the undissociated nitric acid. This approximation is valid at low acid concentrations, which fits the evaporator well. The equilibrium constant is expressed as

$$K_a = A \exp(-dH/R * T)$$

where A is a constant, dH is the heat of reaction, R is the gas constant, and T is the temperature in degrees centigrade. The mole fractions of the individual species can be expressed as a function of the analytical mole fractions and the extent of dissociation of the acid, α .

It is assumed that the salt is totally dissociated, giving

$$X'_{a+} = (\alpha * X) / (1 + \alpha * X + 2 * X)$$

$$X'_{-} = (\alpha * X + 2 * X) / (1 + \alpha * X + 2 * X)$$

$$X'_a = (1 - \alpha) * X / (1 + \alpha * X + 2 * X)$$

$$X'_w = X / (1 + \alpha * X + 2 * X)$$

where the w refers to water and the unprimed X's refer to

the analytical mole fraction, or the number of moles of the compound present in the solution. By substitution of these equations into the simplified equilibrium expression we get

$$K_a = (2 * \alpha * X_a + 2 * \alpha * X_s) / (1 + \alpha * X_a + 2 * X_s)(1 - \alpha)$$

Vapor Pressures

Given the analytical mol fractions and the temperature, the dissociated mol fractions can be calculated. The following Antoine equations were then used to find the equilibrium vapor pressures of water and acid:

$$\log_{10} P_w = 7.949 - 1657.4 / (T + 227.1)$$

$$\log_{10} P_a = 7.616 - 1486.2 / (T + 230.0)$$

where T is expressed in degrees centigrade, P_a is the equilibrium vapor pressure of the acid, and P_w is the equilibrium vapor pressure of the water.

Activity Coefficients

Next, the activity coefficients were calculated. Assuming the effect of pressure to be negligible, the natural logarithms of the activity coefficients can be approximated by a second order polynomial expression in X_a and X_s as

$$\ln \gamma'_a = -2.52 + 6.21 X_a - 3.10 X_a^2 + 23.83 X_s - 24.20 X_s^2 - 15.8 X_a * X_s$$

$$\ln \gamma'_w = -0.17 X_a - 3.62 X_a^2 - 4.47 X_s - 15.83 X_s^2 - 28.20 X_a * X_s$$

Total Pressure

The total pressure at the liquid surface in the evaporator can then be expressed as

$$P_t = \gamma'_a * X'_a * P_a + \gamma'_w * X'_w * P_w$$

3.4 VAPOR FLOW

The valve equation is then used to relate vapor flow to the pressure differential between the pressure at the liquid surface as found from the vapor-liquid equilibrium and the pressure at the top as maintained by the process vent:

$$V = 9185.0 \sqrt{(P_e - P_c)}$$

where P_e is the pressure at the liquid surface, expressed in inches of water pressure, and P_c is the pressure in the condenser, also expressed in inches of water pressure.

3.5 SPECIFIC GRAVITY

The specific gravity was calculated from an equation obtained at SRP:

$$0.001345 C = \rho - 1.0042 + 0.000001(8.4 \rho - 2.4)T^2 - 0.01(0.00314 C + 2.51)Na$$

where T is the temperature expressed in degrees centigrade, ρ is the specific gravity of the solution expressed in g/ml, C is the uranium concentration expressed in grams per liter, and Na is the normality of the acid in the solution.

3.6 COOLING WATER TEMPERATURE

The exit temperature of the cooling water was calculated from an energy balance assuming total condensation, which operating practice indicates is the case, as the exit temperature of the cooling water is kept at or below 50 degrees centigrade.

3.7 TEMPERATURE

The energy balance was implemented in the z-transform form in order to promote stability:

$$T = T \exp(-dt/\tau) + (1 - \exp(-dt/\tau))((F * T_f * Cp_f / B * Cp) - (V * \lambda_v / B * Cp) + (F * \lambda_s / B * Cp))$$

where $\tau = M / B$.

3.8 BOTTOMS FLOW

The bottoms flow was determined using the valve equation to relate the liquid height in the weir to flow:

$$B = K \sqrt{(H - H_0)}$$

where K is the valve constant, H is the liquid height in

the evaporator, expressed in inches, and H_0 is the height of the weir above the bottom of the evaporator, also expressed in inches.

3.9 IMPLEMENTATION

The model was implemented on a DEC-10 computer with a step time of 1 second. The major inputs were identified as feed flow, steam flow, feed composition, feed temperature, and the vent pressure. The possible control variables were identified as being pressure, temperature, specific gravity, liquid height, vapor flow, and bottoms flow. The effect of each input on each output was observed and graphed by computer.

3.10 EFFECT OF VENT PRESSURE DISTURBANCE

It was found that the effect of a vent pressure disturbance could be neglected, as the initial effect was minimal, and the system quickly returned almost to the undisturbed condition, as can be seen from the effect on the vapor flow rate of a decrease of one inch of water pressure in the condenser in Figure 7.

3.11 EFFECT OF FEED FLOW DISTURBANCE

The effect of a feed increase on the specific gravity can be seen in Figure 8. The temperature shows an initial

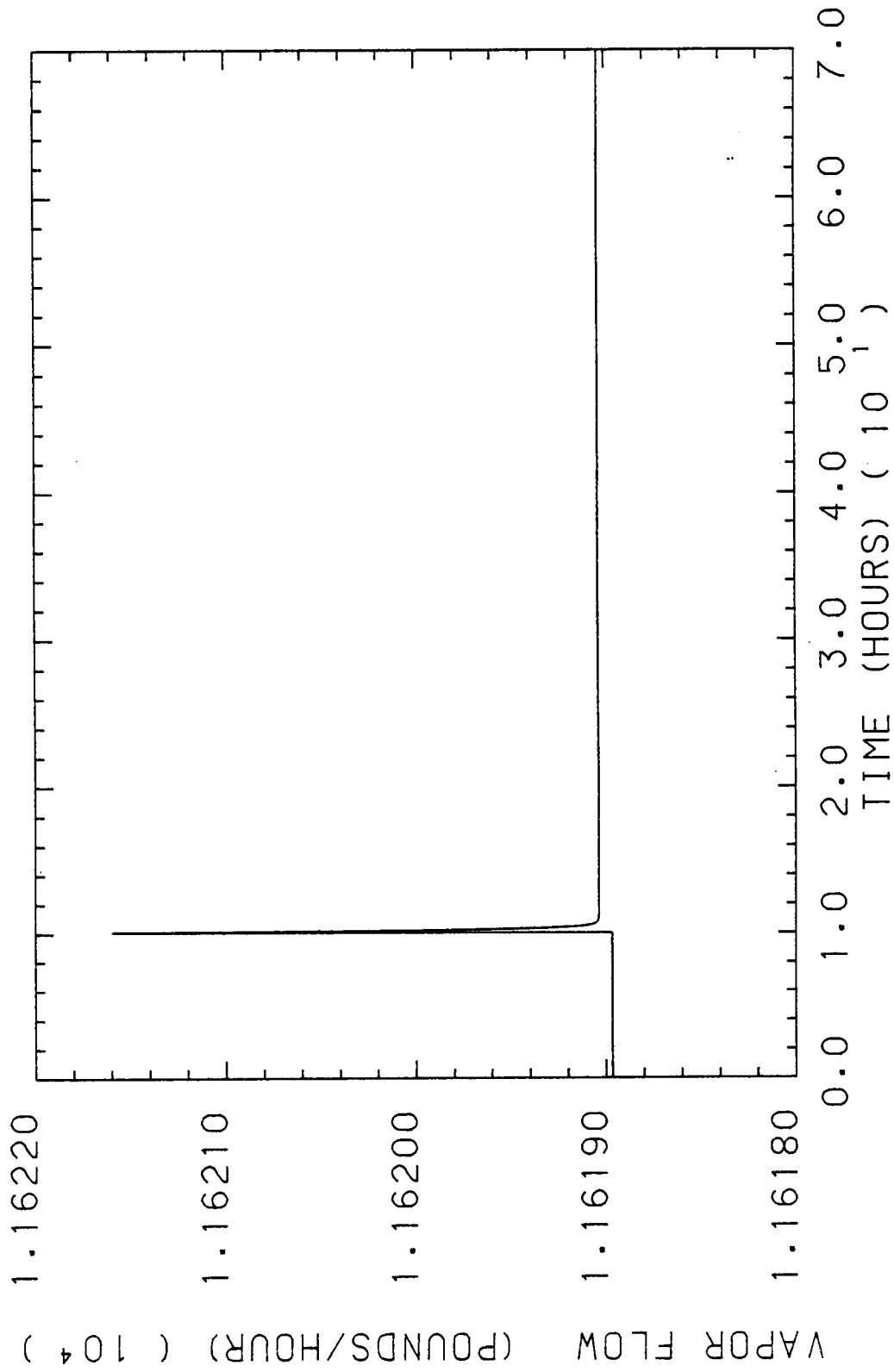


Figure 7. Effect of Vent Pressure Decrease on Vapor Flow

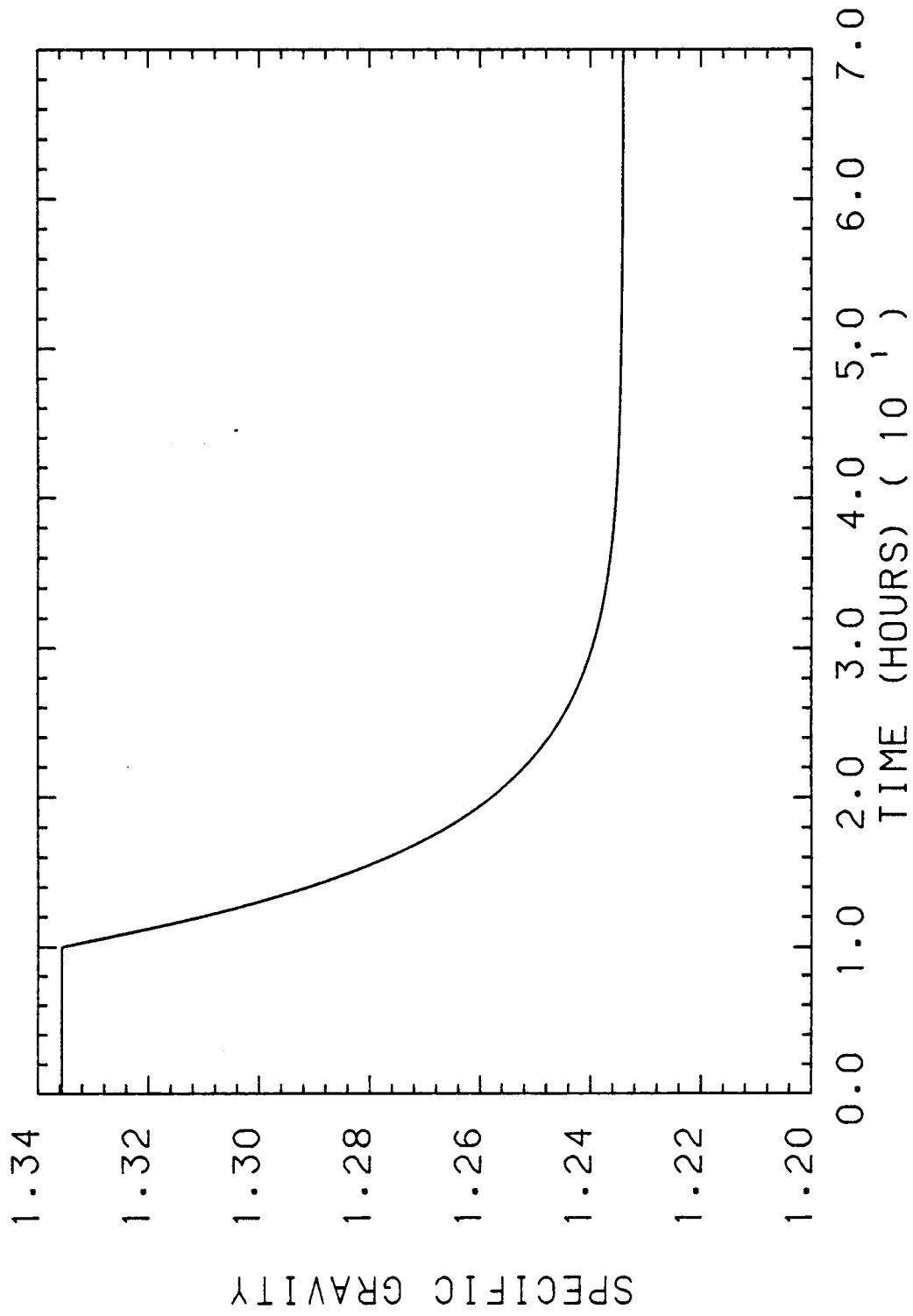


Figure 8. Effect of Feed Increase on Specific Gravity

rise because the feed is an important contributor to the heat balance, followed by a pseudo-first order decrease, as shown in Figure 9.

The pressure shows the same initial increase, followed by a large decrease due to the decreased heat/feed ratio. This is followed by a slow pseudo-first-order increase. This is shown in Figure 10. The increase is caused by the increase in nitric acid concentration and the decrease in the salt concentration. The vapor rate, as shown in Figure 11, naturally follows the pressure.

The liquid height shows an immediate rise followed by a pseudo-first order decrease due to the vapor rate increase, as shown in Figure 12. The bottoms flow follows the liquid height. This is shown in Figure 13.

3.12 EFFECT OF STEAM FLOW DISTURBANCE

The effect of a steam decrease is essentially the same as the effect of a feed increase, as can be seen from Figures 14, 15, 16, 17, 18 and 19.

3.13 EFFECT OF FEED TEMPERATURE DISTURBANCE

The effect of a feed temperature increase is analogous to the effect of a steam increase, as can be seen from Figures 20, 21, 22, 23, 24 and 25.

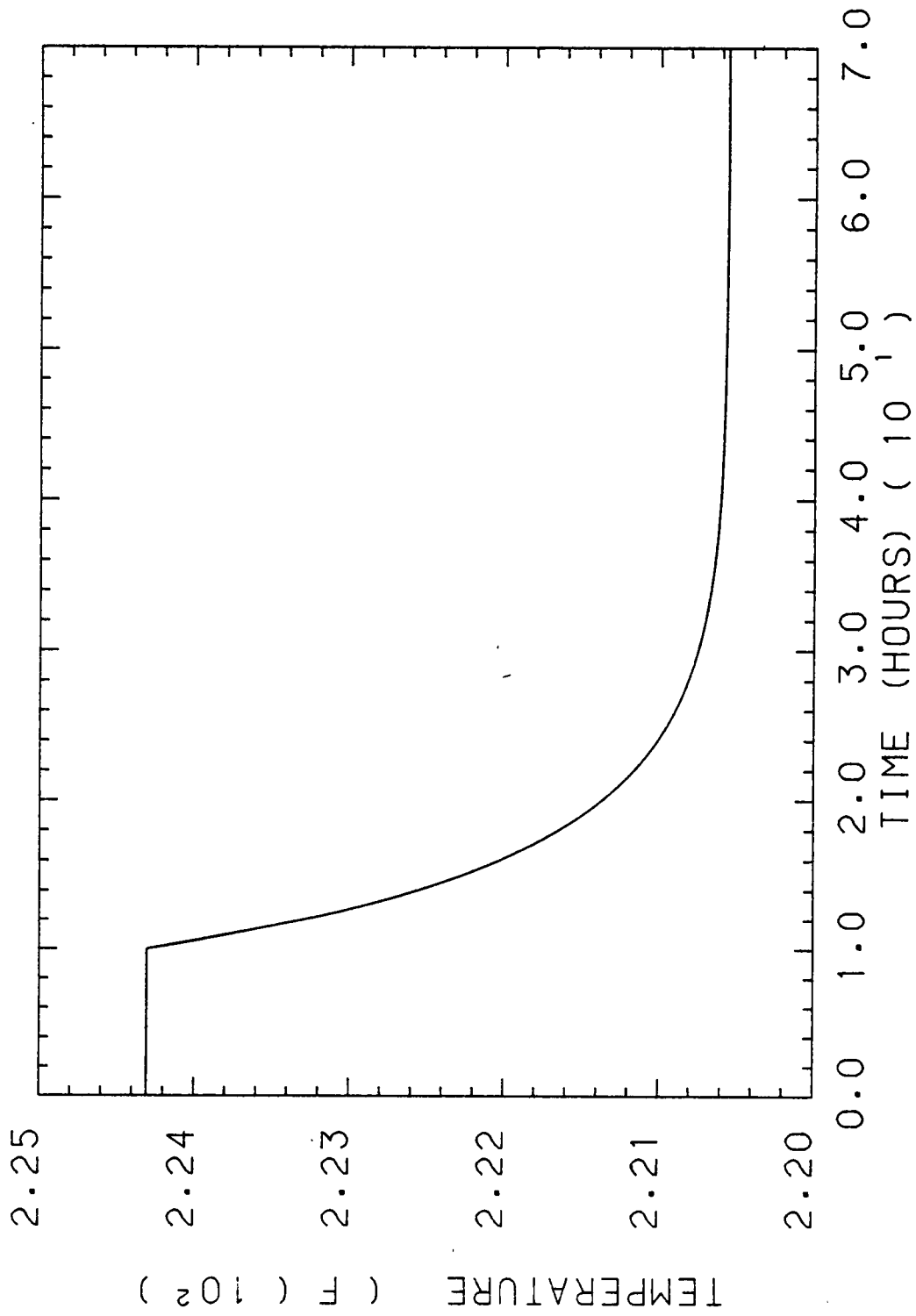


Figure 9. Effect of Feed Increase on Temperature

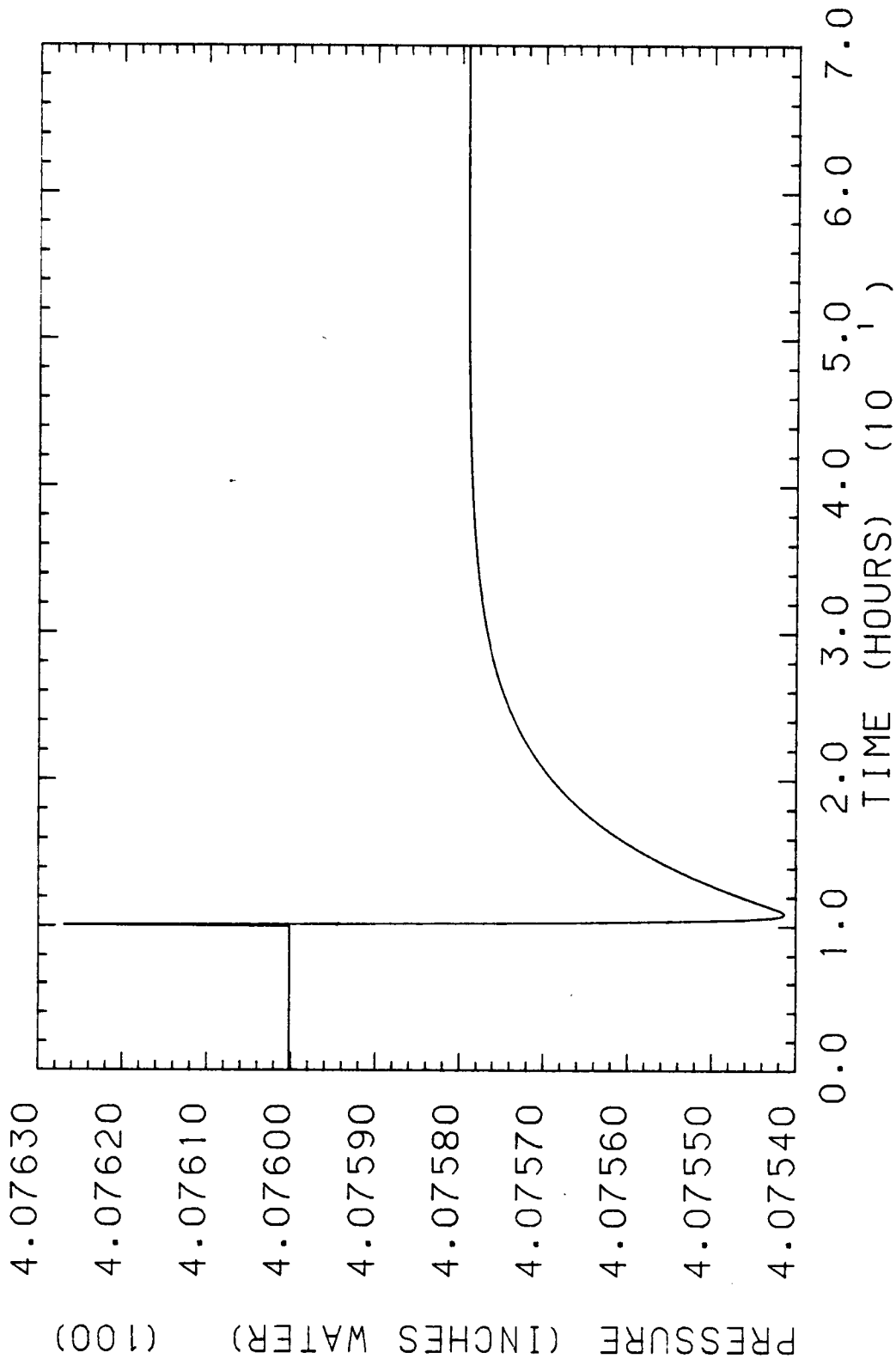


Figure 10. Effect of Feed Increase on Pressure

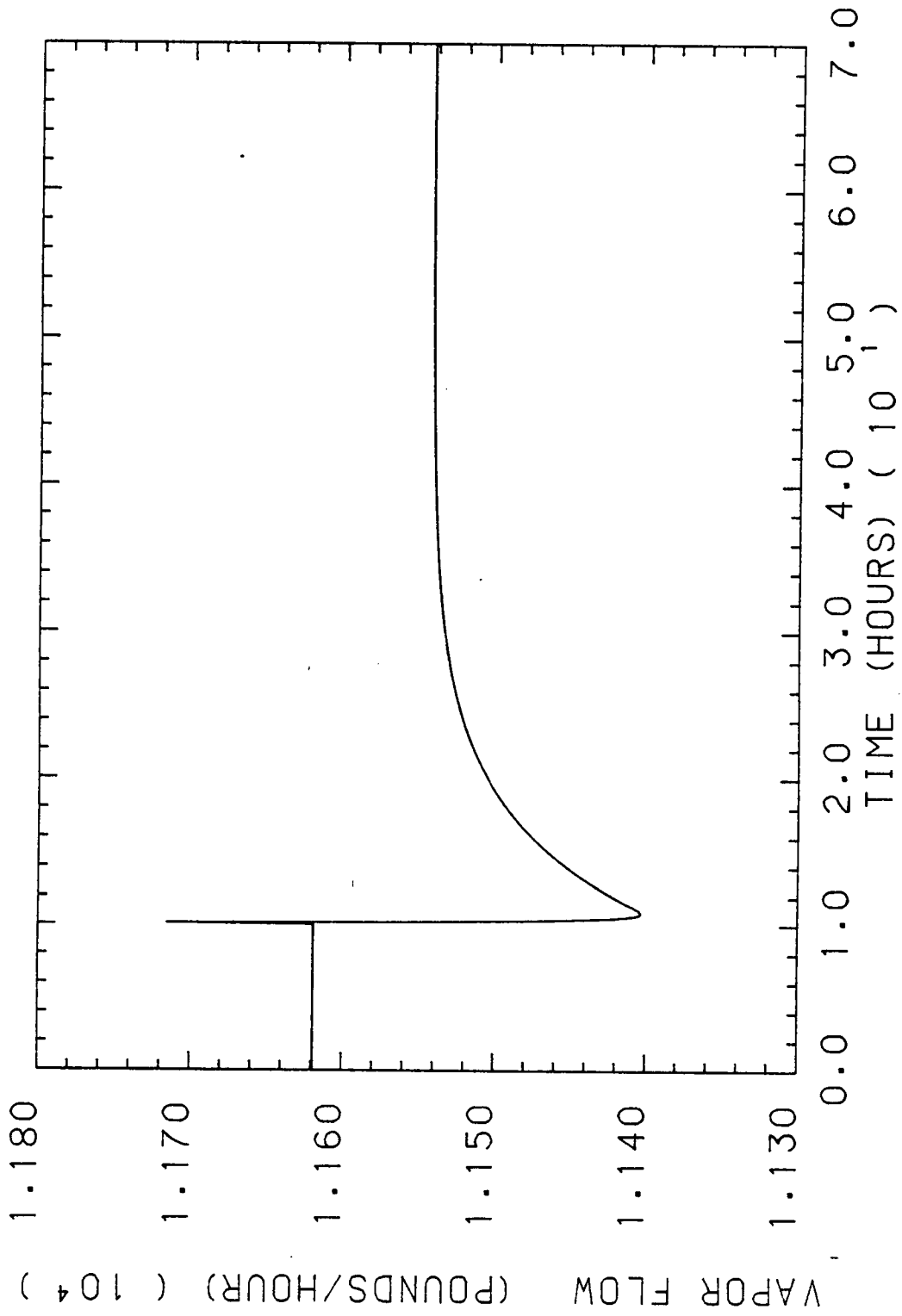


Figure 11. Effect of Feed Increase on Vapor Flow

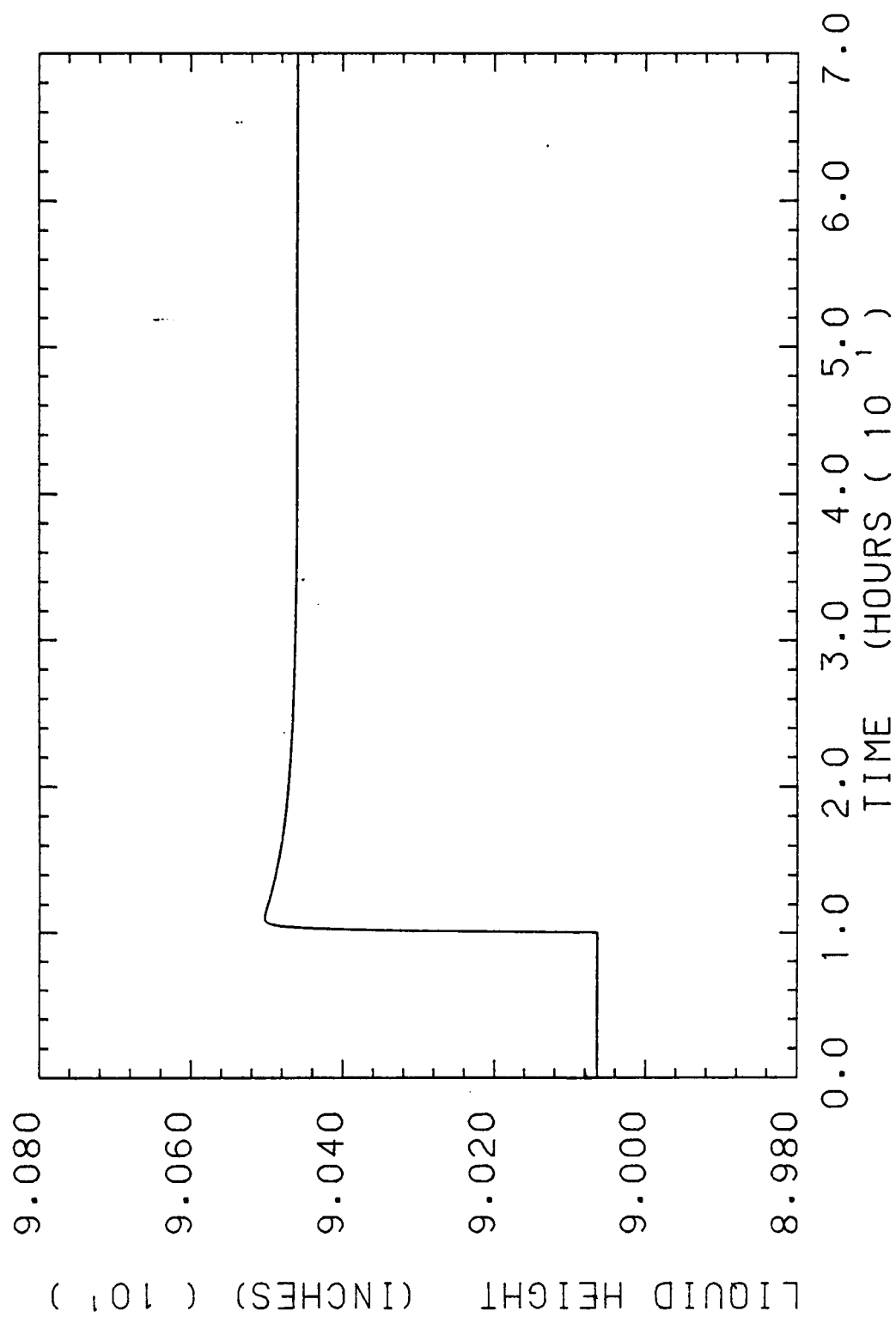


Figure 12. Effect of Feed Increase on Liquid Height

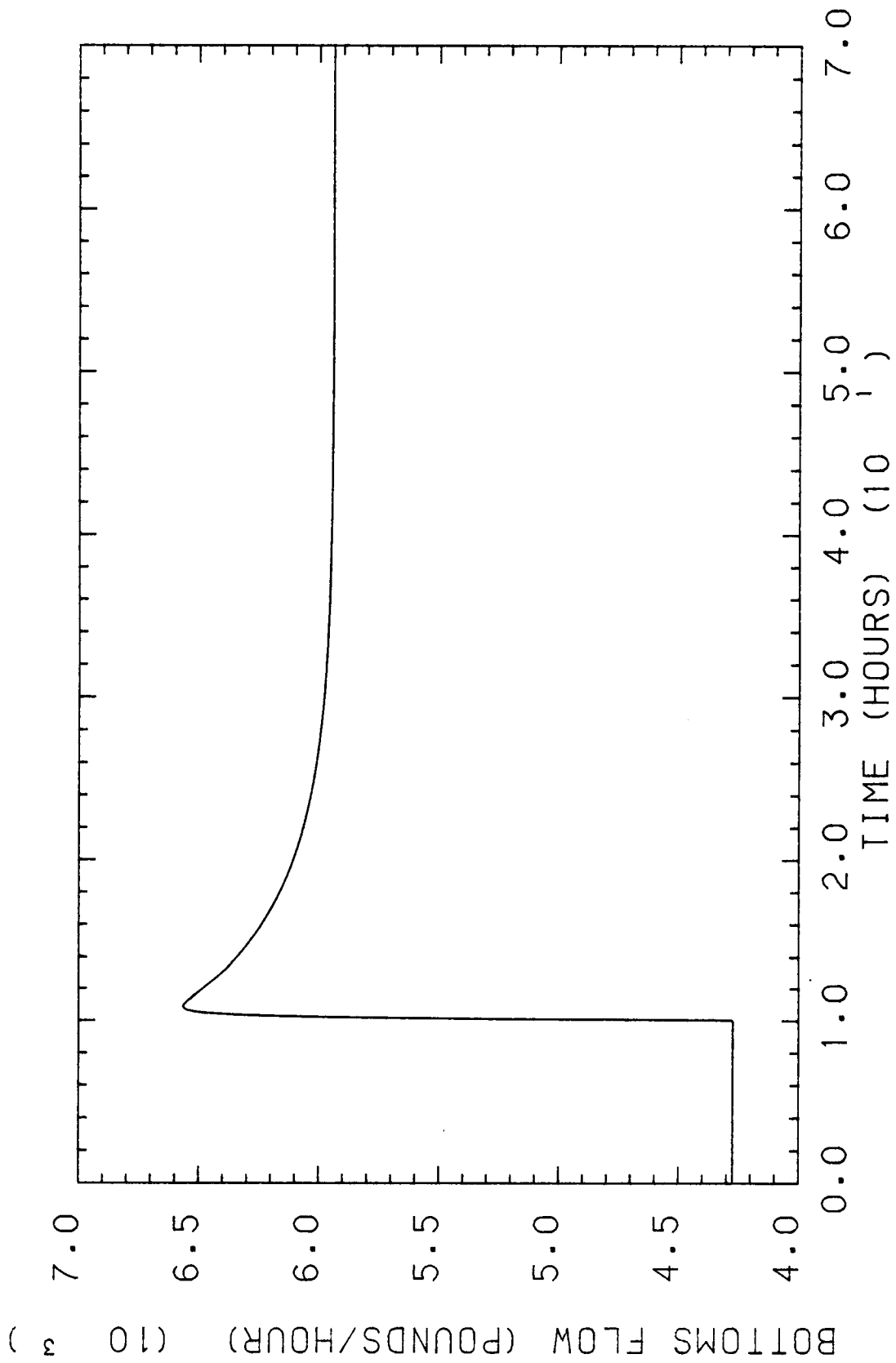


Figure 13. Effect of Feed Decrease on Bottoms Flow

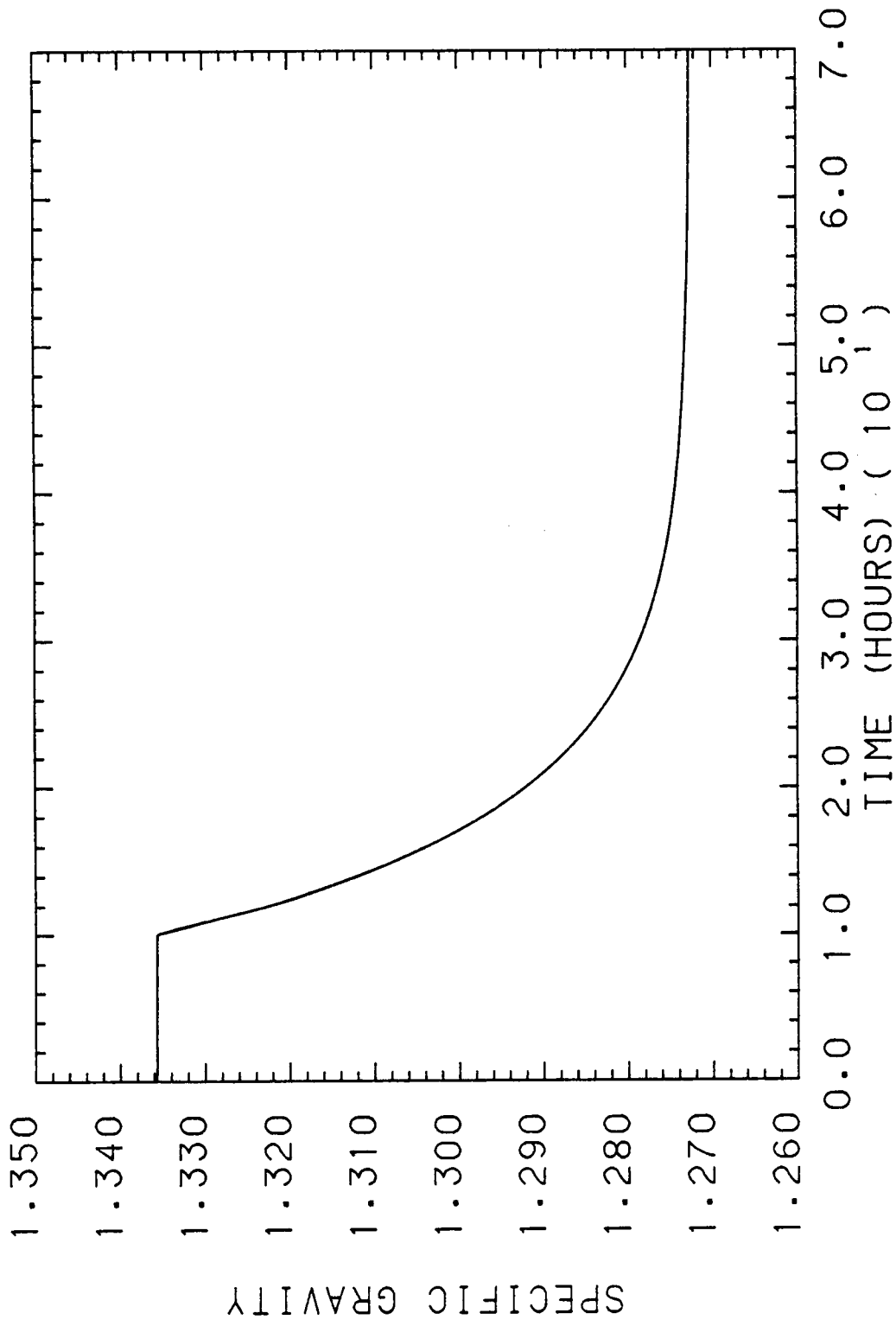


Figure 14. Effect of Steam Decrease on Specific Gravity

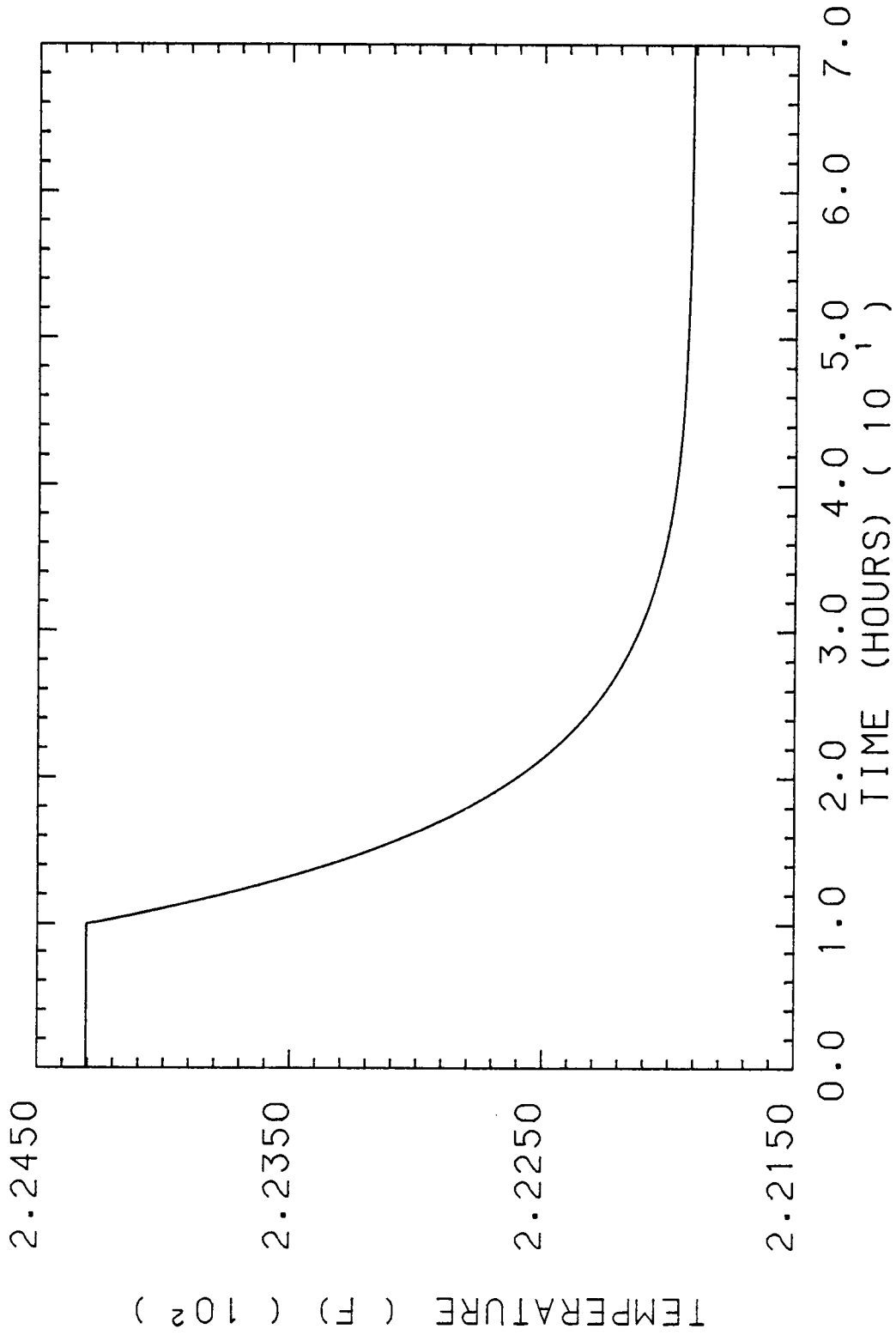


Figure 15. Effect of Steam Decrease on Temperature

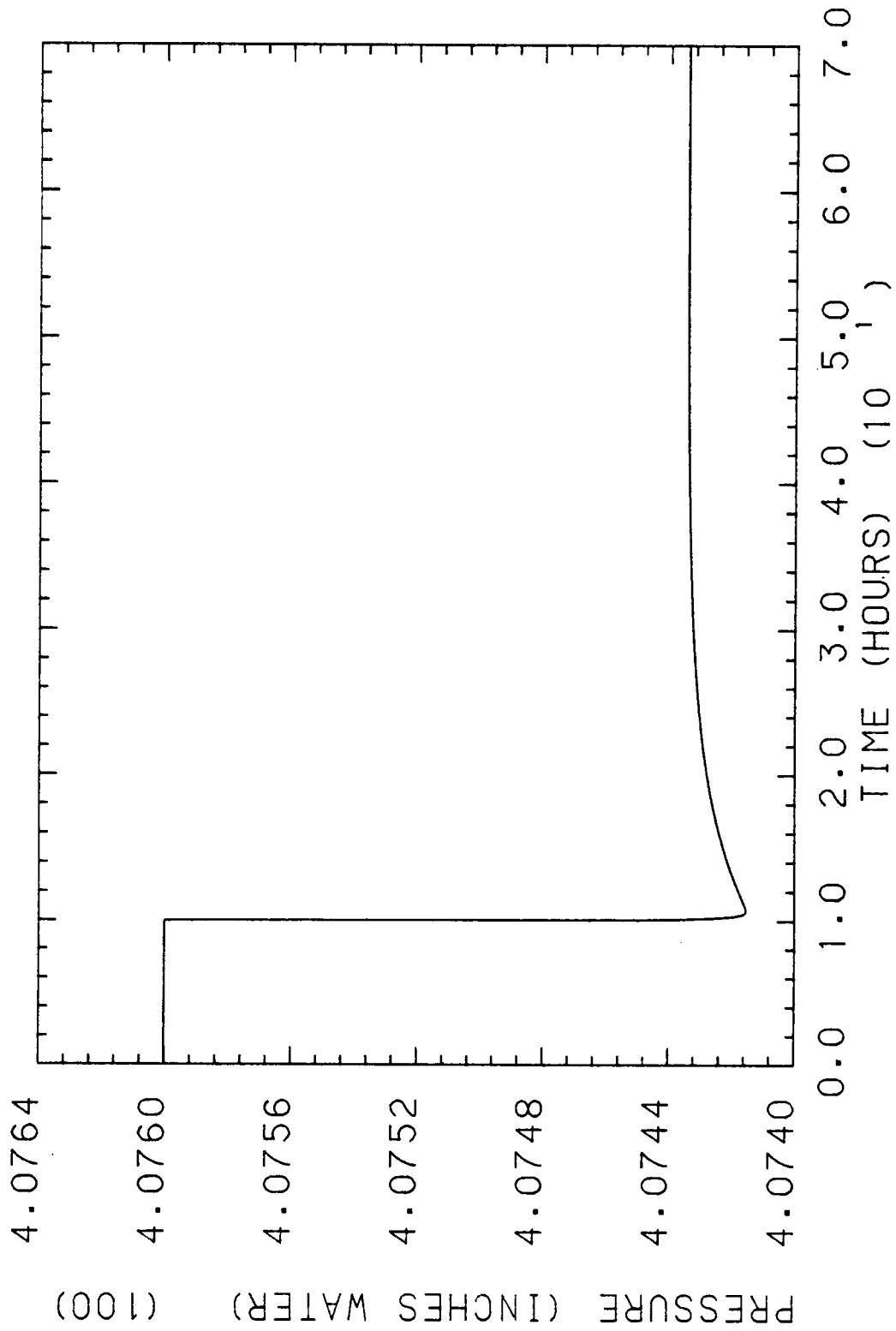


Figure 16. Effect of Steam Decrease on Pressure

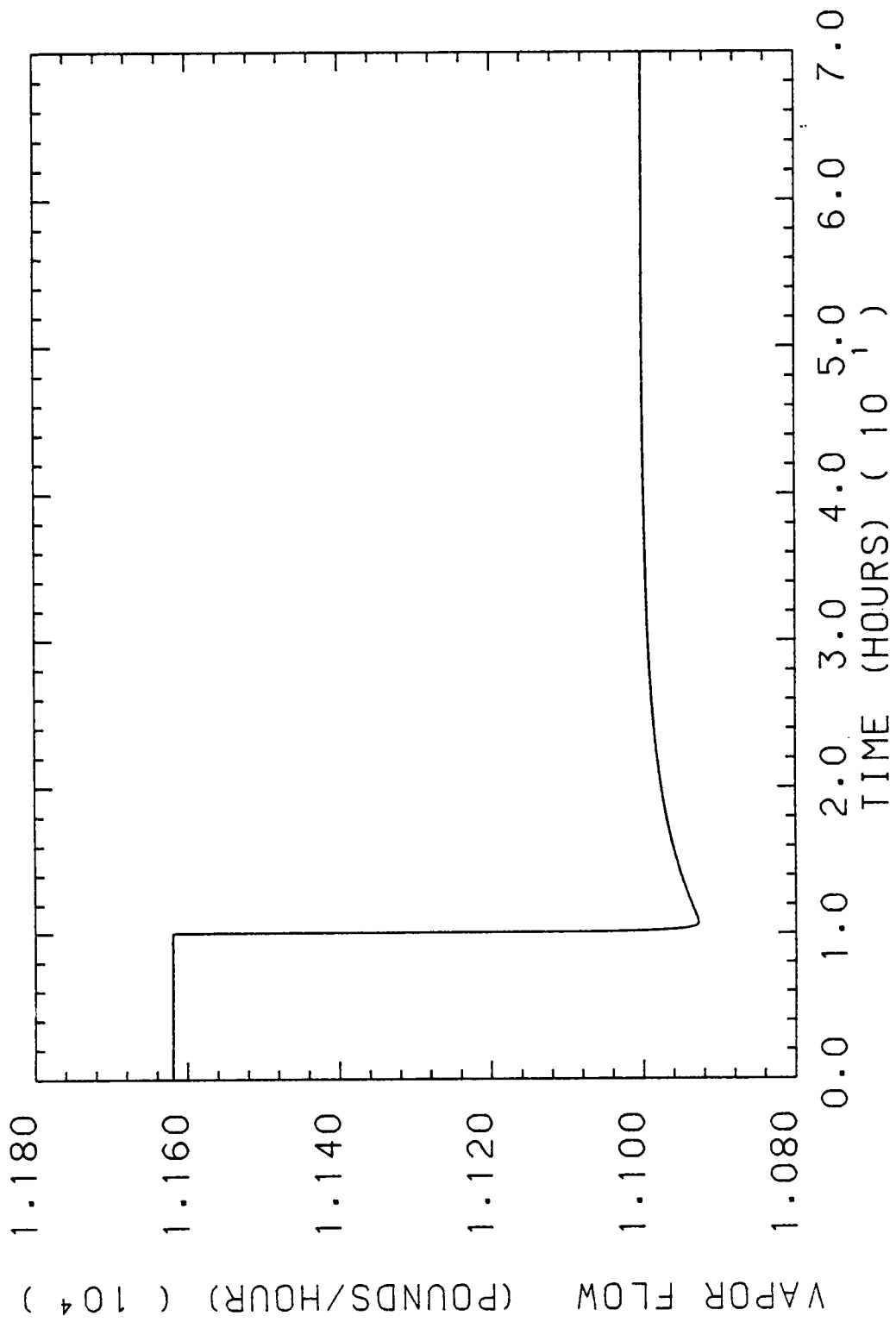


Figure 17. Effect of Steam Decrease on Vapor Flow

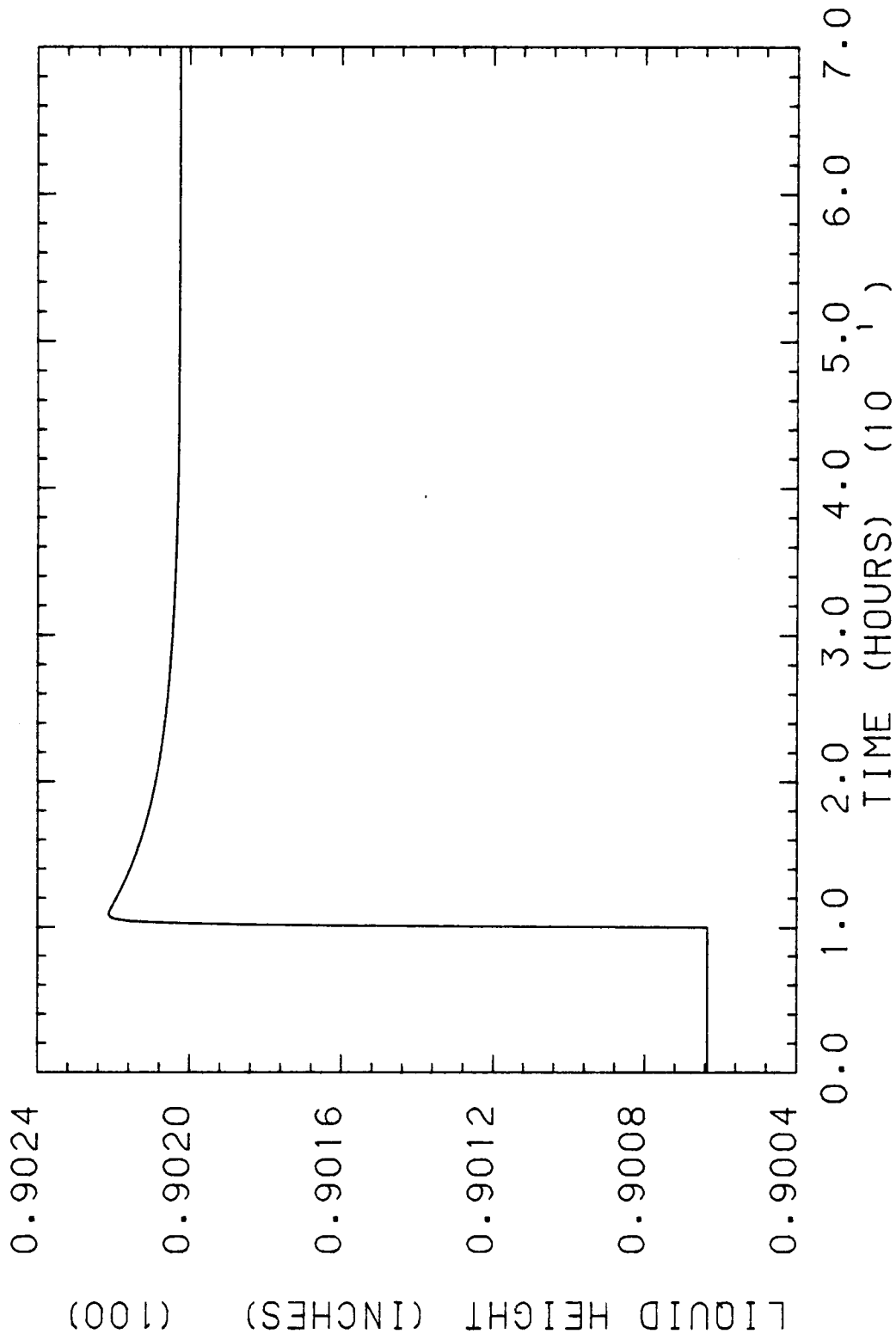


Figure 18. Effect of Steam Decrease on Liquid Height

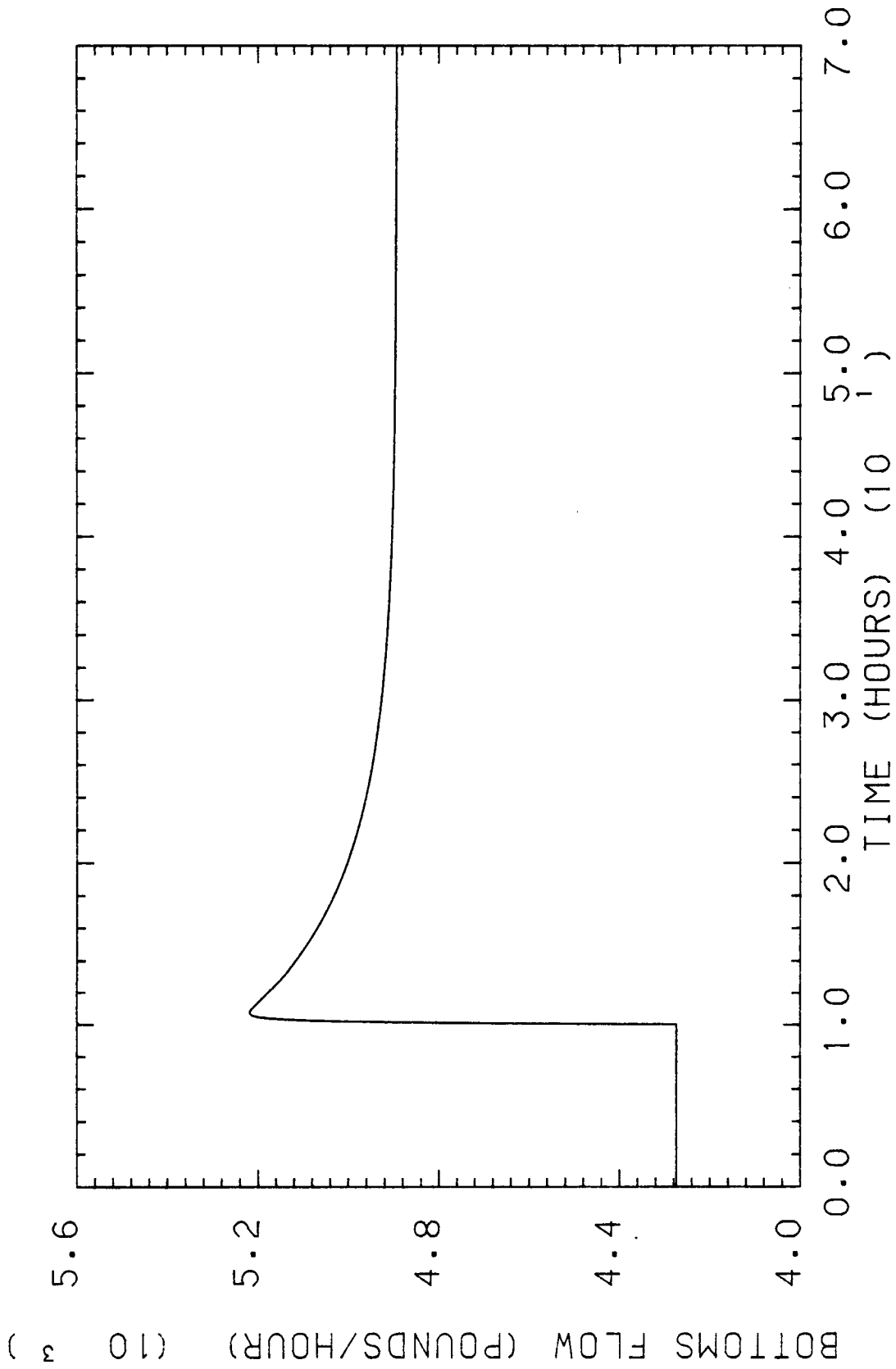


Figure 19. Effect of Steam Decrease on Bottoms Flow

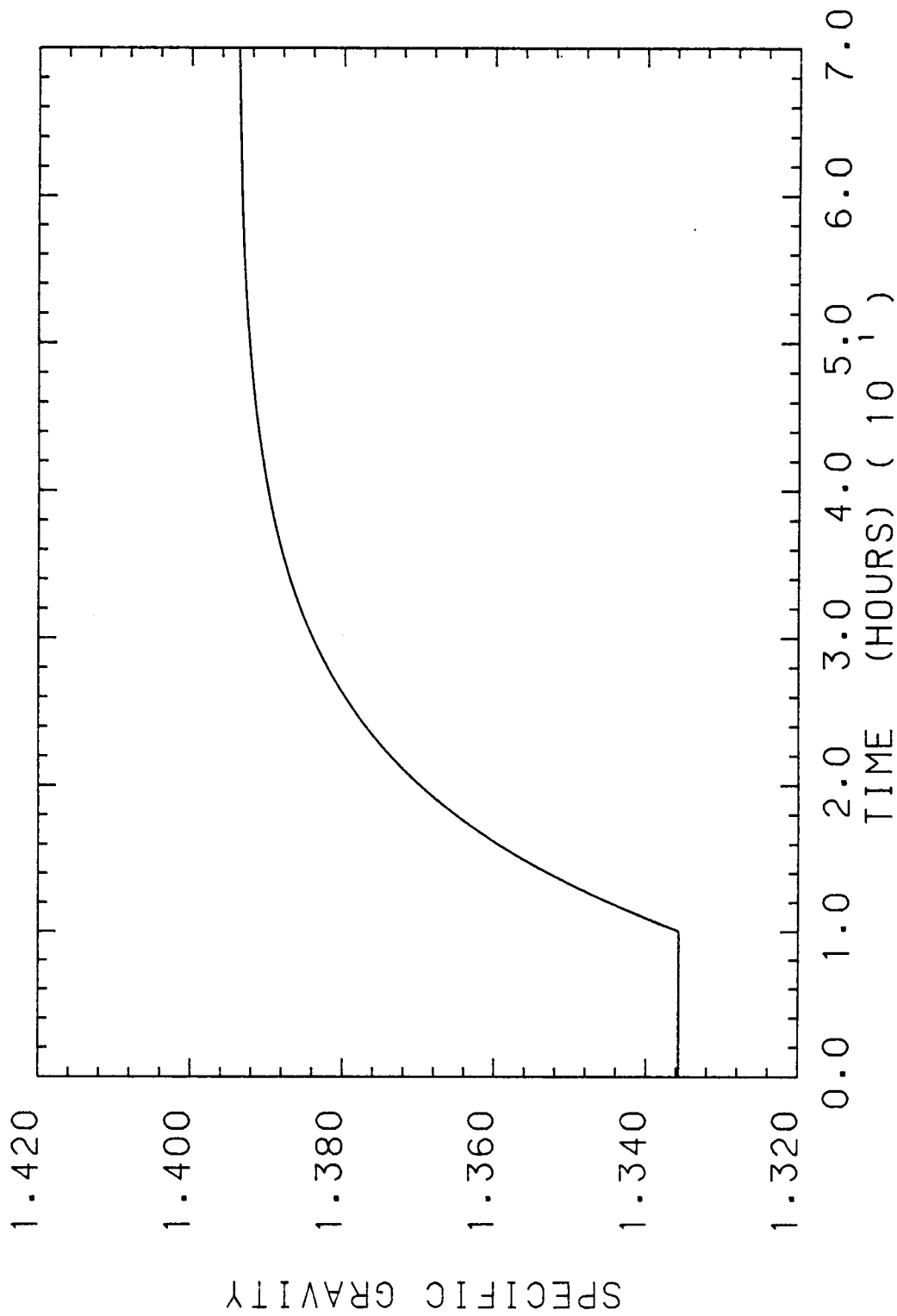


Figure 20. Effect of Feed Temperature Increase on Specific Gravity

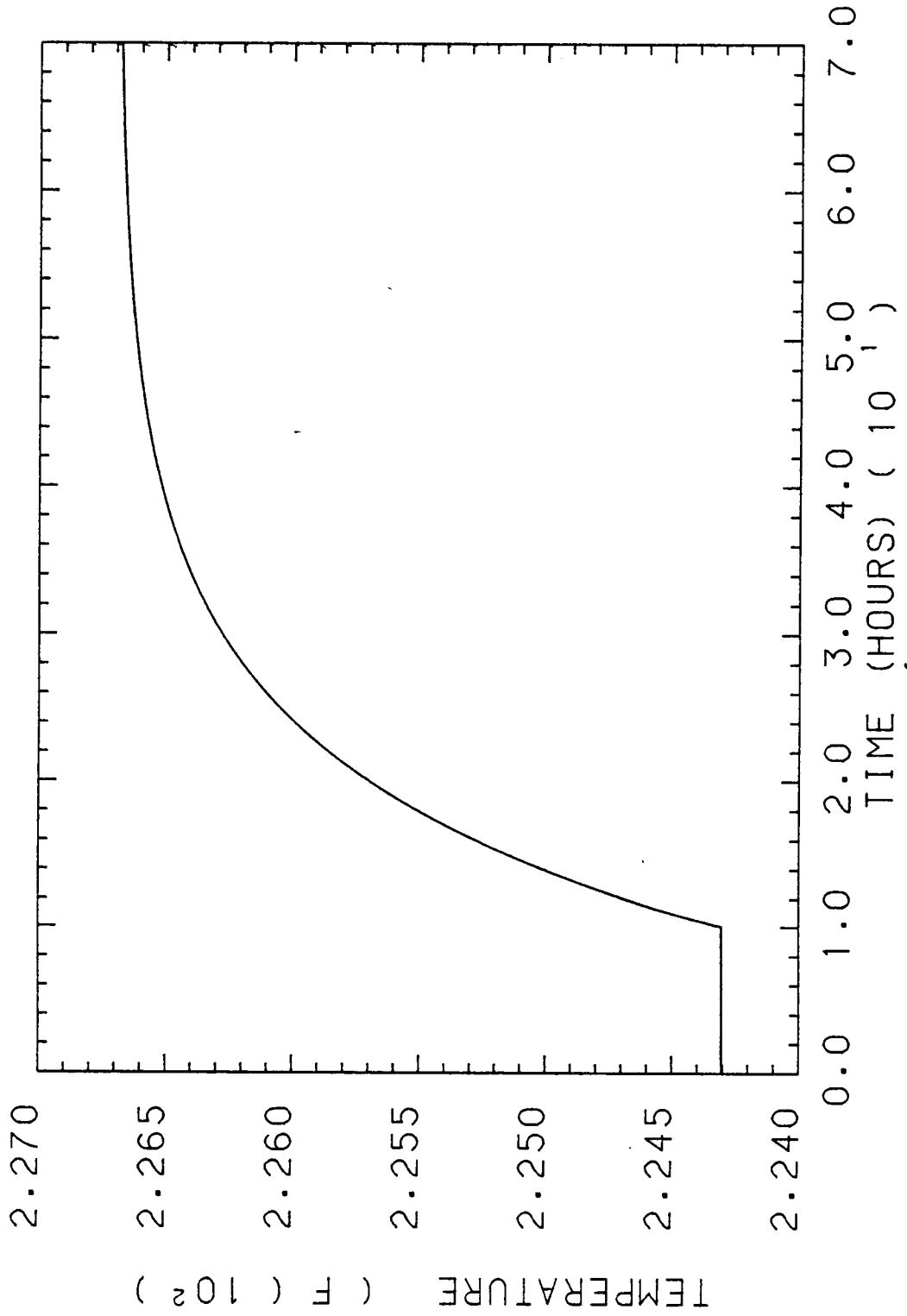


Figure 21. Effect of Feed Temperature Increase on Temperature

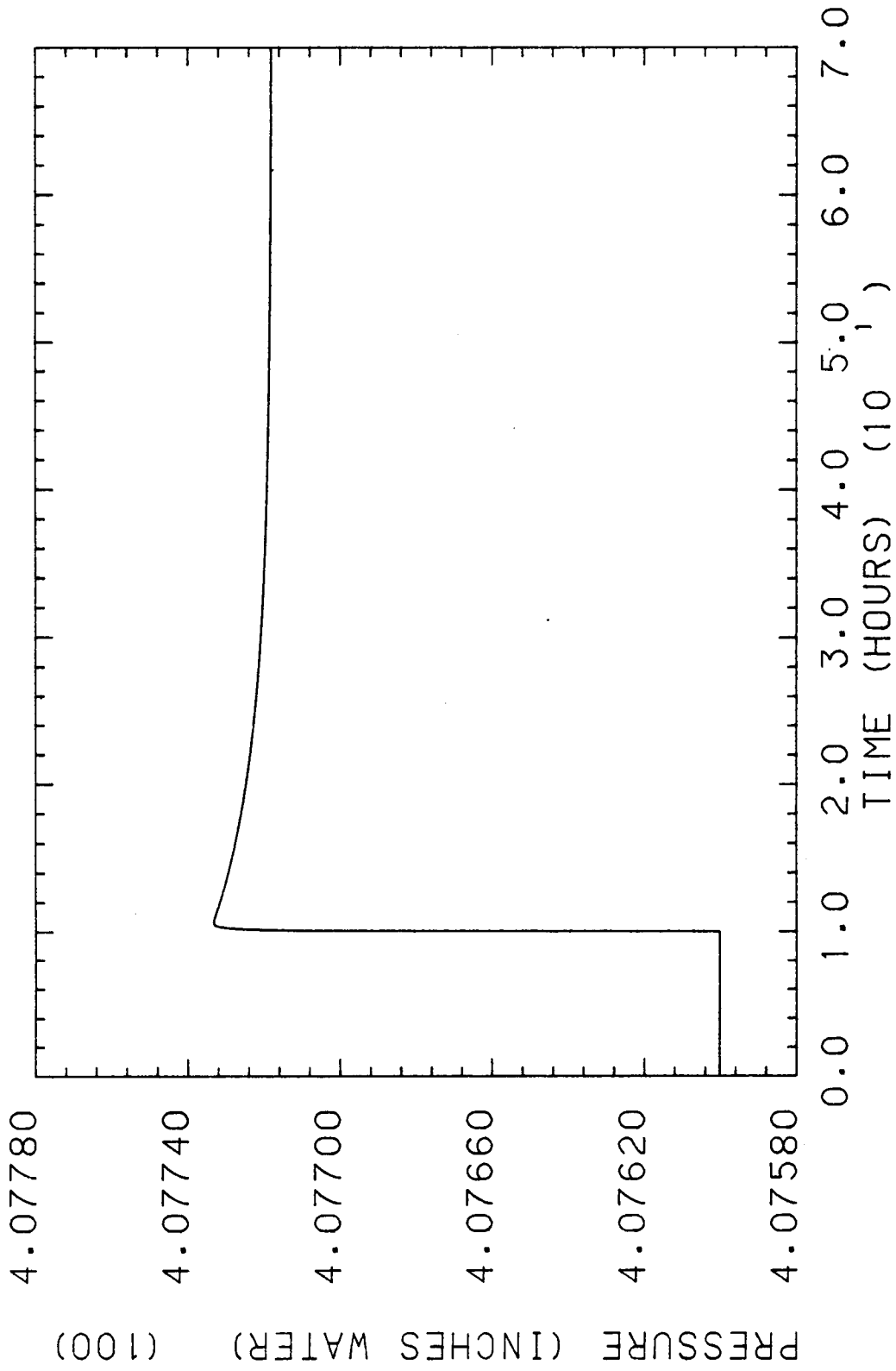


Figure 22. Effect of Feed Temperature Increase on Pressure

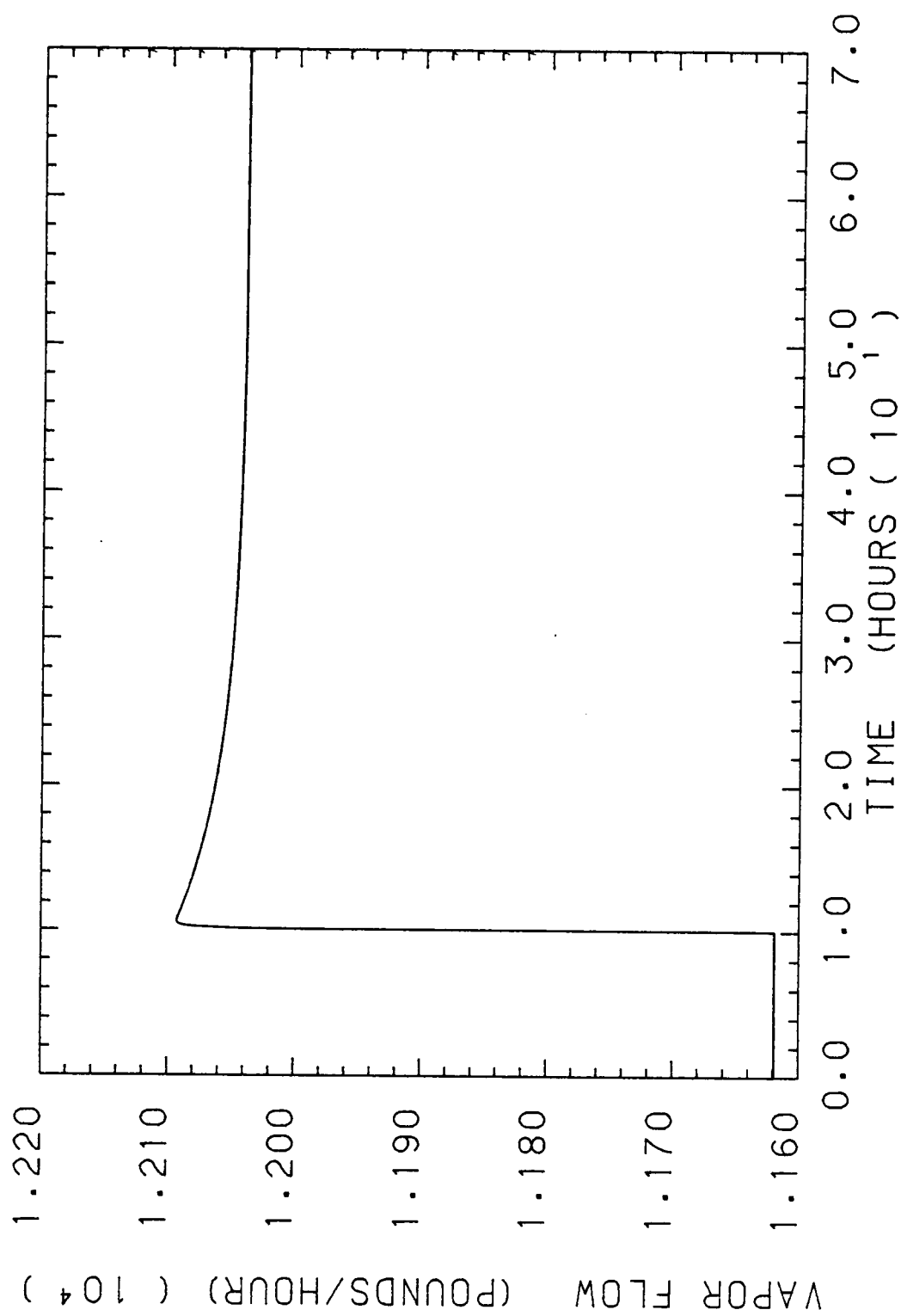


Figure 23. Effect of Feed Temperature Increase on Vapor Flow

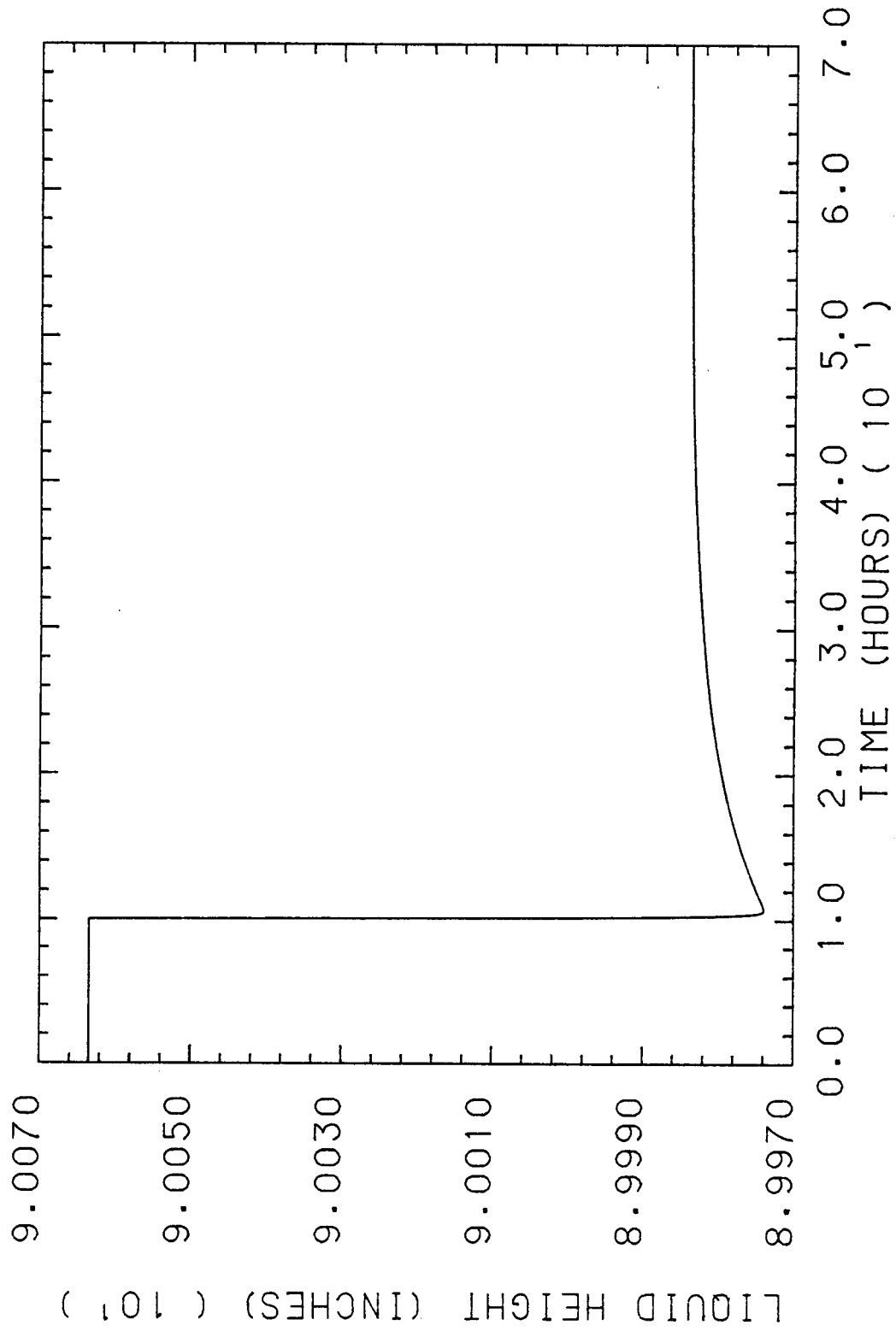


Figure 24. Effect of Feed Temperature Increase on Liquid Height

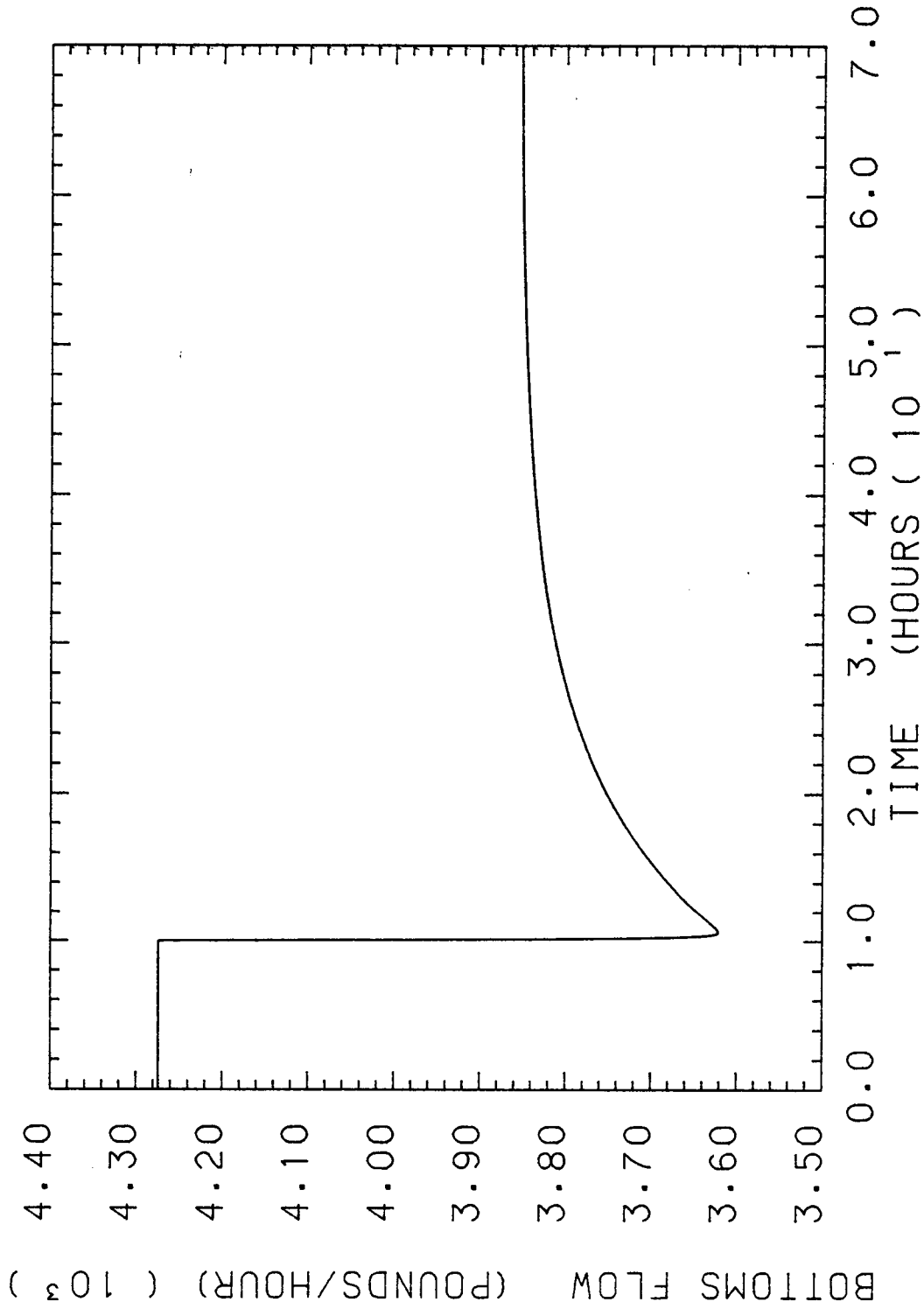


Figure 25. Effect of Feed Temperature Increase on Bottoms Flow

3.14 EFFECT OF FEED COMPOSITION DISTURBANCE

The effect of a feed acid increase is minimal, as can be seen from the effect of a 90% increase in feed acid on the temperature in Figure 26, and on pressure, in Figure 27.

The effect of a feed salt increase could be quite serious, as can be seen from Figure 28, the effect on specific gravity of a 90% increase in feed salt concentration. In this example, when the salt concentration in the feed is increased from 10.5 wt. % to 20 wt. %, the specific gravity of the solution in the evaporator rises from 1.32 to 1.86. Fortunately, the pH of the incoming solution is well maintained by the equipment upstream of the evaporator.

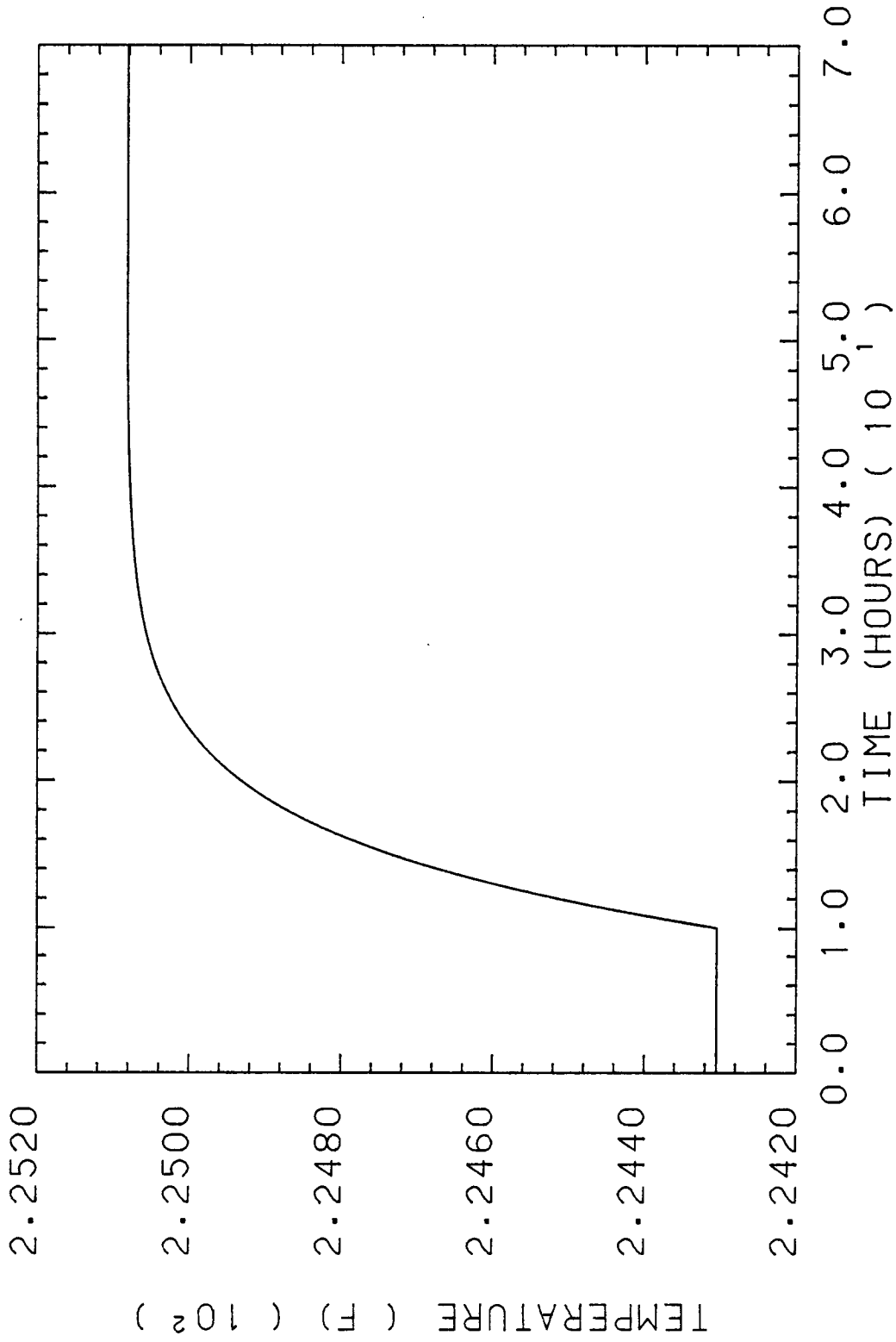


Figure 26. Effect of Feed Acid Increase on Temperature

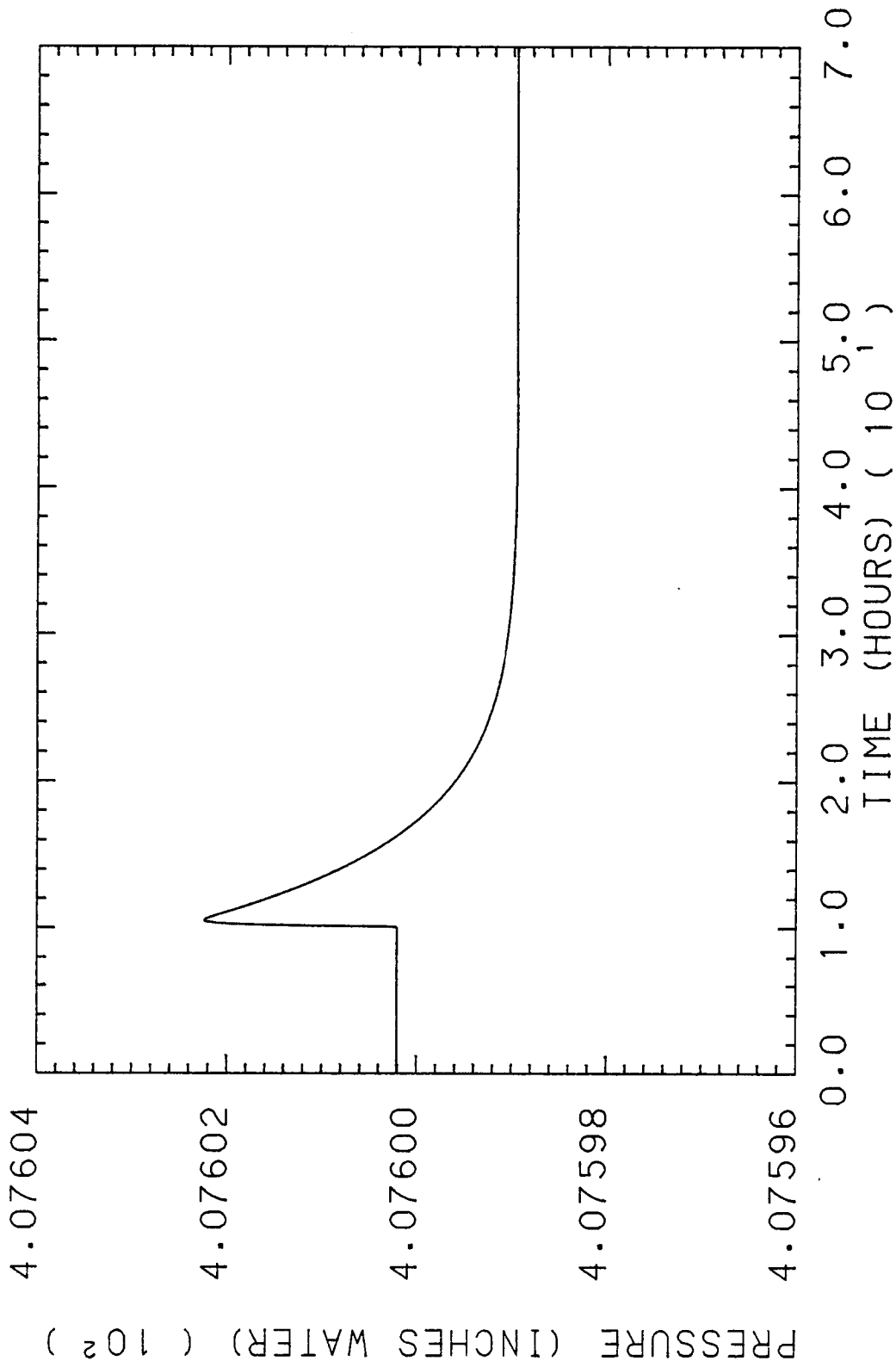


Figure 27. Effect of Feed Acid Increase on Pressure

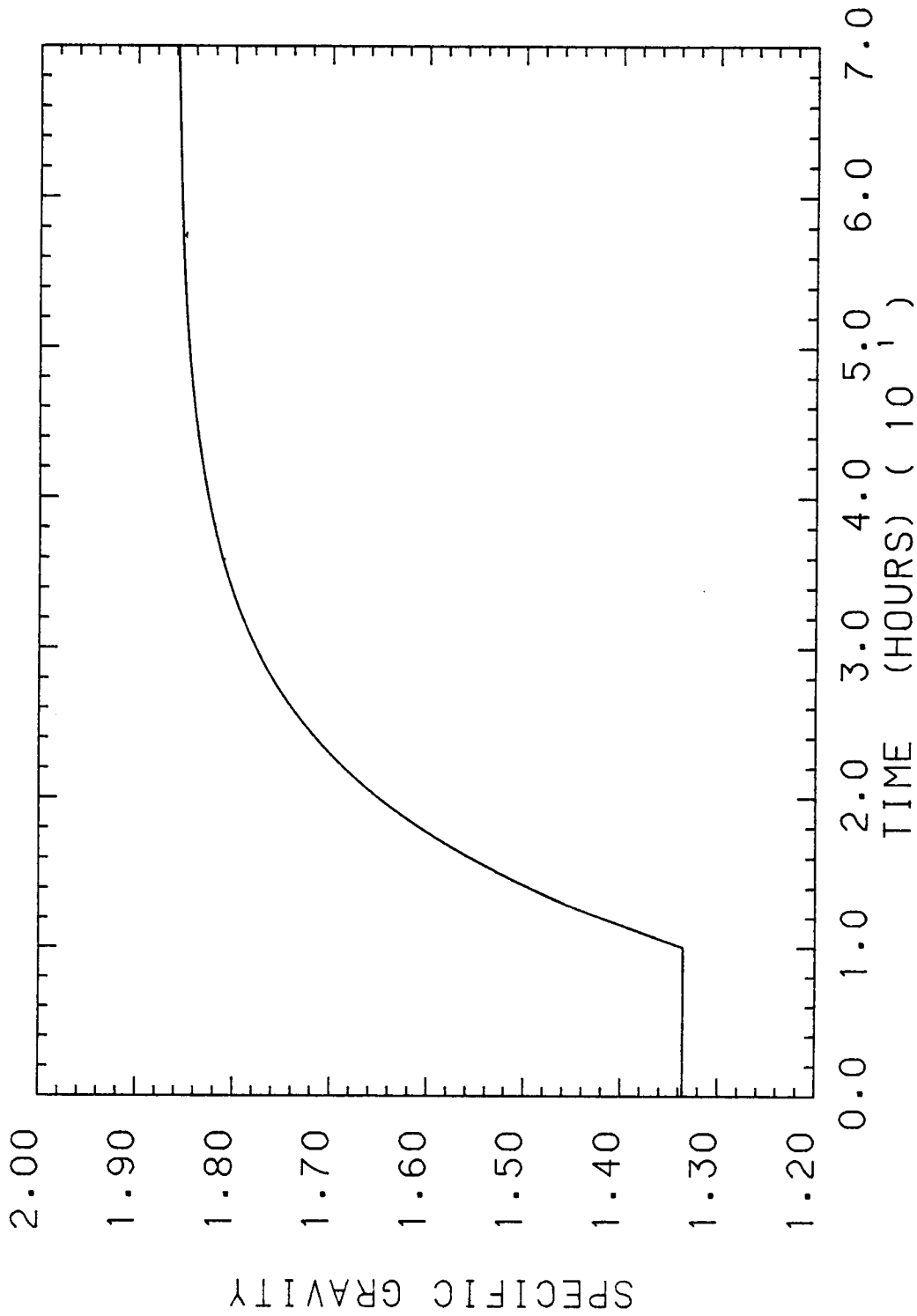


Figure 28. Effect of Feed Salt Increase on Specific Gravity

CHAPTER IV

LINEARIZED MODEL

Since the complete evaporator model contains both very fast and very slow dynamic elements, namely vapor flow, which responds very quickly, and specific gravity, which responds very slowly, the resulting simulation was extremely stiff. To minimize the extremely large computational requirements, a model was developed based on relatively simple linear transfer function relationships. The simplified model was developed by collecting step response data on the full model and curve fitting the parameters of a series of first order lags with dead times. Up to three elements were used to describe each relationship.

A good example is the response of vapor flow to a feed flow disturbance, as shown in Figure 10 on page 29. The relationship was described as a sum of three transfer functions as shown below:

$$V(s)/F(s) = K_1 * \exp(-\theta_1(s))/(1 + \tau_1(s)) + K_2 * \exp(-\theta_2(s)) / (1 + \tau_2(s)) + K_3 * \exp(-\theta_3(s))/(1 + \tau_3(s))$$

where $V(s)$ is the vapor rate, expressed in lb/hr, $F(s)$ is the feed rate, expressed in lb/hr, K is a steady state gain, τ is a time constant, expressed in hours, and θ is a

dead time, expressed in hours. The steady state gains for each relationship were used and the time constants and dead times were fit by hand, and are found in Tables 1 through 6.

In LaPlace form, the model can be described via a matrix. Thus, a disturbance in any or all of the inputs can be related to each output. This model was used for the control method selection and for preliminary tuning of the controller. This simplified model utilized difference equations to represent the process and was run with a step time of one minute.

The form of the difference equation is

$$dX(i) = -a * X(i-1) + b * M(i-1-n)$$

$$X(i) = X_{ss} + \sum dX(i)$$

$$n = N/dt$$

$$\alpha = \exp(-dt/T)$$

$$a = -\alpha$$

$$b = K (1 - \alpha)$$

where $X(i)$ is the current value of the output, $dX(i)$ is the effect on the output of the input, X_{ss} is the steady state value of the output, M is the value of the input, N is the dead time, expressed in hours, n is the integer dead time, T is the time constant of the particular relation, expressed in hours, and a and b are the difference equation constants.

Table 1. Parameters for Linearized Model of Effect of Steam Disturbance

Output Variable	Gain	Time Constant	Dead Time
Specific Gravity	1.2615×10^{-4}	8.2200	-
Temperature	4.7915×10^{-4}	8.0000	-
Pressure I	3.6965×10^{-4}	0.0515	-
Pressure II	-3.8053×10^{-4}	8.5330	0.7330
Vapor Flow I	1.3832	0.1000	-
Vapor Flow II	-0.1464	8.5333	0.7333
Liquid Height I	-3.1537×10^{-4}	0.0860	-
Liquid Height II	3.7280×10^{-4}	8.5000	0.8667
Bottoms Flow I	-1.8898	0.0500	-
Bottoms Flow II	0.6525	8.4667	0.7333

Table 2. Parameters for Linearized Model of Effect of Feed Disturbance

Output Variable	Gain	Time Constant	Dead Time
Specific Gravity	-1.2187×10^{-4}	12.750	-
Temperature	-5.0820×10^{-4}	13.000	-
Pressure I	1.8027×10^{-5}	0.006	-
Pressure II	-8.1276×10^{-5}	0.060	-
Pressure III	4.3947×10^{-5}	13.270	0.6000
Vapor Rate I	0.0412	0.000	-
Vapor Rate II	-0.1850	0.100	-
Vapor Rate III	0.0997	12.660	0.6000
Liquid Height I	1.8832×10^{-4}	0.080	-
Liquid Height II	-1.6191×10^{-5}	13.260	0.8000
Bottoms Flow I	1.4788	0.000	-
Bottoms Flow II	-0.4311	13.260	-

Table 3. Parameters for Linearized Model of Effect of Feed Temperature Disturbance

Output Variable	Gain	Time Constant	Dead Time
Specific Gravity	2.9067×10^{-3}	11.300	-
Temperature	0.1188	13.000	-
Pressure I	6.6555×10^{-3}	0.060	-
Pressure II	-7.6052×10^{-4}	11.267	0.6000
Vapor Flow I	23.6800	0.060	-
Vapor Flow II	-2.6587	21.267	0.6000
Liquid Height I	-4.4761×10^{-3}	0.070	-
Liquid Height II	4.9699×10^{-4}	11.270	0.7333
Bottoms Flow I	-3.2664×10^{-1}	0.070	-
Bottoms Flow II	11.5920	11.267	0.6000

Table 4. Parameters for Linearized Model of Effect of Vent Pressure Disturbance

Output Variable	Gain	Time Constant	Dead Time
Specific Gravity	-2.6955×10^{-4}	0.000	-
Temperature	0.1253	0.000	-
Pressure	0.9998	0.000	-
Vapor Flow I	$-2.6367 \times 10^{+1}$	0.000	-
Vapor Flow II	$2.5643 \times 10^{+1}$	0.080	-
Liquid Height I	$1.6404 \times 10^{-}$	0.000	-
Liquid Height II	-1.6174×10^{-2}	0.150	-
Bottoms Flow I	$1.1110 \times 10^{+2}$	0.000	-
Bottoms Flow II	$-1.1040 \times 10^{+2}$	0.100	-

Table 5. Parameters for Linearized Model of Effect of Feed Acid Concentration Disturbance

Output Variable	Gain	Time Constant	Dead Time
Specific Gravity	$3.5589 \times 10^{+1}$	1.000	-
Temperature I	$3.7718 \times 10^{+3}$	2.778	-
Temperature II	$-3.6450 \times 10^{+1}$	5.500	12.533
Pressure I	$1.6457 \times 10^{+1}$	0.000	-
Pressure II	$-2.2993 \times 10^{+1}$	1.200	-
Pressure III	0.4182	5.100	11.667
Vapor Flow I	$5.8997 \times 10^{+4}$	0.035	-
Vapor Flow II	$-8.2850 \times 10^{+4}$	1.200	0.333
Vapor Flow III	1.5332	4.500	11.200
Liquid Height I	$-5.0216 \times 10^{+1}$	0.030	-
Liquid Height II	$3.9418 \times 10^{+1}$	1.500	0.333
Bottoms Flow I	$-4.6816 \times 10^{+5}$	0.035	-
Bottoms Flow II	$4.9569 \times 10^{+5}$	1.200	0.333
Bottoms Flow III	$5.4010 \times 10^{+3}$	6.000	13.067

Table 6. Parameters for Linearized Model of Effect of Feed Salt Concentration Disturbance

Output Variable	Gain	Time Constant	Dead Time
Specific Gravity	0.0913	5.630	-
Temperature	8.1782	6.000	-
Pressure I	2.1396×10^{-2}	0.000	-
Pressure II	-3.4532×10^{-2}	6.467	-
Vapor Flow I	$7.7654 \times 10^{+1}$	0.060	-
Vapor Flow II	$-1.2535 \times 10^{+2}$	4.000	0.4667
Liquid Height I	-9.1994×10^{-2}	0.053	-
Liquid Height II	5.6490×10^{-2}	6.000	0.5333
Bottoms Flow I	$-6.0860 \times 10^{+2}$	0.060	-
Bottoms Flow II	$6.5643 \times 10^{+2}$	4.000	0.4667

CHAPTER V

HACKMAN HAT FLOW CONTROLLER

In order to properly simulate the actual control system, the Hackman Hat flow control was simulated. The valve equation was used to relate liquid height in the hat to flow:

$$F = K_{\text{hat}} \sqrt{h}$$

where F is the feed into the evaporator, expressed in lb/hr, K_{hat} is the valve constant, and H is the liquid height in the hat, expressed in inches.

The hat has fairly quick response to a feed decrease, as can be seen in Figure 29, which compares the feed flow to the hat and the flow from the hat.

A proportional controller was added to the hat to control the liquid height in the hat using the feed to the hat. The proportional controller was chosen because it is the simplest type of controller and has the fastest and most stable response. The offset that accompanies the use of a proportional controller is of no consequence in the inner loops of a control system, which is where the hat is used. The response of the tuned system is shown in Figure 30. The system was tuned for a quarter decay response.

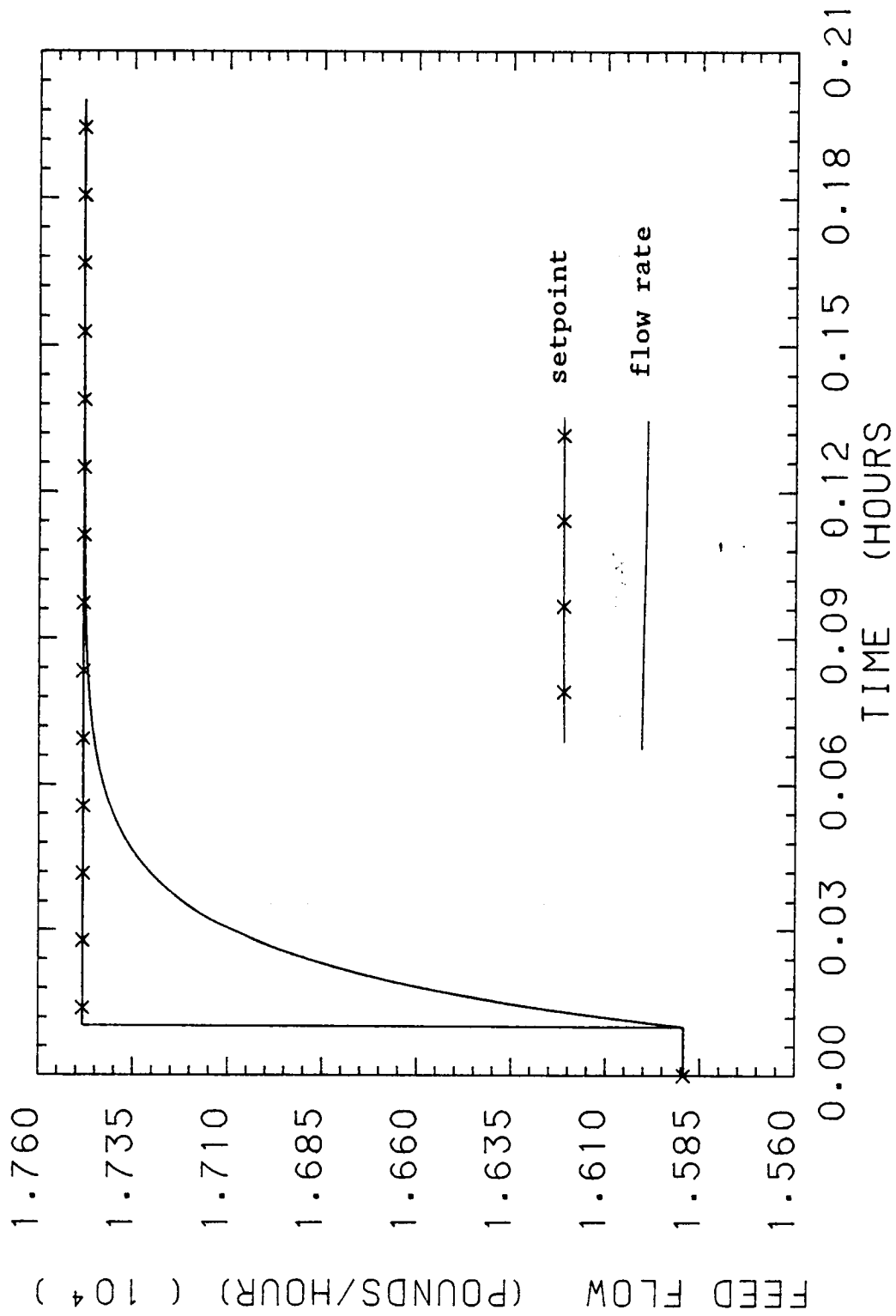


Figure 29. Response of Hat to Input Step

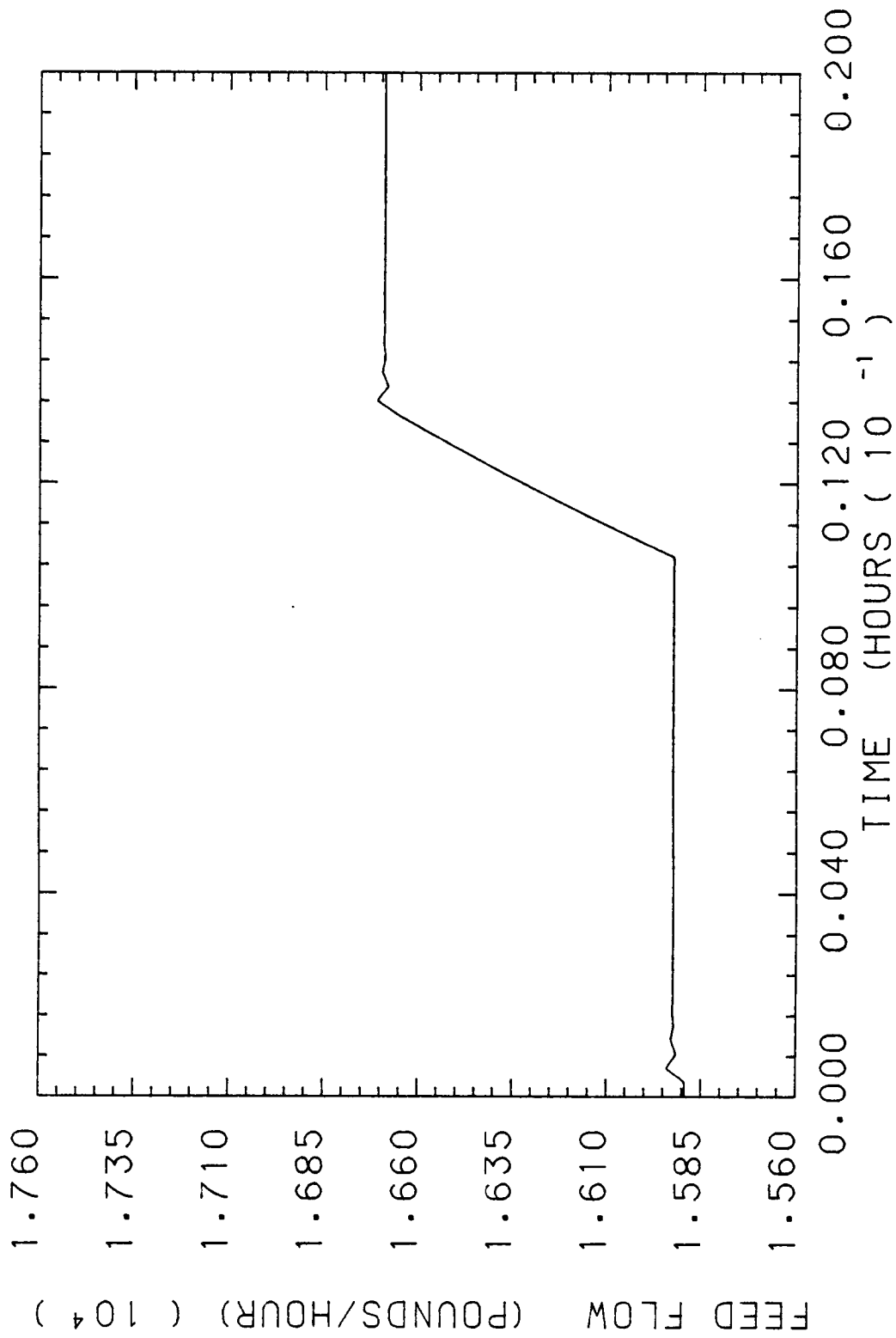


Figure 30. Response of Hat to Setpoint Change

CHAPTER VI

CONTROL SYSTEMS

6.1 PRESENT SYSTEM

The first control system that was tested was the system that is presently used on the evaporator at SRP. The Hackman Hat flow control was coupled to the evaporator, and a PI controller was used as the master controller for the Hackman Hat liquid height control. A block diagram of the control system is shown in Figure 31. The PI controller was chosen in order to eliminate offset from the system. The Hackman Hat liquid level controller was detuned slightly, with the gain reduced from 760 to 660. The specific gravity controller was then tuned using a Pattern Search to minimize the integral time times absolute error (ITAE) + a constant times the integral of the absolute derivative of the control action (CONAC).

$$\text{ITAE} = \int \text{Time} * \text{error}(t) * dt$$

$$\text{CONAC} = \beta \int \left| d C(t)/dt \right| * dt$$

where error is the deviation of the control variable from the setpoint, time is the elapsed time since the disturbance, expressed in hours, β is a tuning constant, and $C(t)$ is the manipulated variable.

The Pattern Search utilizes a subroutine, PATTERN (11), which determines the values of parameters (the gain

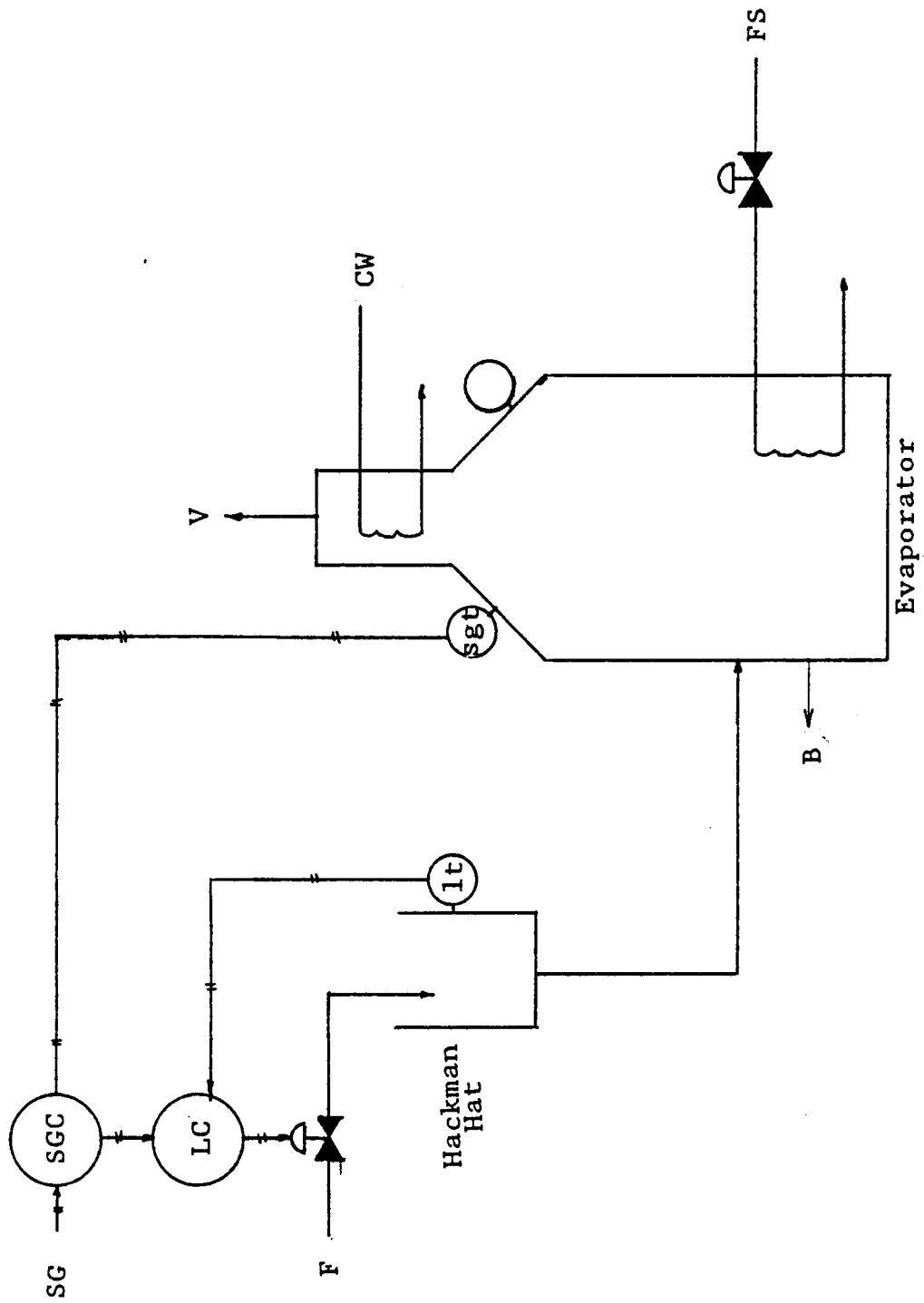


Figure 31. Present Control System

and integral time of the specific gravity controller) which minimize the COST (ITAE + CONAC). The constant was chosen as 0.006 which was the value which minimized the "ringing" behavior of the control system. The gain and integral time were chosen as -4117.25 and 0.1547 hours, respectively. The response of the system to a 20 °F increase in feed temperature is shown in Figure 32. The control action is shown in Figure 33.

6.2 STEAM CONTROLLER

The first alternate system that was considered used the steam flow, rather than the feed flow, as the manipulated variable. A block diagram is shown in Figure 34. The response of the system to the steam controller is almost identical to the response of the system to the feed controller. However, since the evaporator is typically operated at or near the maximum steam flow, this system would be very constrained and therefore unusable. If new evaporators are constructed, they should be designed with higher steam flow capabilities. Then the steam controller could be used. This would be a simple way to avoid the complexity added by the Hackman Hat flow controller.

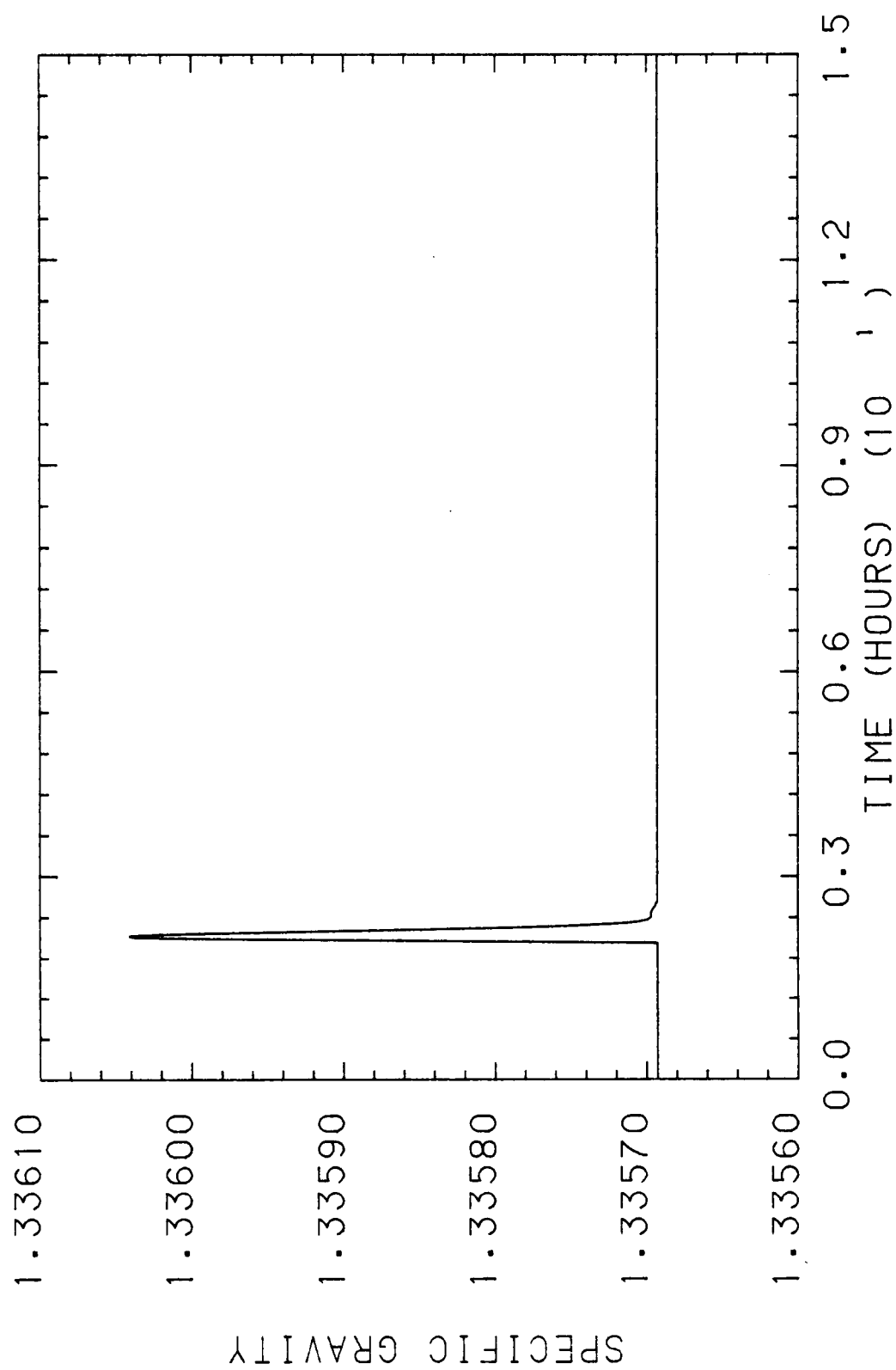


Figure 32. Present Controller on Feed Temperature Disturbance

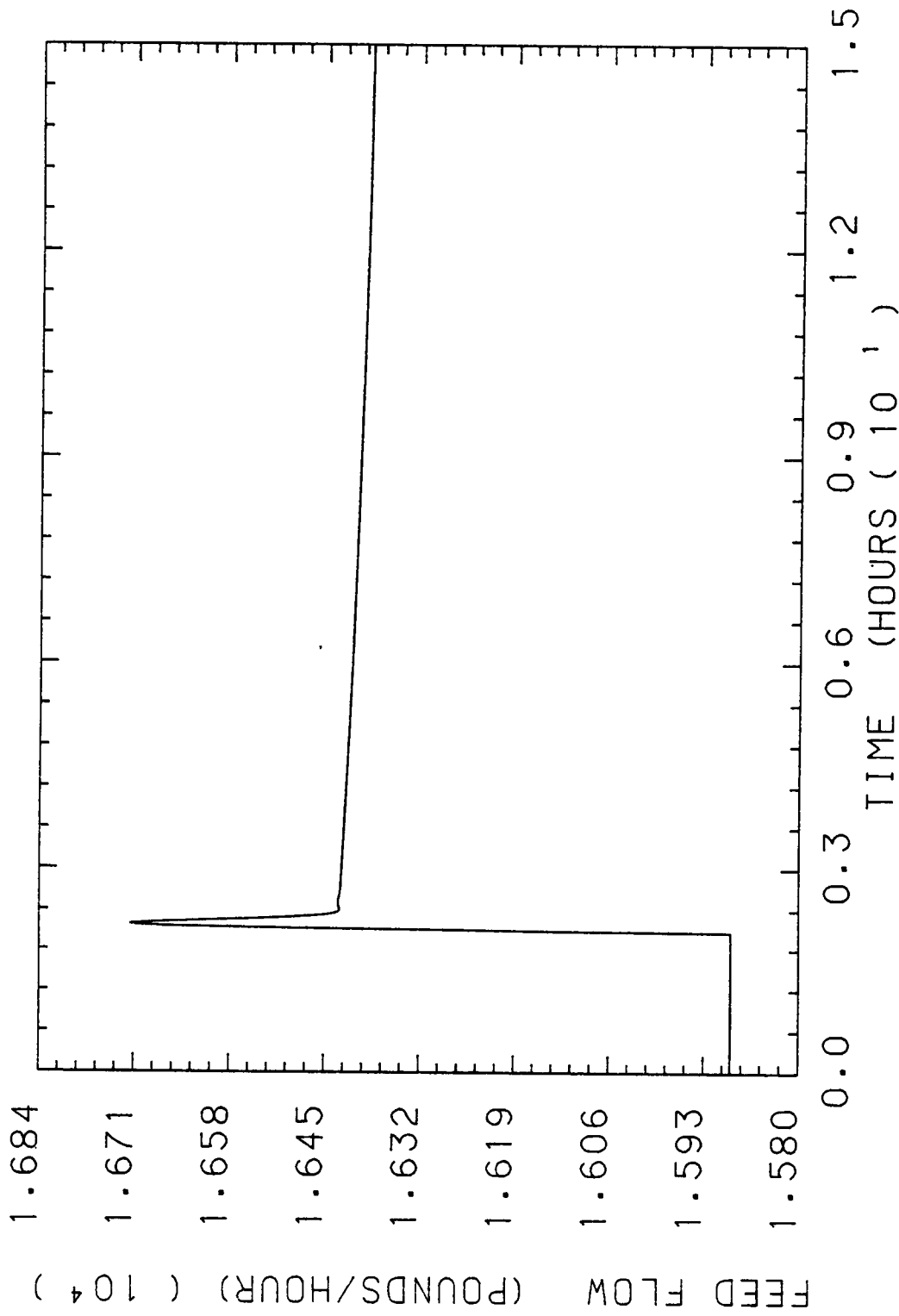


Figure 33. Control action of Present Controller on Feed Temperature, Disturbance

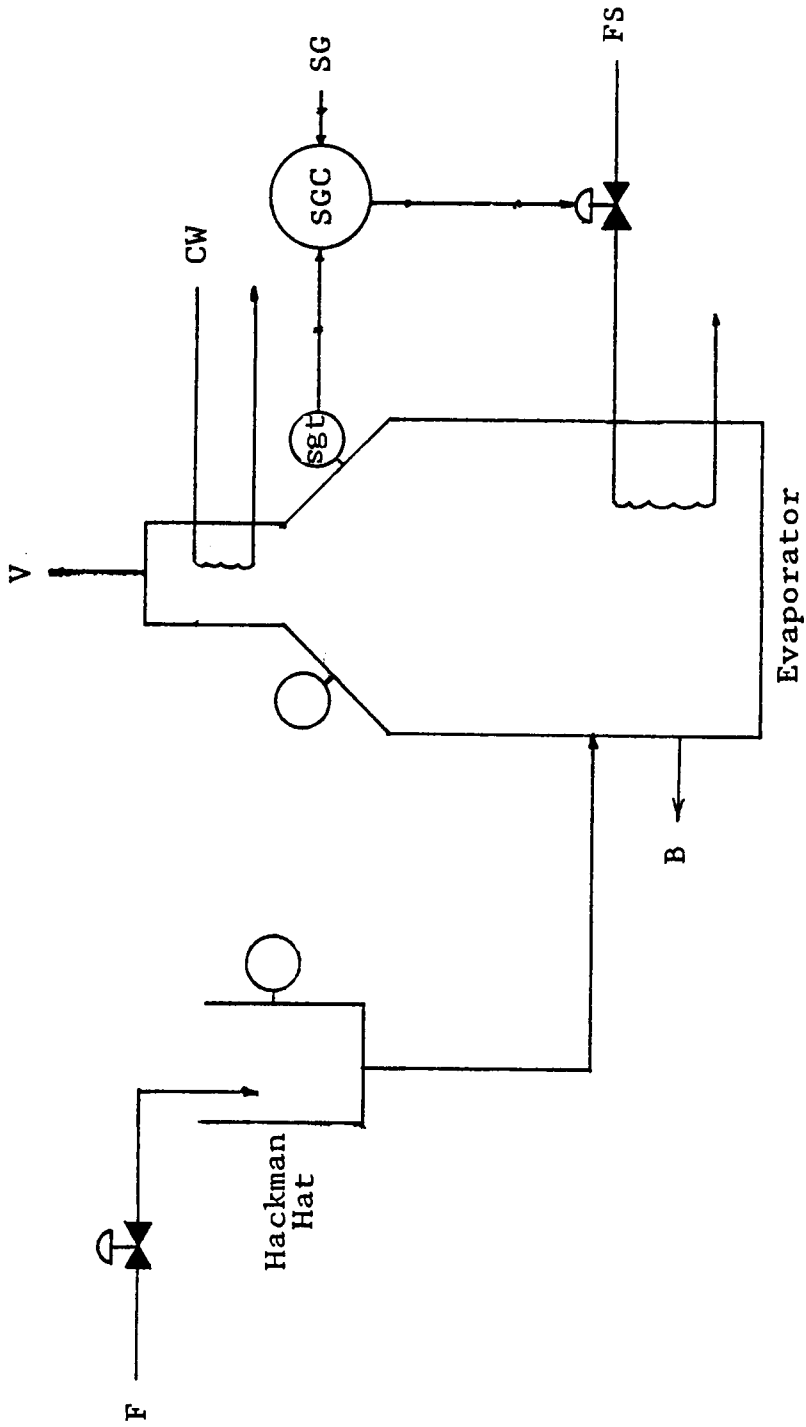


Figure 34. Control System using Steam Flow as the Manipulated Variable

6.3 CASCADE CONTROLLER

The next system to be proposed was a cascade with the evaporator liquid height as the inner, or slave loop controlling the Hackman Hat flow controller, and using a master specific gravity controller. Figure 35 gives a block diagram of this system. This system was more difficult to tune since it had three controllers. The Hackman Hat and evaporator liquid height controllers were proportional-only (P) controllers, as they were inner loops, and a PI controller was used on the outer, specific gravity controller to eliminate steady state offset.

In order to make the Pattern Search of reasonable size, the inner gains were picked and the pattern search was done only on the specific gravity controller. The same tuning parameter as above (ITAE + CONAC) was used for this search. The two inner gains were varied, and the tuning constant, β was chosen for each set of inner gains. The best response was obtained by setting the Hackman Hat flow controller gain to 300 and the height controller gain to 10. The specific gravity controller gain and integral time were chosen as -639.0 and 0.1385 hours, respectively. The response of this system is shown in Figure 36, and the controller actions are shown in Figures 37 and 38, with Figure 37 showing the response of

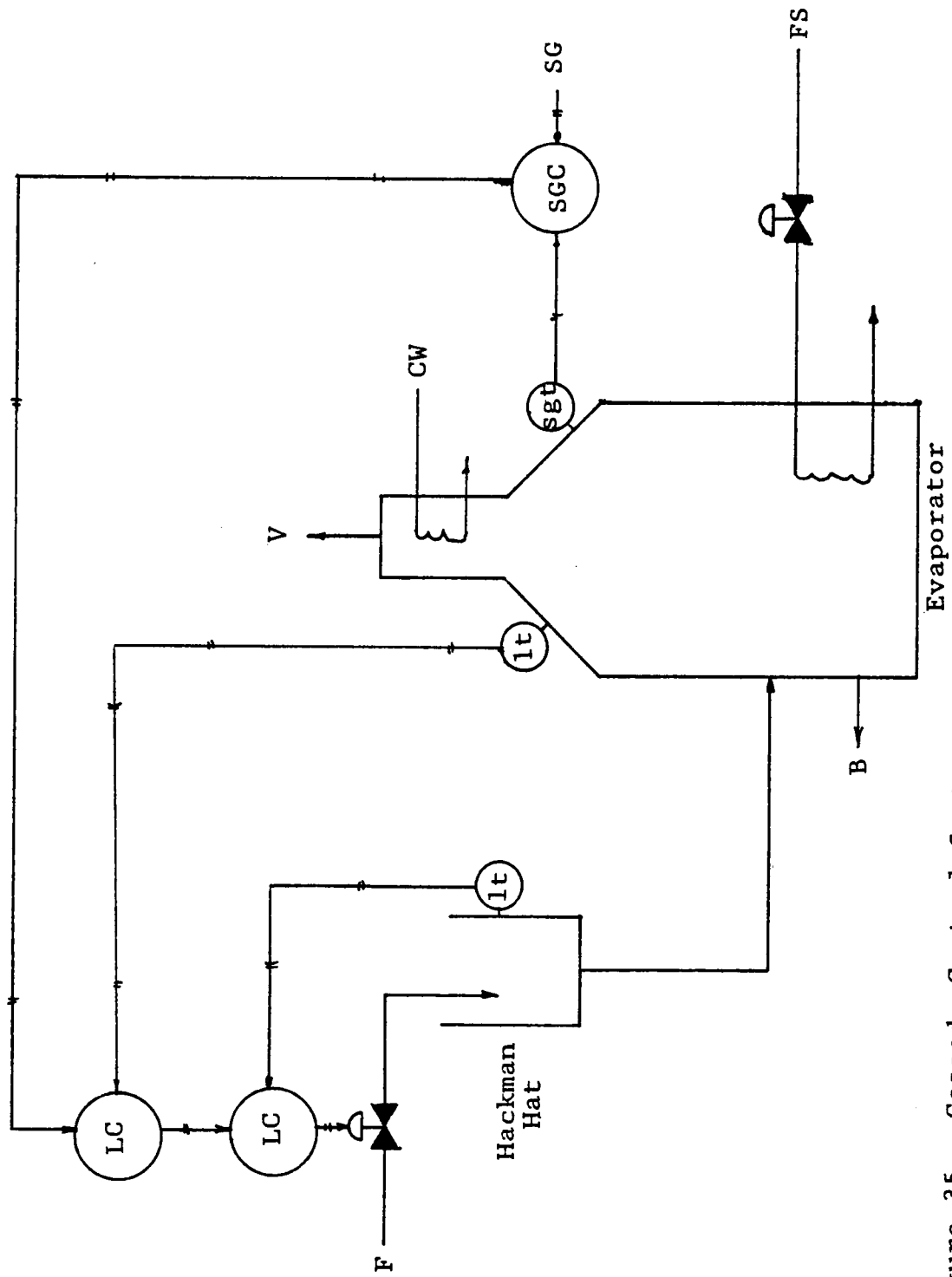


Figure 35. Cascade Control System

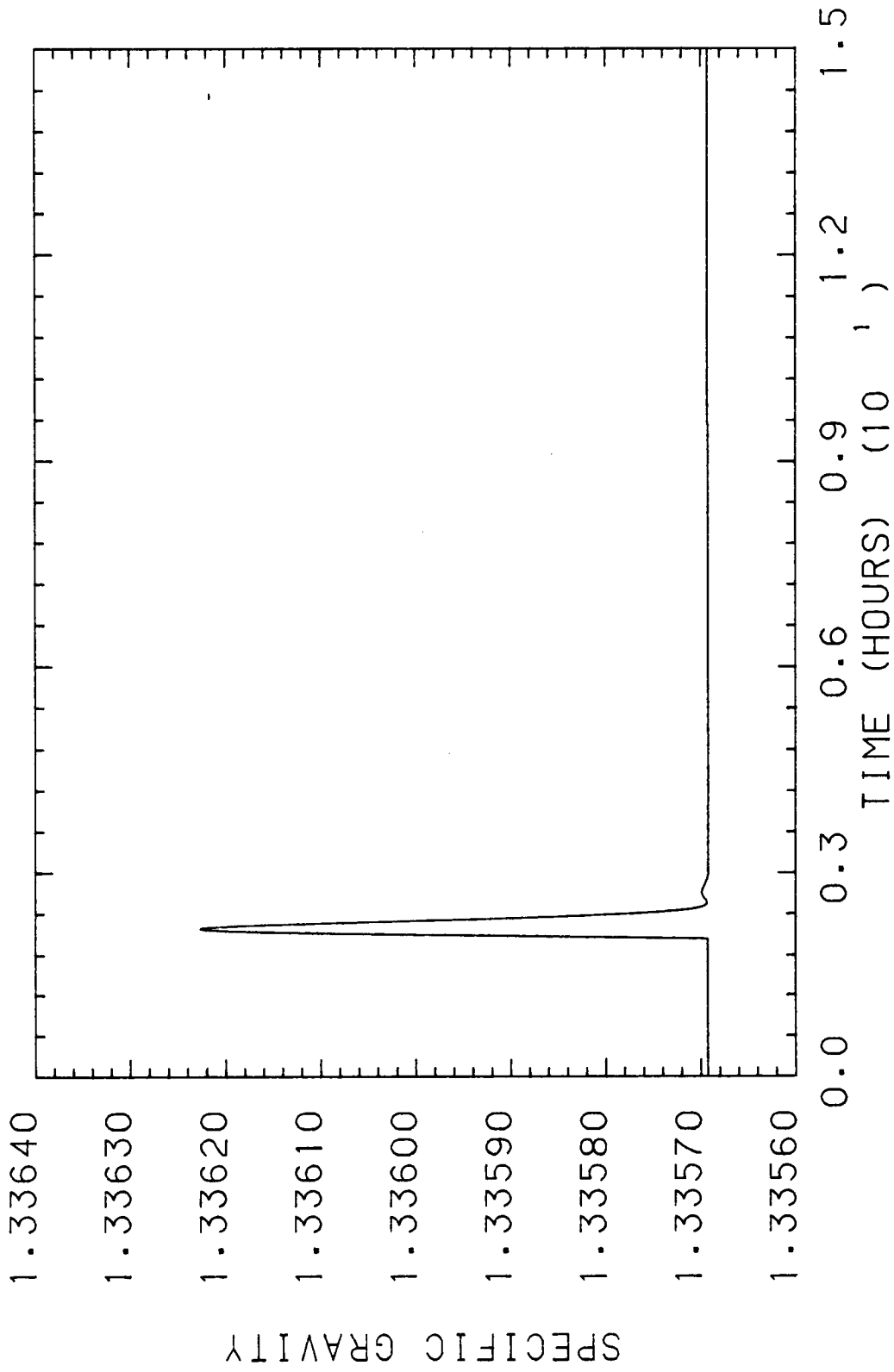


Figure 36. Cascade Controller on Feed Temperature Disturbance

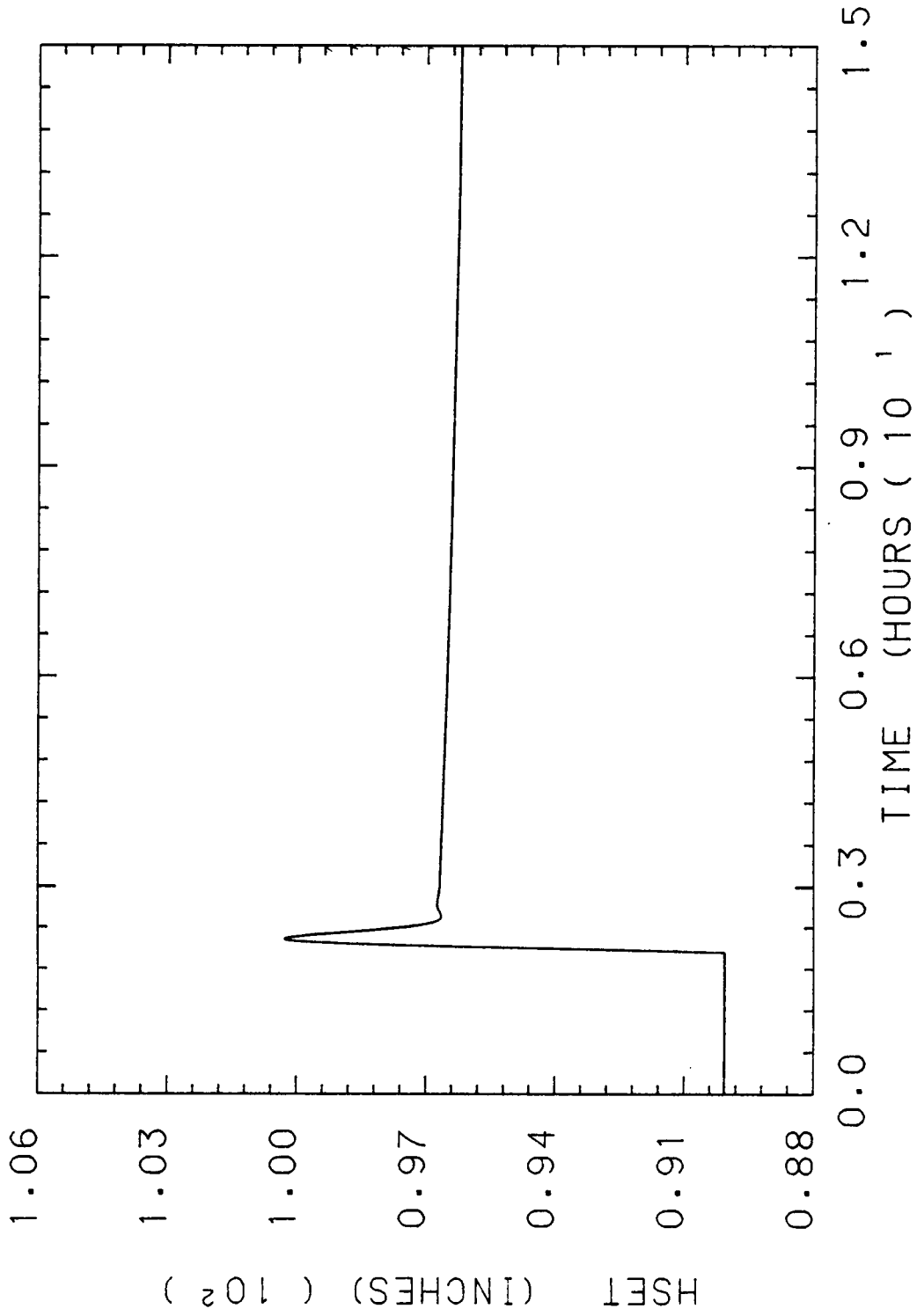


Figure 37. Control Action of Cascade Controller on Feed Temperature Disturbance

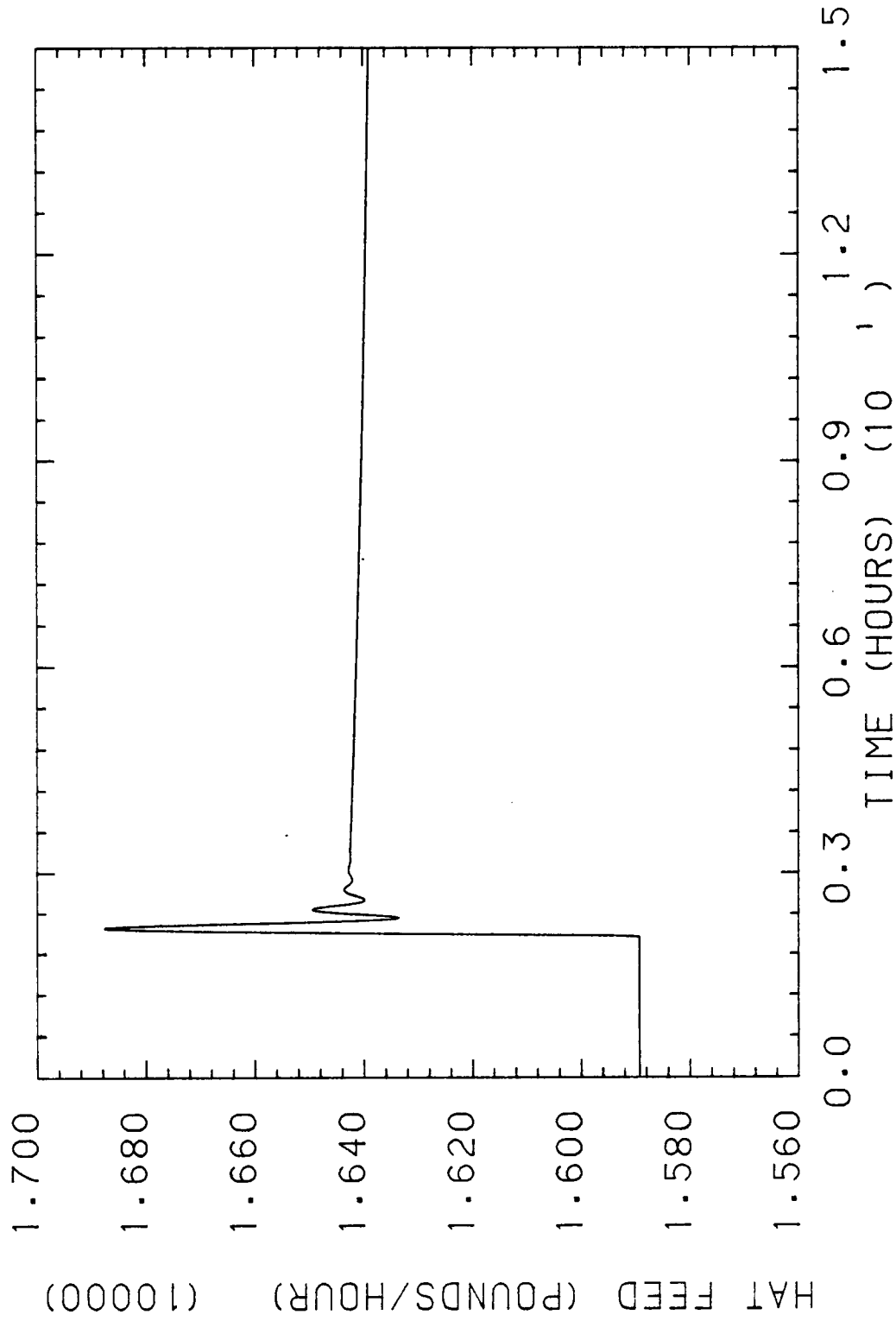


Figure 38. Control Action of Cascade Controller on Feed Temperature Disturbance

the height controller, and Figure 38 showing the response of the hat controller.

This system can be tuned to perform as well as the original system, but it is very difficult to tune. It does not seem worthwhile to add the greater complexity of the inner loop since there is no gain in performance and tuning is made much more difficult.

6.4 COMBINATION CONTROLLER

The next attempt was to make the manipulated variable a combination of both steam and feed flows. A block diagram is given in Figure 39. This is done by adding a ratio controller so that the steam flow "tracks" the feed flow, i.e. if the feed flow is increased by 50 lb/hr, the steam flow is increased by a ratio times 50 lb/hr. The ratio was chosen to be -1.035, which is the ratio between the steady state gains of the effect on the specific gravity of the feed and steam flows. Unfortunately, the addition of the steam flow to the controller slowed the response slightly, which is undesirable. This change also proved to be useless. The response of the system to the new manipulated variable is compared to that of the original system in Figure 40.

Since the evaporator has only one specified variable, that being specific gravity, and the cascade controllers

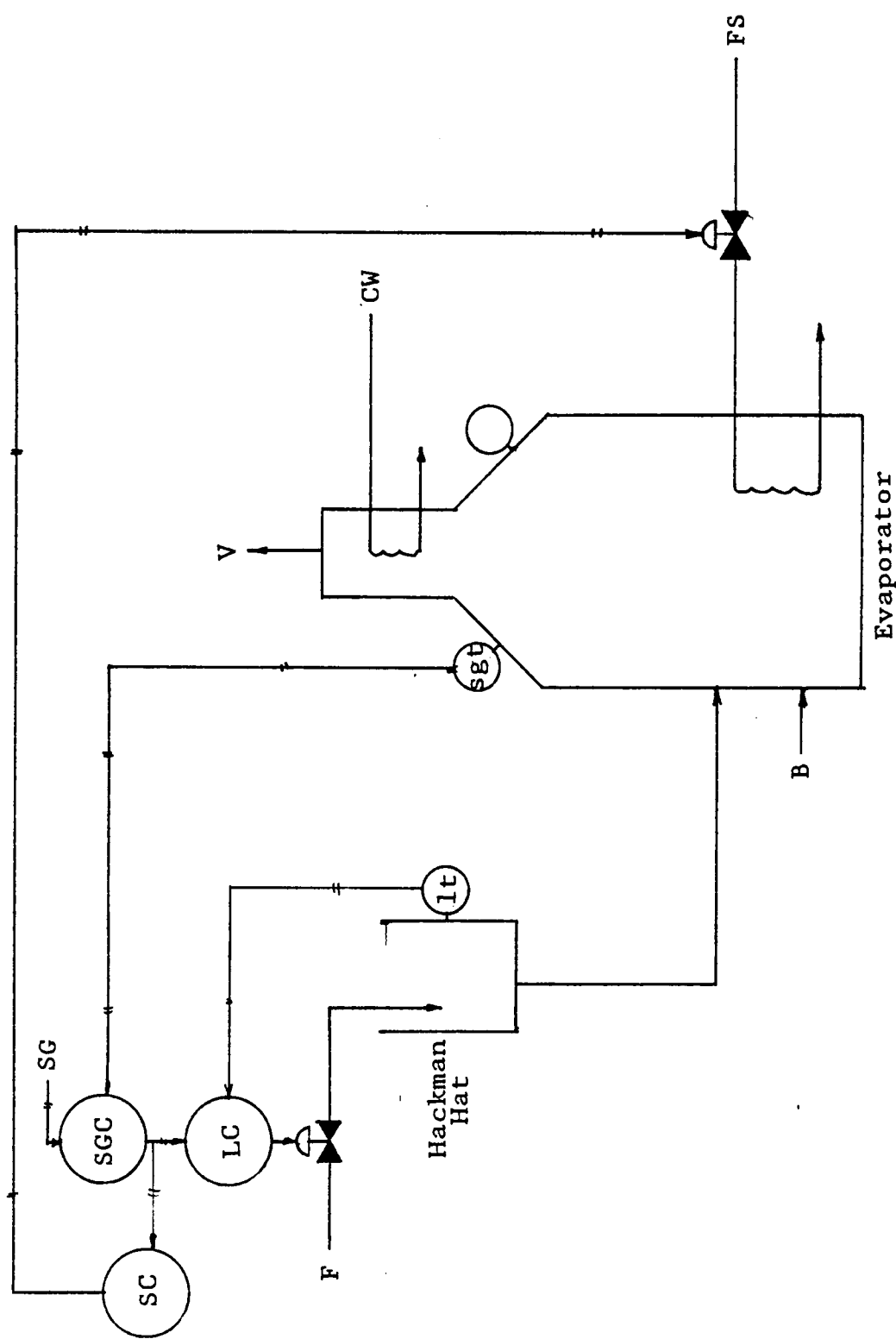


Figure 39. Control System Using Feed and Steam Flows as Manipulated Variable

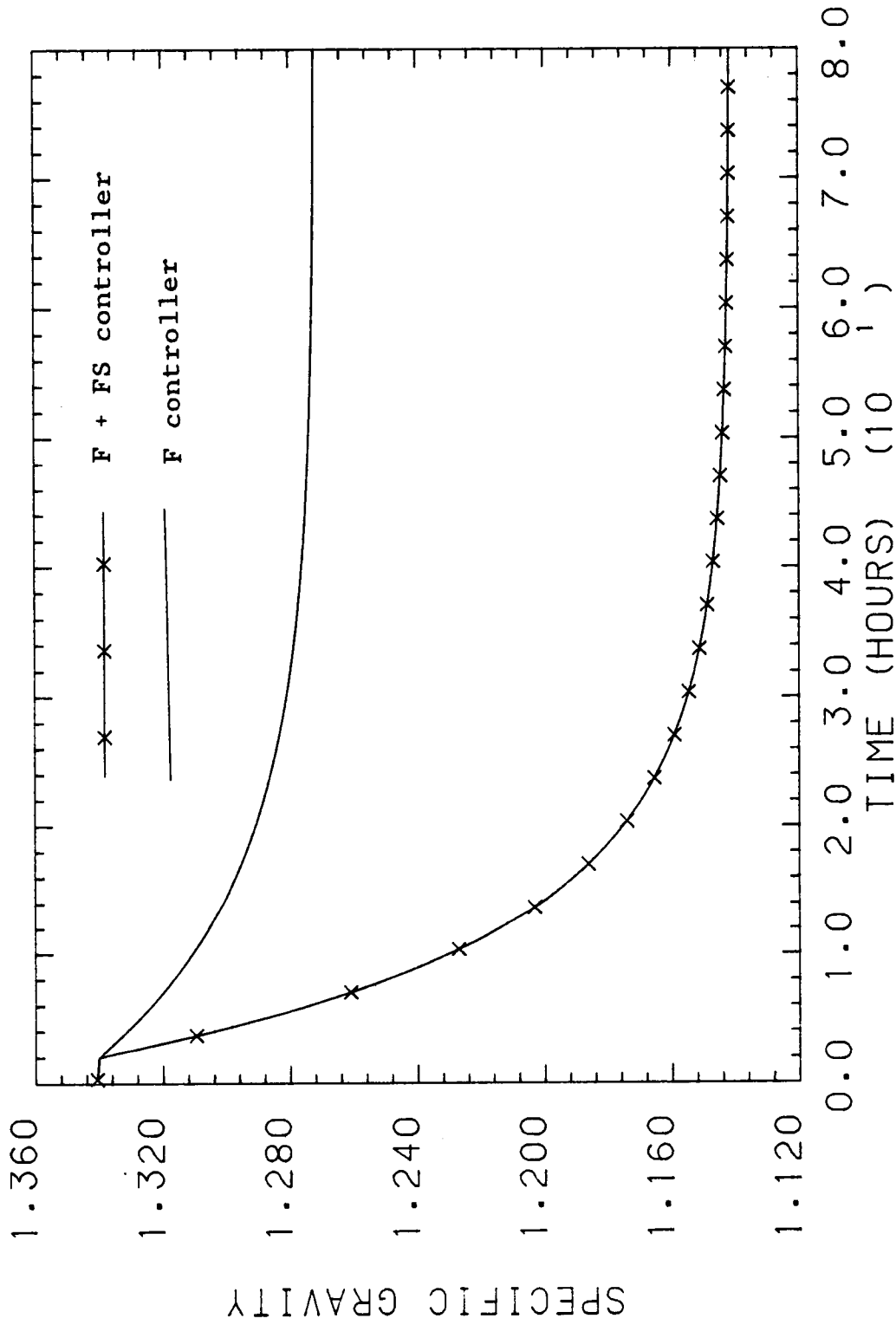


Figure 40. Comparison of System Response to Step Input from Original Control System and Dual Flow Controller

show no benefit over the present single loop control, the preliminary recommendation is to stick with the present control organization.

CHAPTER VII

RELATIVE GAIN ANALYSIS

The primary control variable for the evaporator is specific gravity. However, to help stabilize the system, the possible use of multivariable control of various intermediate variables was considered. Relative gain analysis (RGA) was used to determine possible controller pairings to be used for this purpose. RGA is a method for determining the steady state interaction between a given pairing of inputs and outputs (10).

The response of the system to five percent disturbances in steam and feed flows was used to calculate the steady state gains for use in the RGA calculations. They are given in Table 7. All possible controller pairings were tested using RGA, and the relative gain arrays are given in Tables 8 through 22.

Any control variable pairing must necessarily include specific gravity, as it is the primary control variable. Unfortunately, the only variables that do not exhibit significant steady state interaction with specific gravity are pressure and vapor flow, as shown in Tables 8 and 15.

Since vapor flow is a direct function of pressure, controlling pressure would also control vapor flow. However, controlling the vapor rate would slow the

Table 7. Process Gain Matrix for Evaporator

	Feed Flow	Steam Flow
Pressure	-1.2162×10^{-5}	3.3160×10^{-4}
Temperature	-5.0820×10^{-3}	4.7915×10^{-2}
Specific Gravity	-1.2187×10^{-4}	1.2617×10^{-4}
Liquid Height	1.7213×10^{-4}	-2.7809×10^{-4}
Vapor Flow	-4.4115×10^{-2}	1.2368
Bottoms Flow	1.0476	-1.2376

Table 8. Relative Gain Matrix for Pressure and Specific Gravity

	Feed Flow	Steam Flow
Pressure	-0.04	1.04
Specific Gravity	1.04	-0.04

Table 9. Relative Gain Matrix for Pressure and Liquid Height

	Feed Flow	Steam Flow
Pressure	0.06	0.94
Liquid Height	0.94	0.06

Table 10. Relative Gain Matrix for Pressure and Temperature

	Feed Flow	Steam Flow
Pressure	-0.04	0.96
Temperature	0.96	-0.04

Table 11. Relative Gain Matrix for Pressure and Vapor Flow

	Feed Flow	Steam Flow
Pressure	36.4	-35.4
Vapor Flow	-35.4	36.4

Table 12. Relative Gain Matrix for Pressure and Bottoms Flow

	Feed Flow	Steam Flow
Pressure	-0.05	1.05
Bottoms Flow	1.05	-0.05

Table 13. Relative Gain Matrix for Specific Gravity and Liquid Height

	Feed Flow	Steam Flow
Specific Gravity	2.78	-1.78
Liquid Height	-1.78	2.78

Table 14. Relative Gain Matrix for Specific Gravity and Temperature

	Feed Flow	Steam Flow
Specific Gravity	-10.2	11.2
Temperature	11.2	-10.2

Table 15. Relative Gain Matrix for Specific Gravity and Vapor Flow

	Feed Flow	Steam Flow
Specific Gravity	1.04	-0.04
Vapor Flow	-0.04	1.04

Table 16. Relative Gain Matrix for Specific Gravity and Bottoms Flow

	Feed Flow	Steam Flow
Specific Gravity	8.10	-7.10
Bottoms Flow	-7.10	8.10

Table 17. Relative Gain Matrix for Liquid Height and Temperature

	Feed Flow	Steam Flow
Liquid Height	-1.40	2.40
Temperature	2.40	-1.40

Table 18. Relative Gain Matrix for
Temperature and Vapor
Flow

	Feed Flow	Steam Flow
Temperature	1.03	-0.03
Vapor Flow	-0.03	1.03

Table 19. Relative Gain Matrix for
Temperature and Bottoms
Flow

	Feed Flow	Steam Flow
Temperature	4.96	-3.96
Bottoms Flow	-3.96	4.96

Table 20. Relative Gain Matrix for
Liquid Height, and Vapor
Flow

	Feed Flow	Steam Flow
Liquid Height	1.06	-0.06
Vapor Flow	-0.06	1.06

Table 21. Relative Gain Matrix for
Liquid Height and Bottoms
Flow

	Feed Flow	Steam Flow
Liquid Height	- 2.72	3.72
Bottoms Flow	3.72	- 2.72

Table 22. Relative Gain Matrix for Vapor
Flow and Bottoms Flow

	Feed Flow	Steam Flow
Vapor Flow	-0.04	1.04
Bottoms Flow	1.04	-0.04

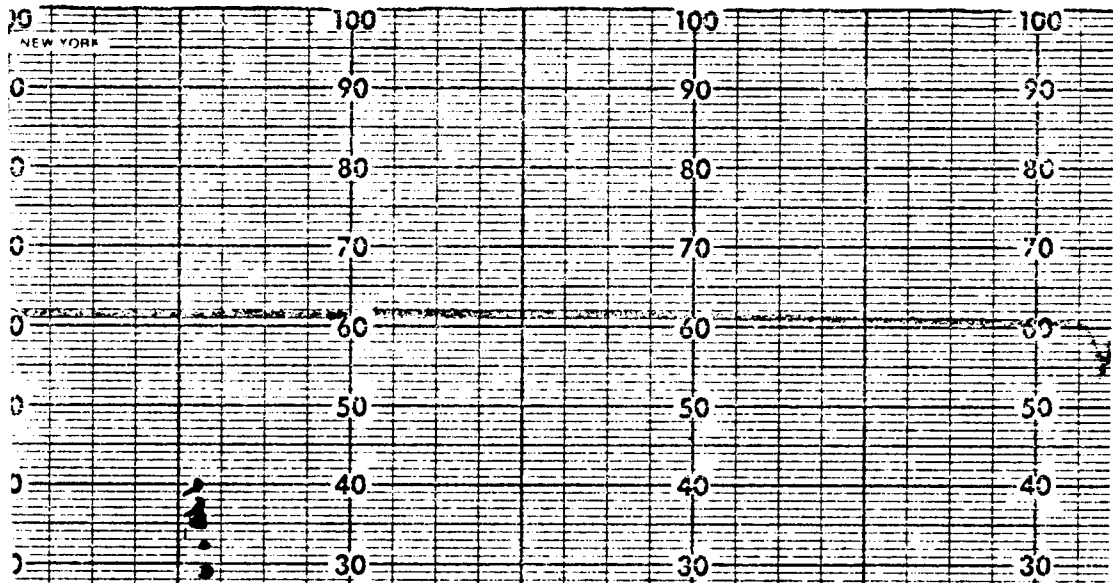
response of the system tremendously, since the evaporator changes the concentration of the liquid by boiling off excess water. Therefore, the use of multivariable control is rejected.

CHAPTER VIII

NOISE

As can be seen from the actual process data in Figure 41, there is a considerable amount of noise in the system. From times when the process was under manual control, the noise level in the specific gravity signal was determined to be plus or minus 0.003. Since the characteristic frequencies (if any) could not be determined, a computer-generated random number was used to represent the noise. The simulated noise signal is shown in Figure 42. This is the worst-case example, anyway, as it is much easier to design a filter to reduce a noise signal if its frequency is known. The addition of such a large noise signal makes control of the process very difficult. Only the original control system was used in this phase of the study.

The two most difficult problems that the noise causes are decreased stability and "bang-bang" valve manipulation, where the control valve opens and shuts repeatedly. This is undesirable, both from an operational and from a maintenance point of view. The controllers were tuned by hand, with the hat controller gain set at 660.0 and the specific gravity controller gain and integral time chosen as -620.0 and 0.4 hours. The



Specific Gravity is Reading Divided by 100 Plus a Constant

Figure 41. Actual Process Data Showing Noise Signal

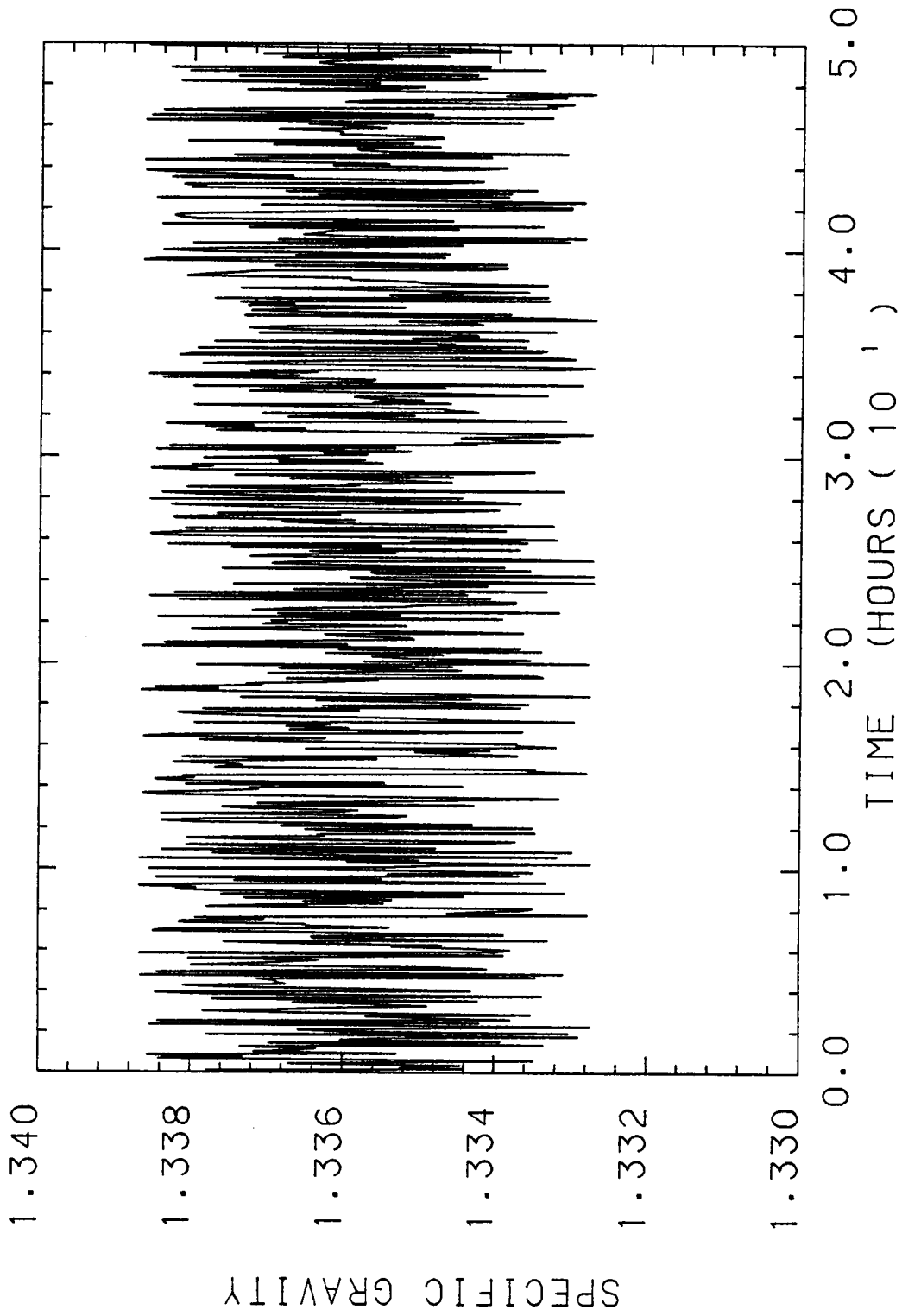


Figure 42. Simulated Noise Signal

response is shown in Figure 43. The control action is shown in Figure 44.

An integral-only (I) controller was applied to the system, but the response of the system was just too slow. The gain for the controller was chosen as -50.0. The response of this system to a 20 degree increase in feed temperature is given in Figure 45.

8.1 FILTERS

The obvious solution to this problem is the use of a filter to decrease the noise. The drawbacks of a filter are that it increases the order of the system and slows the response, both decreasing stability.

First Order Filters

A first order filter was implemented of the form

$$dX(i) = -a * x(i-1) + b * M(i-1-n)$$

$$X(i) = X_{ss} + \sum dX(i)$$

$$n = N/dt$$

$$\alpha = \exp(-dt/T)$$

$$a = -\alpha$$

$$b = K (1 - \alpha)$$

where $X(i)$ is the current value of the output, $dX(i)$ is the effect on the output of the input, X_{ss} is the steady state value of the output, N is the dead time, expressed in hours, n is the integer dead time, T is the time

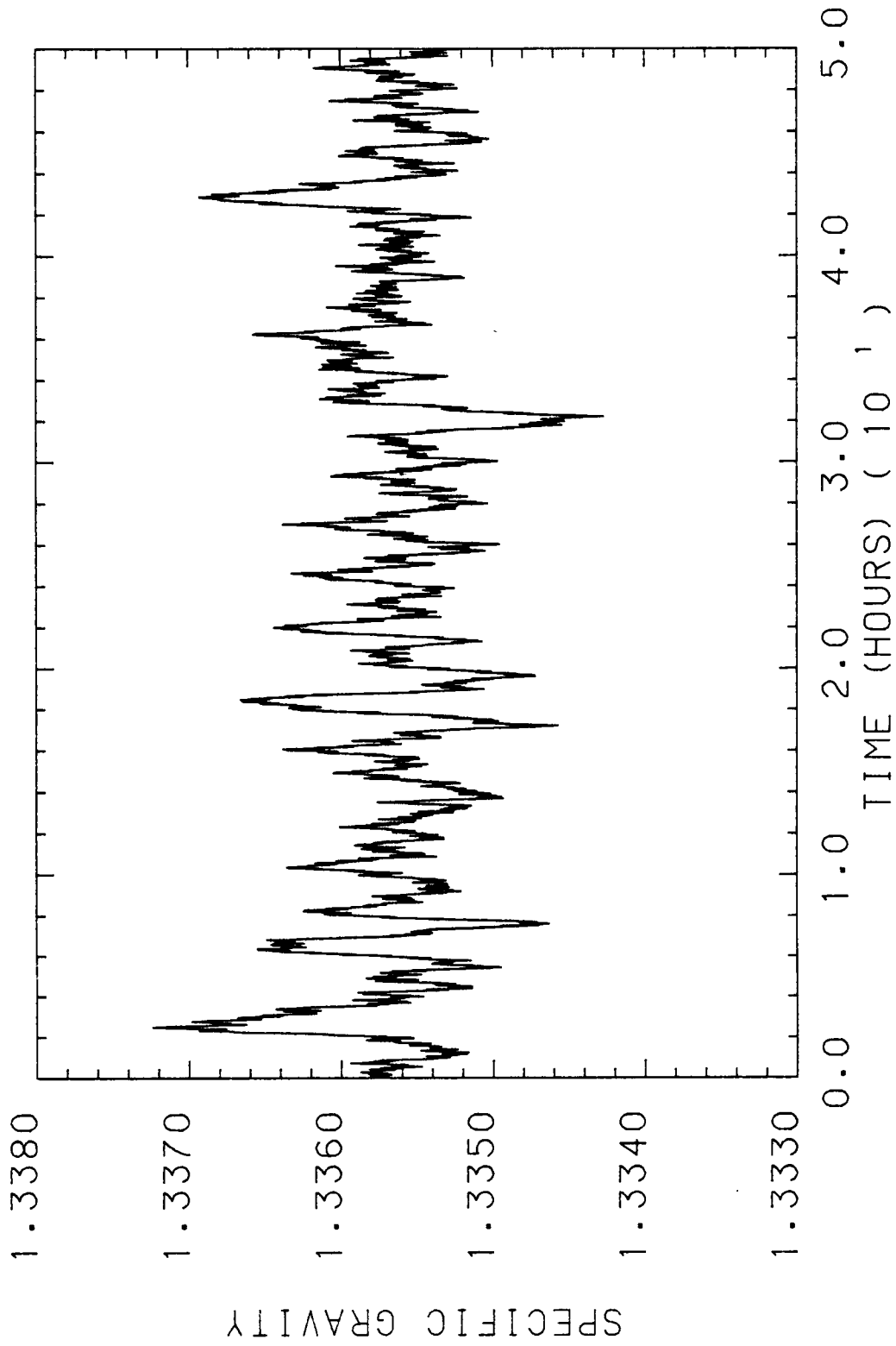


Figure 43. Original Controller on Feed Temperature Disturbance with Noise

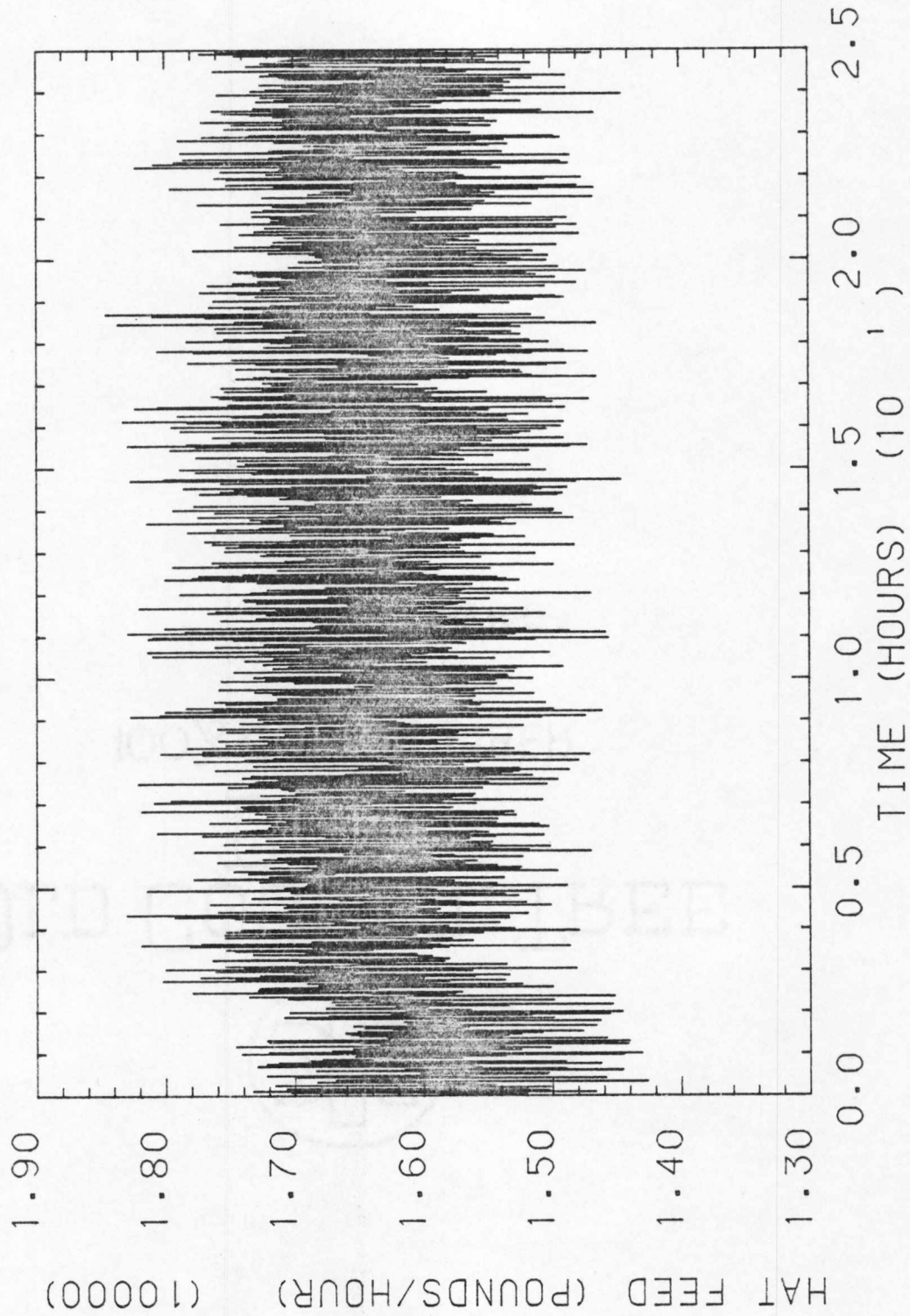


Figure 44. Control Action of Original Controller on Feed Temperature Disturbance with Noise

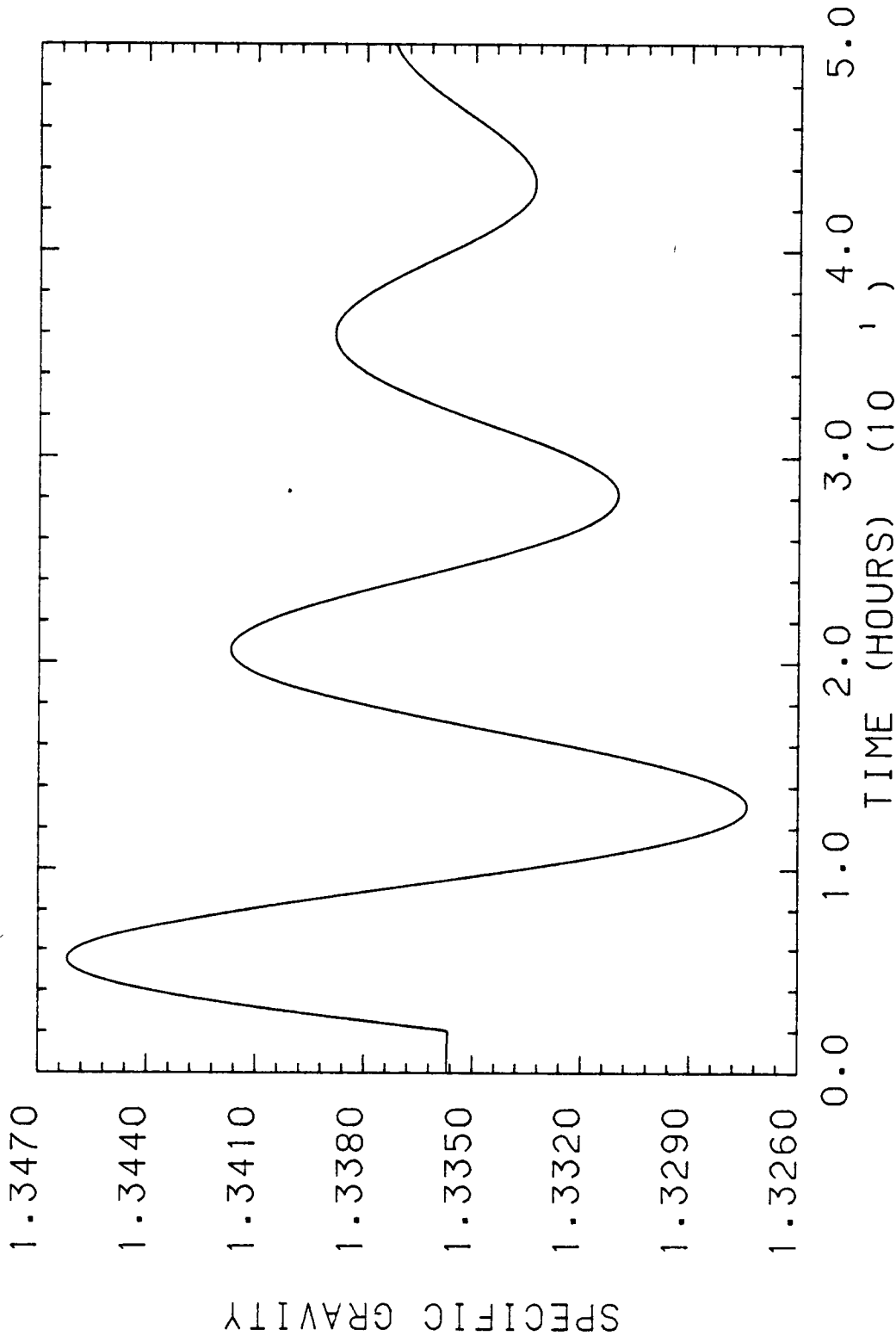


Figure 45. I Controller on Feed Temperature Disturbance with Noise

constant of the particular relation, expressed in hours, and a and b are the difference equation constants.

The filter and the controllers were tuned by hand since the pattern search proved to be very noise-sensitive. The oscillation caused by the noise was so high that it masked the deviation of the specific gravity from the set point. The response of the system is shown in Figure 46, the readout of the specific gravity instrument is shown in Figure 47, and the controller action is shown in Figure 48.

One problem with a situation such as this is that it is difficult to say what is the best control. There is a tradeoff between keeping the deviation from setpoint small and reducing the control valve oscillation. An alternate tuning point is given, showing this tradeoff. The gain of the hat controller is identical in both cases, at 660.0. The first uses a filter time constant of 0.1333 hours and a master controller gain and integral time of -3000.0 and 0.7 hours. The alternative tuning uses a filter time constant of 0.3333 hours, and a master controller gain and integral time of -500.0 and 1.5 hours. The response of the alternately tuned system to the feed temperature increase is shown in Figure 49 and the controller action appears in Figure 50.

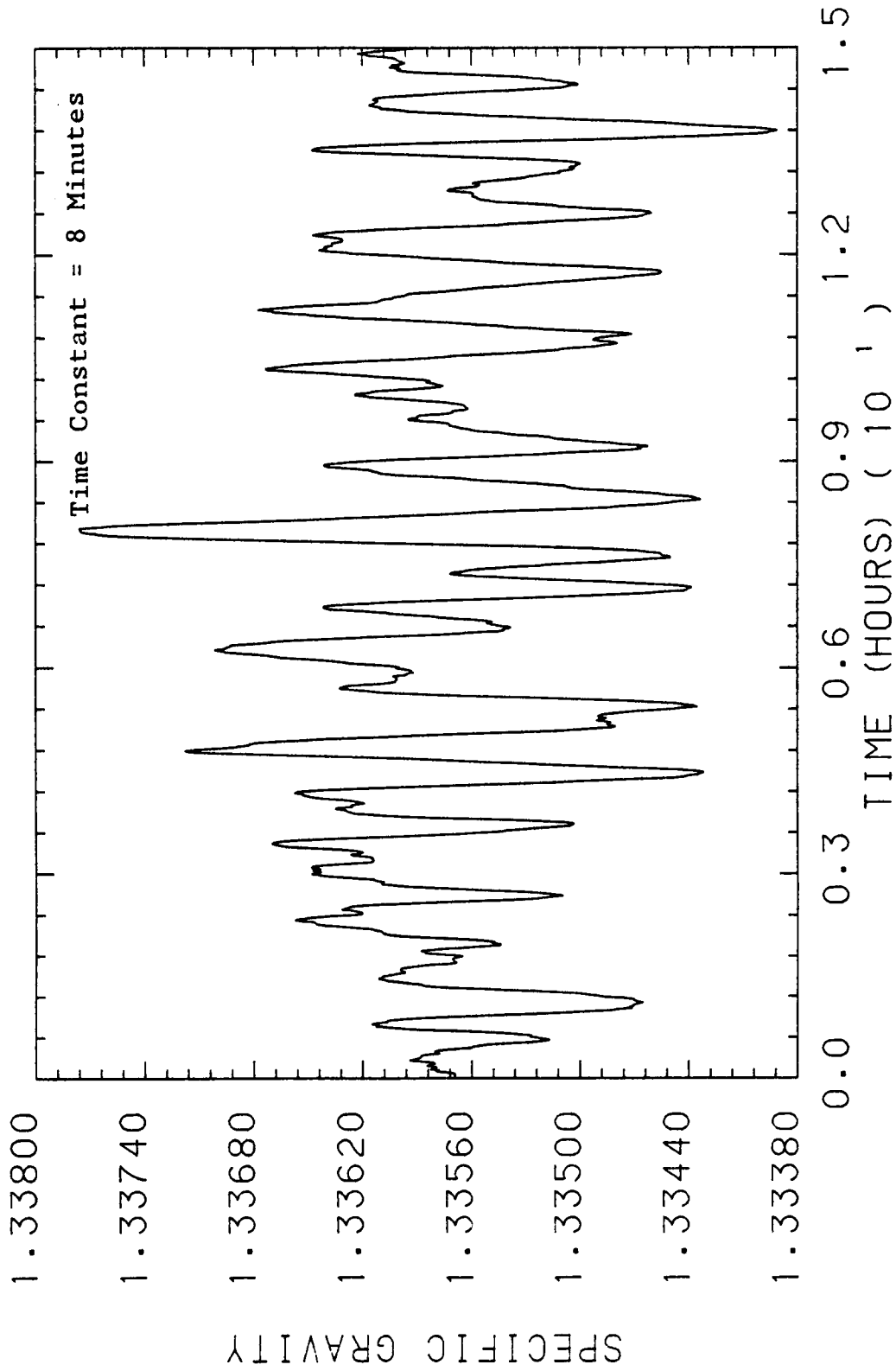


Figure 46. Response using First Order Filter

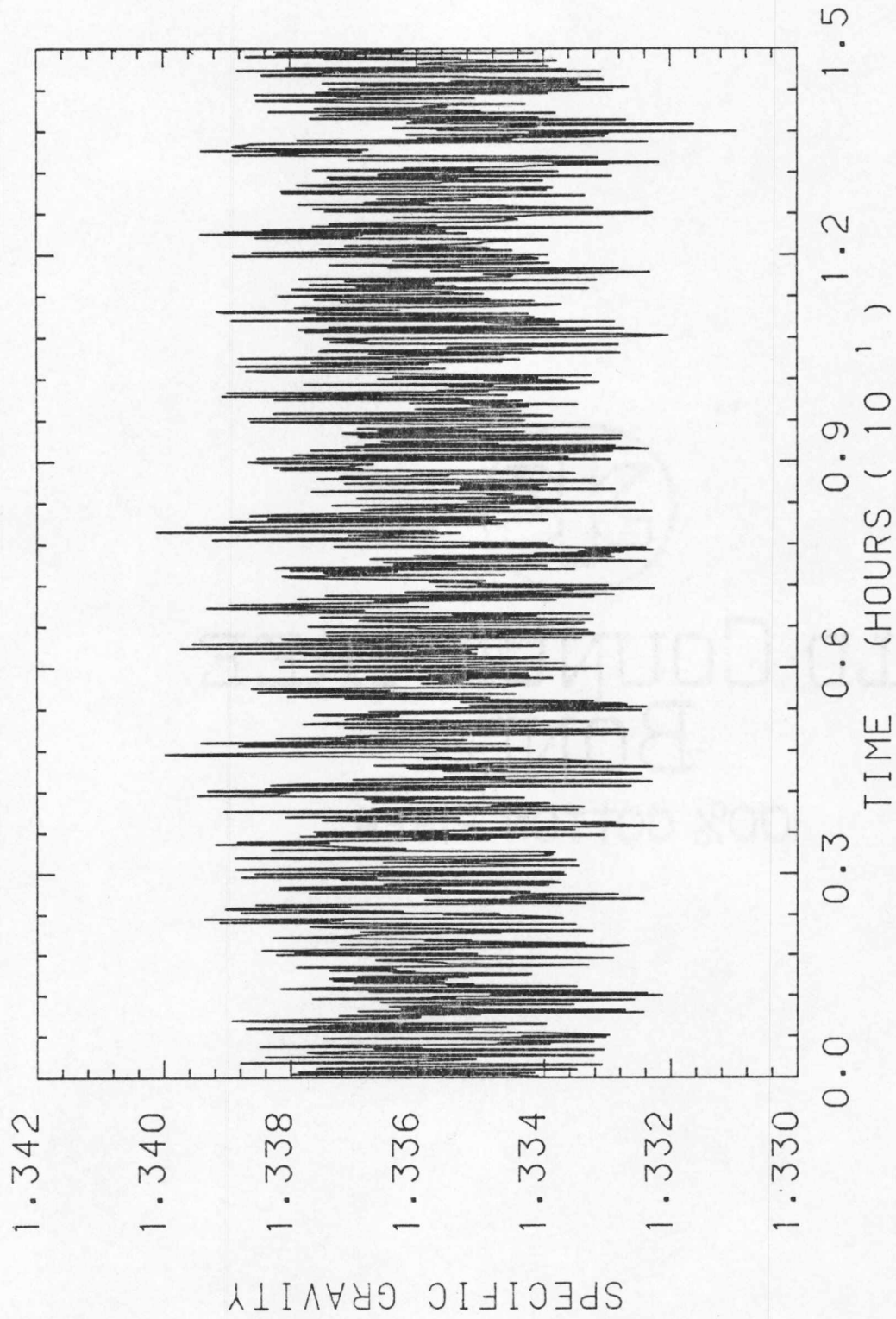


Figure 47. Signal from Specific Gravity Instrument

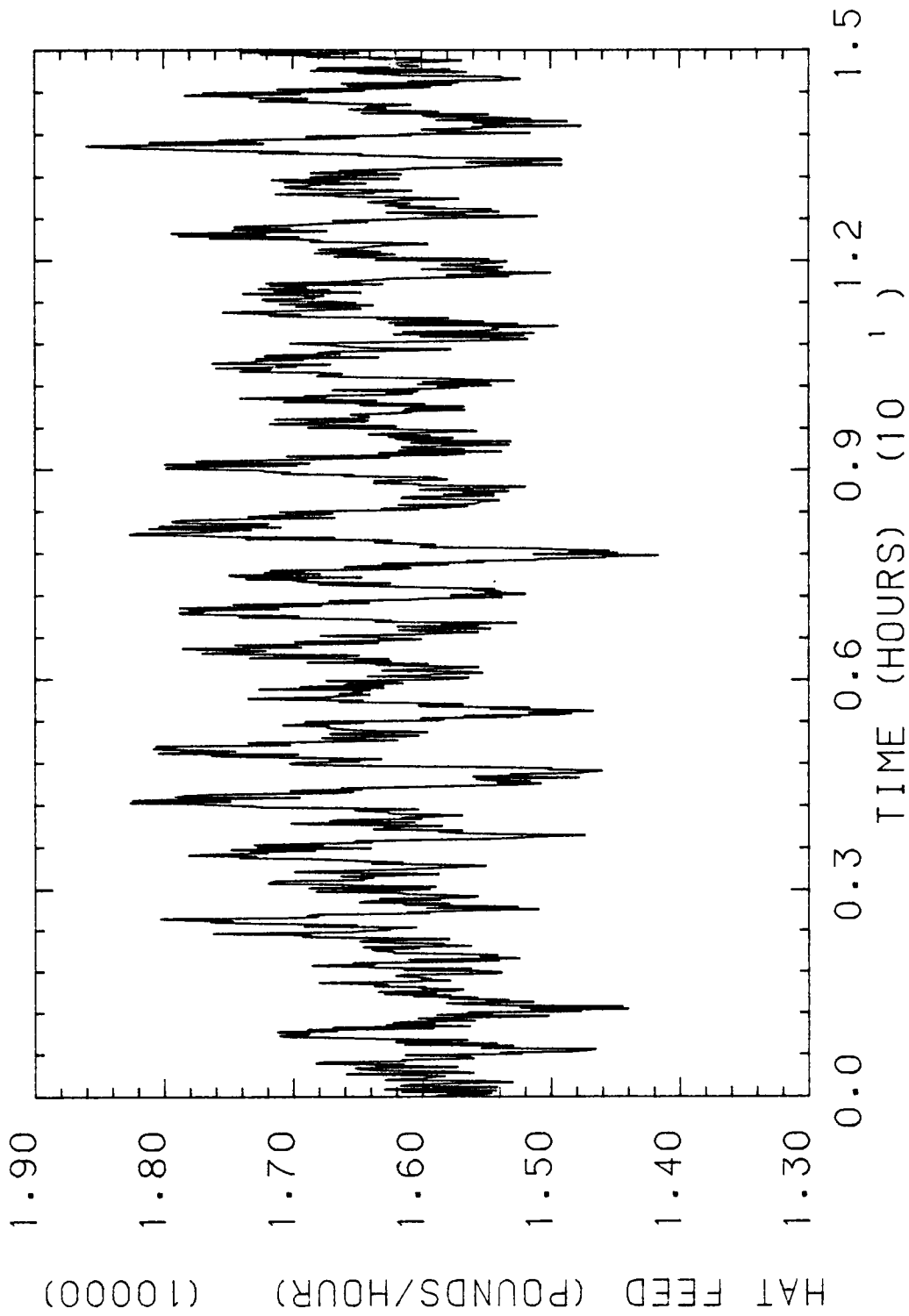


Figure 48. Control Action using First Order Filter

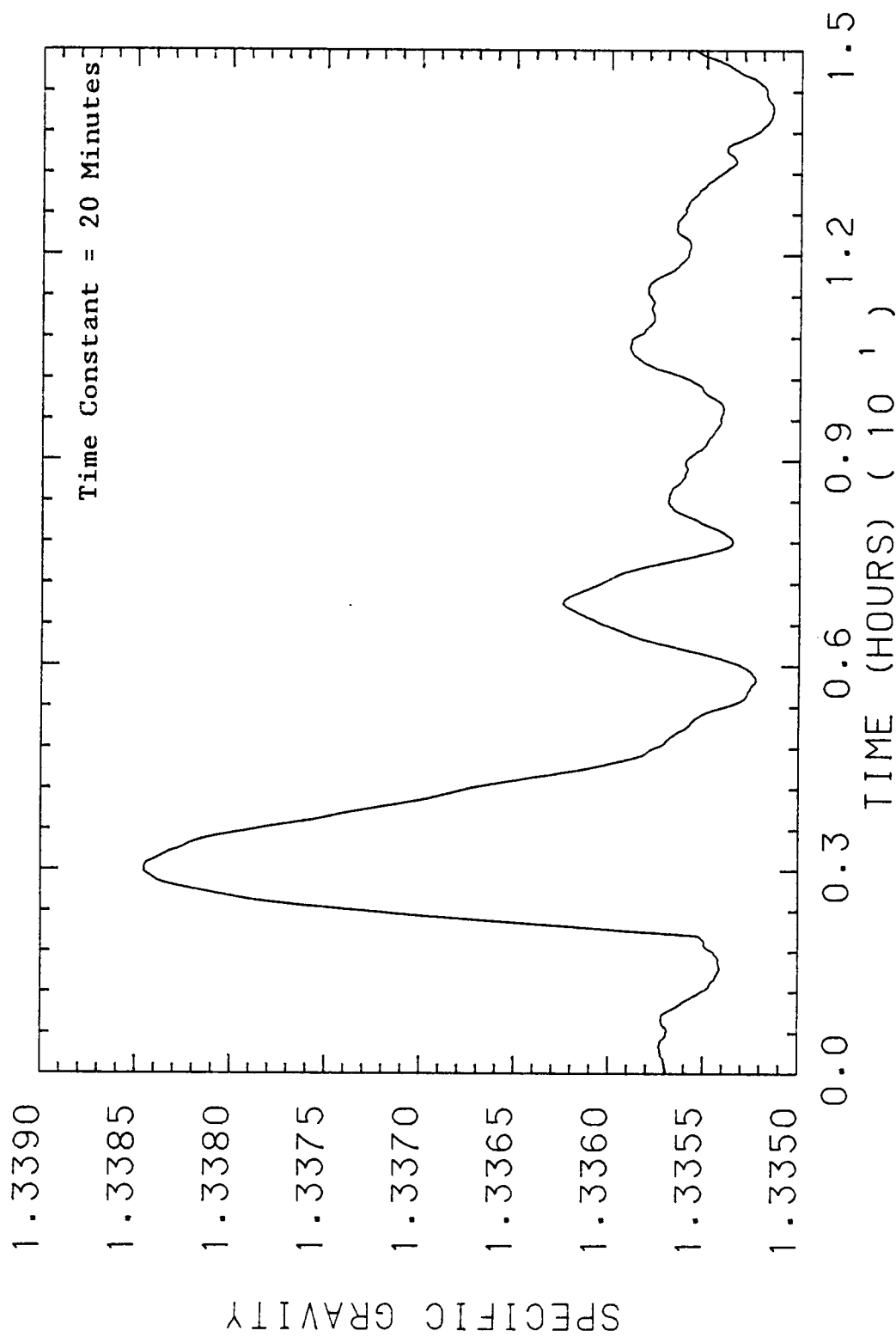


Figure 49. Alternate Response using First Order Filter

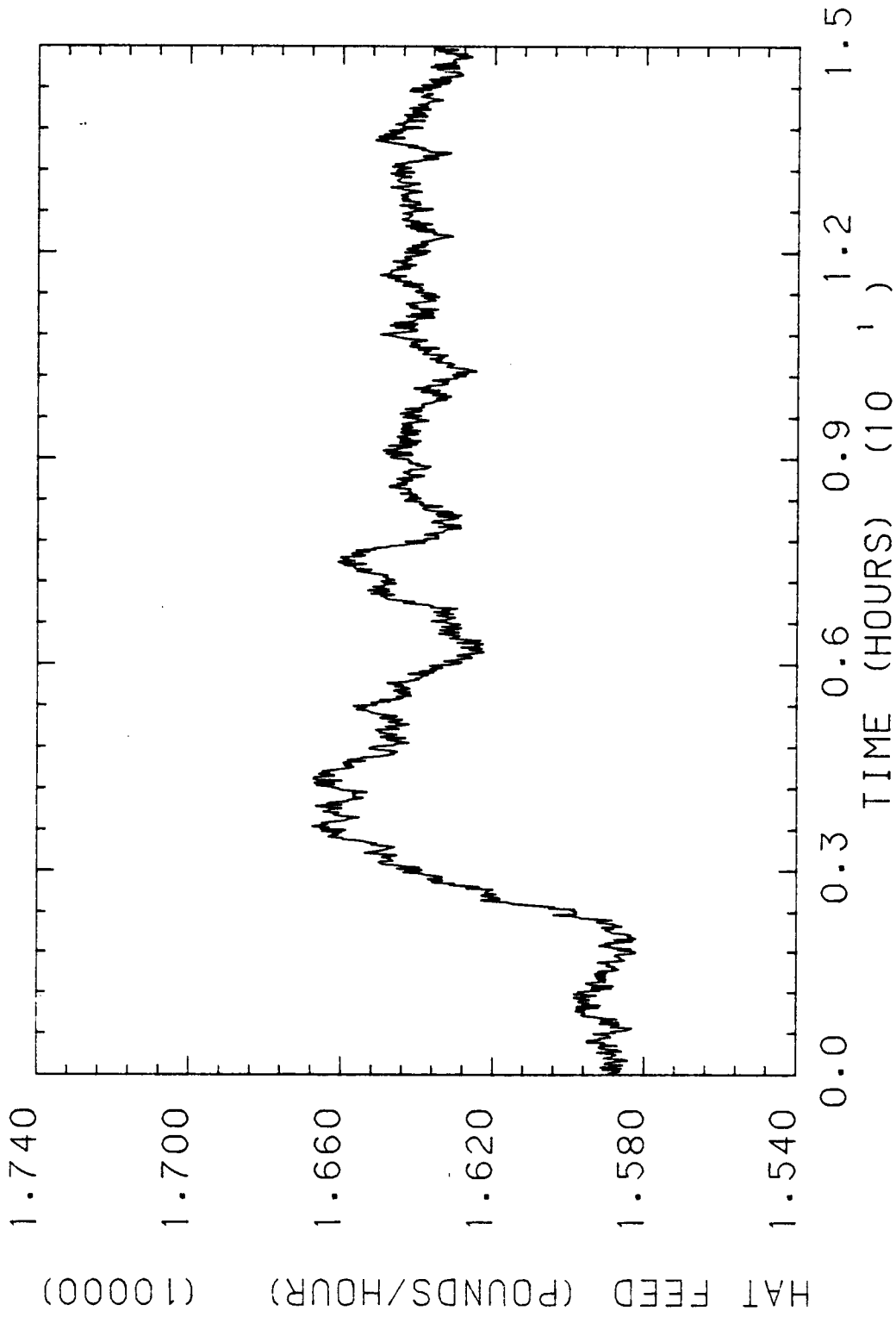


Figure 50. Alternate Control Action using First Order Filter

Notice that the higher filter time constant decreases the noise, but delays the response of the system, necessitating a greater integral time and smaller gain in the controller, which slows its response. The actual tuning choice will depend on the amount of control valve oscillation and deviation from setpoint that can be tolerated. The gain of the controller can be increased, which will lessen the initial overshoot due to the disturbance but increase the "steady state" oscillation due to noise.

Second Order Filter

Next, a second order filter was tried, using two identical time constants. This filter should show greater noise attenuation, but unfortunately it also delays the system response greatly. The second order filter was implemented in difference equation form. The equation is

$$X(i) = -a_1 * X(i-1) - a_2 * X(i-2) + b_1 * M(i-1-n) + b_2 * M(i-2-n)$$

$$a = -2 * \alpha$$

$$a = \alpha^2$$

$$b = K [1 - \alpha (1 + T / \tau)$$

$$b = K [\alpha (\alpha - 1 - T / \tau)$$

where X is the output, M is the input, and n is the integer dead time.

The filter time constant was chosen as 0.3333 hours and the system was tuned by hand, as was the first order filter. The hat controller gain was chosen as 660.0, and the master controller gain and integral times were -500.0 and 5.0 hours. The response of the system using the second order filter with the above tuning is given in Figure 51.

Split Filtering

A small improvement to the control system was made by filtering only the signal to the proportional part of the controller as shown in Figure 52. The responses of the system with complete filtering and with partial filtering are compared in Figure 53. The line with the x's is the split controller. Note that the initial overshoot is slightly less for the split controller, but the difference quickly becomes negligible.

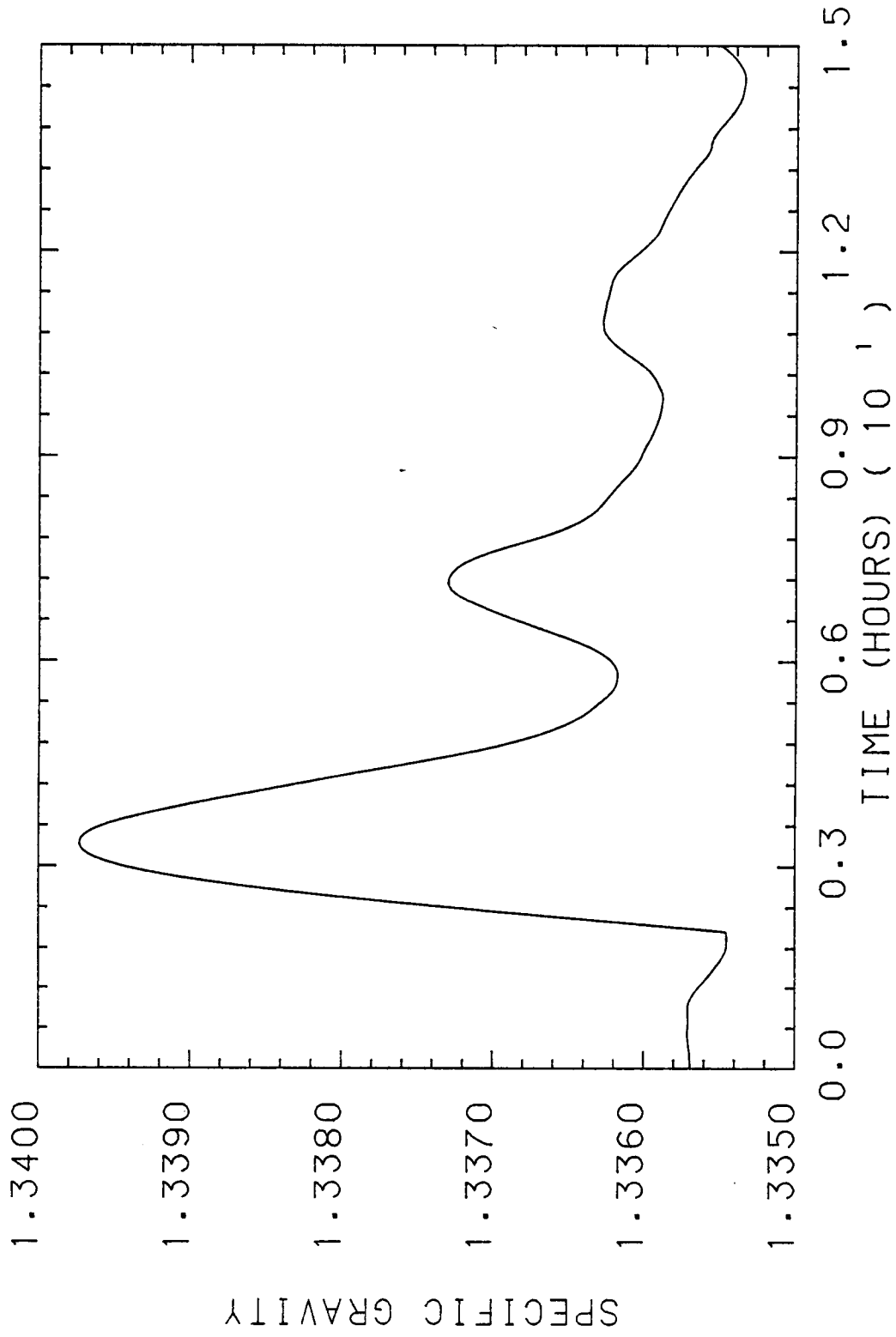


Figure 51. Response using Second Order Filter

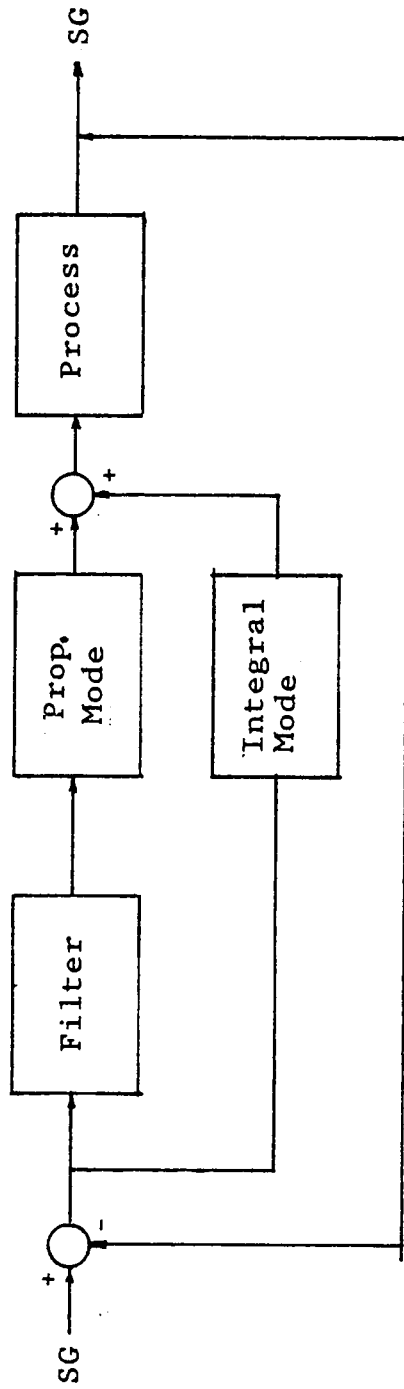


Figure 52. Flowchart of Split Filter Control System

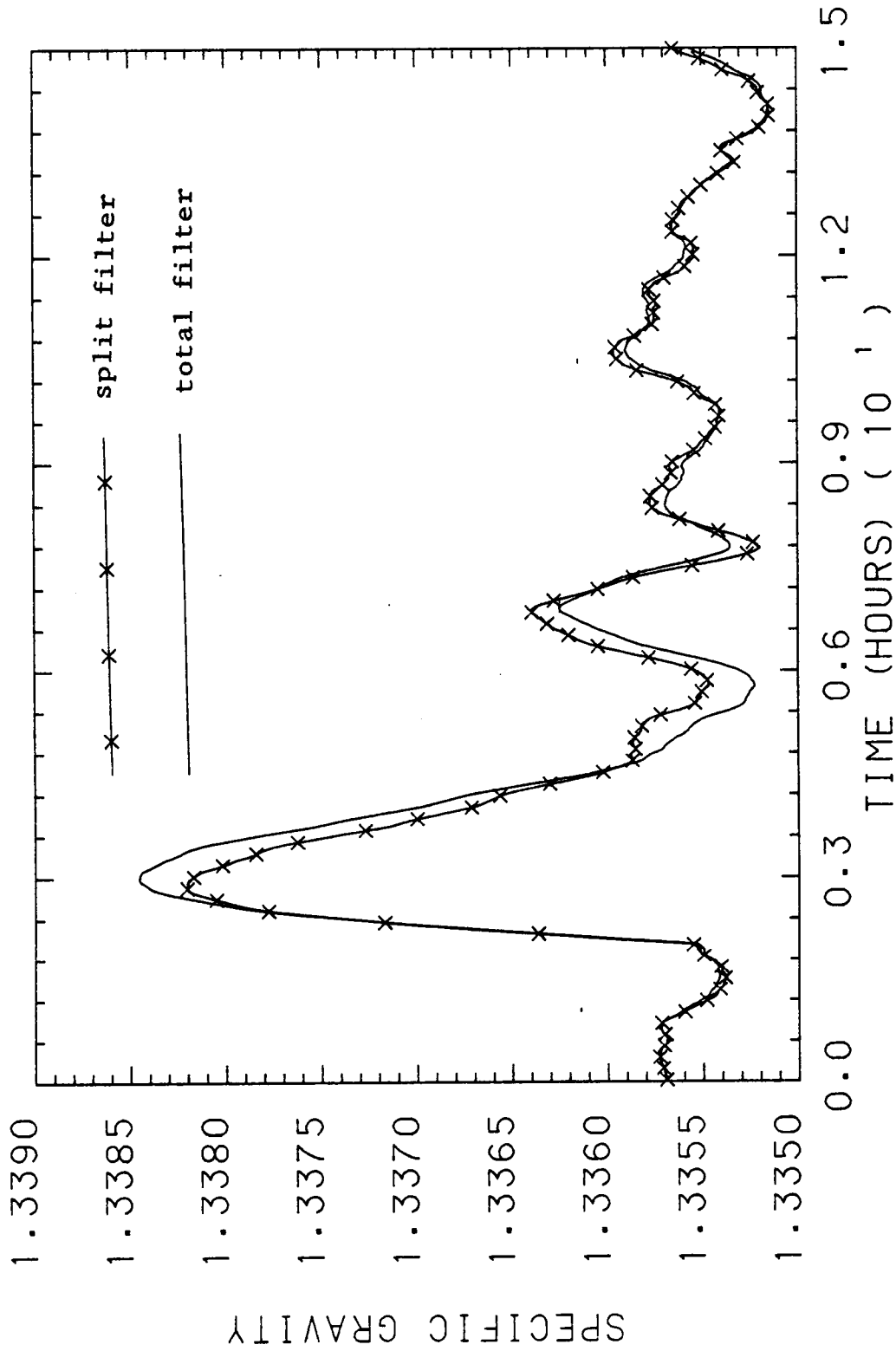


Figure 53. Effect of Filtering only Signal to Proportional Mode

CHAPTER IX

CONCLUSIONS AND RECOMMENDATIONS

The control studies showed that the control algorithm now in use at SRP is the best and simplest available. In this algorithm, the feed flow is used to control the specific gravity of the liquid in the evaporator. The use of a first order filter on the specific gravity transducer signal was found to greatly reduce control valve oscillation caused by noise. There was a small benefit from filtering only the signal to the proportional mode of the controller.

The time constant of the filter should be selected after deciding on the tradeoff between the relative amounts of overshoot and control valve oscillation that can be accepted. Tuning the specific gravity controller should be done using the ITAE + CONAC parameter used in this study. The tuning constant, β , should be selected to give the best possible response.

If it is desired to use the model for control studies for other evaporators, experiments should be undertaken to determine whether the constants in the dissociation equations fit the uranium salt solutions as well as the magnesium salt solutions that they were developed for. If a flowmeter can be found that meets reliability

requirements, the Hackman Hat flow control should be replaced. It introduces a first order lag into the system and adds to the difficulty in tuning the system since it has a level controller.

If new evaporators are to be constructed, they should have provision for a much higher steam flow rate, as the evaporators presently run at or near the maximum steam flow rate. This would make it possible to use the steam flow, rather than the feed flow, as the manipulated variable. This would be a good alternative to the system presently used.

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BIBLIOGRAPHY

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APPENDIX

FORTRAN PROGRAMS

FORTRAN program listings for the following programs are given in this appendix:

1. DLSTEM.FOR - The rigorous mathematical model of the evaporator;
2. FILP2.FOR - The linearized model with noise, a controller, and a first order filter.

DLSTEM.FOR

```

C      THIS PROGRAM WORKS WITH LIQUID DYNAMICS
C=====
C
C      THIS PROGRAM WILL SIMULATE A CONTINUOUS EVAPORATOR.
C      THE PARAMETERS ARE SET UP FOR 17.7, THE EVAPORATOR IN
C      THE SECOND URANIUM CYCLE, BUT THE PROGRAM WILL WORK FOR
C      ANY OF THE CONTINUOUS EVAPORATORS.
C=====
C      IMPLICIT REAL*8 (A-H,K-Z)
C      OPEN(FILE='STEAMS.TE1',UNIT=23,ACCESS='SEQOUT')
C      OPEN(FILE='feeds.TE1',UNIT=23,ACCESS='SEQOUT')
C      open(file='steams.te2',unit=22,access='seqout')
C      open(file='feeds.te2',unit=22,access='seqout')
C      OPEN(FILE='TFD.TE2',UNIT=22,ACCESS='SEQOUT')
C      OPEN(FILE='TFD.TE1',UNIT=23,ACCESS='SEQOUT')
C
C
C
C
C----- LIST OF VARIABLES-----
C
C      AA      ANTOINE CONSTANT FOR NITRIC ACID
C      ALPHA   EXTENT OF DISSOCIATION          (MOL/MOL)
C      AQUAD   QUADRATIC EQUATION "A"
C      AREA    CROSS-SECTIONAL AREA OF EVAPORATOR      IN**2
C
C      ATAU    EXP(-TAU)
C      AVMOL   AVERAGE MOLECULAR WEIGHT OF VAPOR      (LB/MOL)
C      AW      ANTOINE CONSTANT FOR WATER
C      B       BOTTOMS FLOW RATE                      LB/HR
C      BA      ANTOINE CONSTANT FOR NITRIC ACID
C      BQUAD   QUADRATIC EQUATION "B"
C      BW      ANTOINE CONSTANT FOR WATER
C      C       URANIUM CONCENTRATION IN EVAPORATOR      GRAM/LITER
C      CA      ANTOINE CONSTANT FOR NITRIC ACID
C
C      CQUAD   QUADRATIC EQUATION "C"
C      CW      ANTOINE CONSTANT FOR WATER
C      CP      HEAT CAPACITY                          BTU/LB/F
C      DT      INCREMENTAL TIME                        HR
C      ELITER  VOLUME OF EVAPORATOR                    LITER
C      F       FLOW RATE OF FEED                       LB/HR
C      FS      FLOW RATE OF STEAM                      LB/HR
C      FW      FLOW RATE OF COOLING WATER               LB/HR
C      GAMMAA  ACTIVITY COEFFICIENT FOR ACID
C      GAMMAW  ACTIVITY COEFFICIENT FOR WATER
C      H       HEIGHT OF LIQUID IN EVAPORATOR           (IN)
C      HO      WEIR HEIGHT IN EVAPORATOR               (IN)
C      ICOUNT  INTERNAL COUNTER
C      IDISK   INTERNAL COUNTER
C      IFLAG   INTERNAL FLAG
C      K       VAPOR FLOW CONSTANT                      (SEE PROGRAM)
C      KH      BOTTOMS FLOW CONSTANT                    (LITER/HR/IN)
C      KSALT   EQUILIBRIUM COEFFICIENT OF SALT
C      L       HEAT OF VAPORIZATION OF FEED             BTU/LB
C      LS      HEAT OF VAPORIZATION OF STEAM            BTU/LB
C      MB      INCREMENTAL MASS OF BOTTOMS              LB
C      MBA     INCREMENTAL MASS OF ACID IN BOTTOMS      LB
C      MBS     INCREMENTAL MASS OF SALT IN BOTTOMS      LB
C      MBW     INCREMENTAL MASS OF WATER IN BOTTOMS     LB

```

ITERATION COUNTER

```

COUNT=0
IDISK=0
TIME=0.0
C
C COOLING WATER FLOW RATE (LB/HR)
FW=420000.0
C
C STEAM FLOW RATE
FS=10000.0
C
C ANTOINE'S CONSTANTS FOR WATER
AW=7.949
BW=1657.4
CW=227.1
C
C ANTOINE'S CONSTANTS FOR NITRIC ACID
AA=7.616
BA=1486.2
CA=230.0
C
C HEAT CAPACITY (BTU/LB/F)
CP=0.9576315
XW=0.97475532
C
C FLUID DENSITIES (LB/GAL)
RW=8.345
RA=12.54
C
C MOLECULAR WEIGHTS (LB/MOL)
MWA=63.0
MWW=18.03
MWS=394.0
C
C VENT PRESSURE (IN. H2O)
PC=406.0
C
C HEIGHT OF LIQUID CONSTANTS
HO=89.75
AREA=11310.0
KH=684.0
C
C COOLING WATER IN TEMPERATURE (F)
T1=95.0
C
C EVAPORATOR COMPOSITION (WT/WT)
XES=0.3904414592
XEA=0.01139601651
XEW=1.0-XEA-XES
C
C MAXIMUM VOLUME OF EVAPORATOR (GALLONS)
MAXVOL=4740.2075103
C
C SPECIFIC GRAVITY
SG=1.335692373
C
C FLOW CONSTANT (LB/HR/(IN. H2O)**1/2)
K=9185.0
C
C VAPOR RATE (LB/HR)
V=11618.96720

```

```

C
C   BOTTOMS RATE   (LB/HR)
C   B=4274.028301
C
C   HEAT OF VAPORIZATION OF FEED   (BTU/LB)
C   L=959.0
C
C   HEAT OF VAPORIZATION OF STEAM   (BTU/LB)
C   LS=932.0
C
C   TEMPERATURE IN EVAPORATOR   (F)
C   T=224.3048484
C
C   TIME INCREMENT   (HR)   1 second
C   DT=1.0/3600.0
C
C   FEED RATE   (LB/HR)
C   F=15893.0
C
C   FEED TEMPERATURE   (F)
C   TF=175.0
C
C   TOTAL MASS IN EVAPORATOR   (LB)
C   ME=49212.2807049
C
C   FEED COMPOSITION   (WT/WT)
C   XFS=0.105
C   XFA=0.005
C   XFW=0.890
C
C   VAPOR COMPOSITION   (WT/WT)
C   YVA=0.000759082188
C   YVW=1.0-YVA
C
C   INDICATE WHETHER TO WRITE DATA TO DISK
C   WRITE(5,6500)
C   READ(5,*)IFLAG
C
C   MES=XES*ME
C   MEW=XEW*ME
C   MEA=ME-MES-MEW
C
C   WRITE HEADINGS ON TELETYPE
C   WRITE(05,1400)
C   WRITE(05,1500)
C   WRITE(05,1600)
C   WRITE(05,1650)
C   WRITE(05,1700)
C
C   IF(IFLAG.EQ.0)GOTO 5
C   WRITE HEADINGS ON DISK
C   WRITE(23,1400)
C   WRITE(23,1500)
C   WRITE(23,1600)
C   WRITE(23,1650)
C   WRITE(22,1700)
C   WRITE(22,1750)
C
C   INCREMENTAL FEED, BOTTOMS, AND VAPOR
C   MV=V*DT
C   IF(TIME.GT.9.99999)TF=195.0

```

```

C      IF (TIME.GT.9.99999) FS=9500.0
C      if (time.gt.9.99999) f=17482.3
C      MF=F*DT
C      MB=B*DT
C
C      VAPOR COMPONENTS
C      AVMOL=YVA*MWA+YVW*MWW
C      MOLVAP=MV/AVMOL
C      MOLVA=YVA*MOLVAP
C      MOLVW=YVW*MOLVAP
C      MVA=MOLVA*MWA
C      MVW=MOLVW*MWW
C
C      FEED COMPONENTS
C      MFS=XFS*MF
C      MFA=XFA*MF
C      MFW=MF-MFS-MFA
C
C      BOTTOMS COMPONENTS
C      MBA=XEA*MB
C      MBS=XES*MB
C      MBW=MB-MBA-MBS
C
C      TOTAL
C      MEW=MEW+MFW-MVW-MBW
C      MES=MES+MFS-MBS
C      MEA=MEA+MFA-MVA-MBA
C      ME=MEA+MES+MEW
C      XES=MES/ME
C      XEA=MEA/ME
C      XEW=1.0-XES-XEA
C
C      EVAPORATOR VOLUME
C      VOLE=ME*0.453/3.785/SG
C      vole=4409.5354
C
C-----SPECIFIC GRAVITY-----
C
C      C=CONCENTRATION OF URANIUM IN SOLUTION (GRAMS/LITER)
C      MEU=MES*453.0*238.0/394.0
C      ELITER=VOLE*3.785
C      C=MEU/ELITER
C
C      N=NITRIC ACID NORMALITY
C      MMOLEA=MEA*453.0/63.0
C      N=MMOLEA/ELITER
C
C      TC=TEMPERATURE IN CENTIGRADE
C      TC=(T-32.0)*5.0/9.0
C
C      SPECIFIC GRAVITY CALCULATED BY EMPIRICAL EQUATION
C      SG=1.345E-3*C+1.0042+2.4E-6*(TC**2)+3.14E-5*C*N
C      SG=(SG+2.51E-2*N)/(1.0+8.4E-6*(TC**2))
C
C-----
C
C      SPECIFIC HEAT
C
C      CP=1.002028*(XW**2)+0.005718*XW
C
C      BOTTOMS FLOW

```

```

H=VOLE*231.0/AREA
IF(H.LE.H0)GOTO 6
VOLB=KH*DSQRT(H-H0)
B=VOLB*3.785*SG/0.453
GOTO 7
6 B=0.0
C VOLB=VOLE-MAXVOL
C IF(VOLB.LE.0.0)VOLB=0.0
C B=VOLB*3.785*SG/0.453
C IF(VOLE.GE.MAXVOL)VOLE=MAXVOL
7 IF(IFLAG.EQ.0)GOTO 14
C WRITE TO DISK
IF(IDISK.NE.1.0/(15.0*DT))GOTO 14
C IF(TIME.LT.0.995)GOTO 14
WRITE(23,1200)FW,FS,F,B,V
WRITE(23,1200)SG,PE,TIME,ME,H
WRITE(23,1200)T,TF,C,PA,PW
WRITE(23,1350)PARA,PARW,VOLE,ATAU
WRITE(22,1200)XEA,XES,XFA,XFS,YVA
WRITE(22,1325)TIME,GAMMAA,GAMMAW,XPA,XPW
IDISK=0
C
C WRITE ON TELETYPE
14 IF(ICOUNT.NE.1.0/DT)GOTO 20
WRITE(05,*)FW,FS,F,B,V
WRITE(05,*)SG,PE,TIME,ME,H
WRITE(05,*)T,TF,C,PA,PW
WRITE(05,*)PARA,PARW,VOLE,ATAU
WRITE(05,*)XEA,XES,XFA,XFS,YVA
WRITE(05,*)GAMMAA,GAMMAW,XPA,XPW
ICOUNT=0
C
C TEMPERATURE
20 IF(b.LE.0.0)b=1.0
TAU=ME/B
ATAU=DEXP(-DT/TAU)
T=ATAU*T+(1-ATAU)*(F*TF/B-V*L/B+FS*LS/B)
C
C PRESSURE
MOLEA=MEA/MWA
MOLEW=MEW/MWW
MOLES=MES/MWS
MOLTOT=MOLEA+MOLEW+MOLES
XA=MOLEA/MOLTOT
XW=MOLEW/MOLTOT
XS=1.0-XA-XW
TK=TC+273.16
KSALT=0.0015*DEXP(1459.0/TK)
AQUAD=(1.0+KSALT)*XA
BQUAD=2*XS*(1.0+KSALT)-KSALT*XA+KSALT
CQUAD=-(KSALT+2.0*KSALT*XS)
ALPHA=(-BQUAD+DSQRT(BQUAD**2-4.0*AQUAD*CQUAD))/(2.0*AQUAD)
XPA=((1.0-ALPHA)*XA)/(1.0+ALPHA*XA+2.0*XS)
XPW=XW/(1.0+ALPHA*XA+2.0*XS)
PW=10.0**((AW-BW)/(TC+CW))
PA=10.0**((AA-BA)/(TC+CA))
GAMMAA=DEXP(-2.52+6.21*XA-3.10*(XA**2)+23.83*XS-
1 24.20*(XS**2)-15.8*XA*XS)
GAMMAW=DEXP(-0.17*XA-3.62*(XA**2)-4.47*XS-15.83*(XS**2)
1 -28.20*XA*XS)

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```

PE=GAMMAA*XPA*PA+GAMMAW*XPW*PW
YVA=(GAMMAA*XPA*PA)/PE
PARA=GAMMAA*XPA*PA
PARW=GAMMAW*XPW*PW
YVW=(GAMMAW*XPW*PW)/PE
CHECK=YVA+YVW
C
PW=PW*407.0/760.0
PA=PA*407.0/760.0
PE=PE*407.0/760.0
IF(PE.LT.PC)PE=PC
C
C VAPOR COMPOSITION
V=K*DSQRT(PE-PC)
C
C COOLING WATER OUT TEMPERATURE
T2=T1+V*L/(FW*CP)
C
C INCREMENT COUNTER
ICOUNT=ICOUNT+1
IDISK=IDISK+1
IF(IFLAG.EQ.0)GOTO 17
IF(TIME.GT.70.0)STOP
17 IF(TIME.GT.70.0)STOP
TIME=TIME+DT
GOTO 5
C
1200 FORMAT(5G24.10)
1300 FORMAT(5G24.10,/)
1325 FORMAT(5G24.10,/)
1350 FORMAT(4G24.10,/)
1400 FORMAT(1H,14X,'FW',22X,'FS',23X,'F',24X,'B',24X,'V')
1500 FORMAT(1H,14X,'SG',22X,'PE',21X,'TIME',20X,'ME',23X,'H')
1600 FORMAT(1H,14X,'T',24X,'TF',23X,'C',23X,'PA',23X,'PW')
1650 FORMAT(1H,12X,'PARA',22X,'PARW',22X,'VOLE',
1      22X,'ATAU',/)
1700 FORMAT(1H,13X,'XEA',22X,'XES',20X,'XFA',22X,'XFS',22X,'YVA')
1750 FORMAT(1H,12X,'TIME',/)
6500 FORMAT(/,'WRITE TO DISK? (ENTER 1 FOR YES, 0 FOR NO)')
STOP
END

```

FILP2.FOR

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C      THIS PROGRAM IS A Z-TRANSFORM MODEL OF THE
C      CONTINUOUS EVAPORATOR MODEL.  IT ONLY CALCULATES
C      THE EFFECT OF 6 INPUT VARIABLES, (F,FS,PC,TF,XFA,XFS)
C      ON 6 OUTPUT VARIABLES (PE,SG,T,B,V,H).
C
C      activate the hackman hat flow controller
C      Now put the sg controller on the hat height
C      Now add the noise and filter
C
C-----List of Variables-----
C
C      A1      Difference Equation Constant for the Evaporator
C      A1f     Difference Equation Constant for the Hackman Hat
C      A1h     Difference Equation Constant for the Hackman Hat
C      Afil    Difference Equation Constant for the Filter
C      Alpha   CONAC Tuning Constant
C      B       Bottoms Flow, lb/hr
C      B1      Difference Equation Constant for the Evaporator
C      B1f     Difference Equation Constant for the Hackman Hat
C      B1h     Difference Equation Constant for the Hackman Hat
C      Bfil    Difference Equation Constant for the Filter
C      Bss     Steady State Bottoms Flow Rate, lb/hr
C      CONAC   Integral of the Absolute Derivative of the Control
C              Action
C      COST    Parameter to be Minimized by Pattern Search
C      DelB    Deviation of Bottoms Flow from Steady State, lb/hr
C      DelF    Deviation of Feed Flow from Steady State, lb/hr
C      DelH    Deviation of Evaporator Liquid Height from Steady
C              State, inches
C      DelHH   Deviation of Hackman Hat Liquid Height from Steady
C              State, inches
C      DelPe   Deviation of Evaporator Pressure from Steady State,
C              inches water
C      DelSG   Deviation of Evaporator Liquid Specific Gravity from
C              Steady State
C      DelT    Deviation of Evaporator Temperature from Steady State, F
C      DelV    Deviation of Vapor Flow from Steady State, lb/hr
C      dF1     Deviation of Hackman Hat Feed Flow from Steady State,
C              lb/hr
C      dT      Time Increment, hours
C      Ernoiz  Deviation of Specific Gravity from Setpoint with
C              Noise Signal
C      Erorsg  Filtered Deviation of Specific Gravity from Setpoint
C              with Noise Signal
C      Error   Deviation of Specific Gravity from Setpoint
C      Erorh   Deviation of Hackman Hat Liquid Level from Setpoint,
C              inches
C      F       Evaporator Feed Flow, lb/hr
C      F1      Hackman Hat Feed Flow, lb/hr
C      F1m     Deviation of Hackman Hat Feed Flow from Steady State,
C              lb/hr
C      Flss    Steady State Hackman Hat Feed Flow Rate, lb/hr
C      Fint    Total Feed Used During Simulation, pounds
C      Fs      Steam Flow Rate, lb/hr
C      Fsint   Total Steam Used During Simulation, pounds
C      Fss     Evaporator Feed Flow at Steady State, lb/hr
C      Fsss    Steam Flow at Steady State, lb/hr
C      H       Evaporator Liquid Height, inches
C      Hhat    Hackman Hat Liquid Height, inches
C      Hhatss  Hackman Hat Liquid Height at Steady State, inches

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c      Hset      Hackman Hat Liquid Height Setpoint, inches
c      Hsetss    Hackman Hat Liquid Height Setpoint at Steady State,
c                inches
c      Hss       Evaporator Liquid Height at Steady State, inches
c      I         Internal Program Counter
c      II        Internal Program Counter
c      Index     Internal Program Counter
c      ISEsg     Integral Squared Error for the Specific Gravity
c                Controller
c      ITAEh     Integral Absolute Error for the Height Controller, inches
c      ITAEsg    Integral Time times Absolute Error for the Specific
c                Gravity Controller
c      JJ        Internal Program Counter
c      JK        Internal Program Counter
c      K         Gains for the Transfer Functions
c      KCh       Gain for the Hackman Hat Controller
c      KCsg      Gain for the Specific Gravity Controller
c      Kf        Gain for the Hackman Hat Transfer Function
c      Kh        Gain for the Hackman Hat Transfer Function
c      L         Internal Program Counter
c      M         Internal Program Counter
c      N1        Internal Program Counter
c      N         Internal Program Counter
c      NUMfil    Integer Time Constant for the Filter, hours
c      OF1       Previous Value of F1, lb/hr
c      OFeed     Previous Value of F, lb/hr
c      OHhat     Previous Value of Hhat, inches
c      OHTset    Previous Value of Hset, inches
c      Osg       Previous Value of SG
c      Osgfil    Previous Filtered Value of SG
c      OX        Previous Value of X
c      Pc        Condenser Pressure, inches water
c      Pe        Evaporator Pressure, inches water
c      Pess      Steady State Value of Pe, inches water
c      SG        Specific Gravity
c      SGclen    Specific Gravity Signal without Noise
c      SGnoiz    Specific Gravity Signal with Noise
c      SGset     Setpoint for Specific Gravity Controller
c      SGss      Steady State Value of SG
c      SUMsg     Internal Sum for PI Specific Gravity Controller
c      T         Evaporator Temperature, F
c      Tau       Time Constant for Transfer Functions, hours
c      Tauf      Time Constant for Hackman Hat Transfer Functions, hours
c      Tauh      Time Constant for Hackman Hat Transfer Functions, hours
c      Tf        Feed Temperature, F
c      Theta     Dead Time for Transfer Functions, hours
c      Time      Elapsed Time for Simulation, hours
c      Tlsg      Integral Time for Specific Gravity Controller, hours
c      Tss       Steady State Value for T, F
c      V         Vapor Flow Rate, lb/hr
c      Vss       Steady State Value for V, lb/hr
c      X         Output for the Transfer Functions
c      XFA       Weight Fraction of Nitric Acid in Liquid
c      XFS       Weight Fraction of Salt in Liquid
c
c      REAL K(6,20),M(6,6000),KH,KF,KCH,itaeh
c      real kcsG,itaesG,iaesG,isesG
c      DIMENSION TAU(6,20),A1(6,20),B1(6,20),X(6,20)
c      DIMENSION THETA(6,20),N(6,20),OX(6,20)
c      OPEN(UNIT=20,FILE='SIM.DAT',ACCESS='SEQUOUT')

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C      OPEN( FILE='SVDINT.DAT',UNIT=22,ACCESS='APPEND' )
      DT=1.0/60.0
      alpha=0.006
      cost=0.0
      conac=0.0
C
C      HAT CONTROLLER INITIALIZATION
C      KCh U =1520.0
C      KCh = 0.5*KCh U
C      KCh=660.0
      hset=9.960553288
C
C      HAT INITIALIZATION
      OHHAT=0.0
      OFEED=0.0
C
C      filter initialization
C      numfil=8
      numfil=20
      tauf=float(numfil)*dt
      afil=-exp(-dt/tauf)
      bfil=1.0+afil
      sgfil=1.335693172
C
C      specific gravity controller initialization
      SGSET=1.335693172
C      kcsq=-3000.0
      kcsq=-500.0
C      tisc=0.7
      tisc=1.5
      sumsq=9.960553288
      itaesq=0.0
      iaesq=0.0
      isesq=0.0
C
C      Z-TRANSFORM PARAMETERS FOR MODEL
C
C      HHAT/F1
      KH=1.1909E-3
      TAUH=0.0134
C
C      F/F1
      KF=1.0
      TAU=0.0134
C
C      PE/FS (PART 1)
      K(1,1)=3.6965E-4
      TAU(1,1)=0.051493246
C
C      PE/FS (PART 2)
      K(1,2)=-3.8053E-5
      TAU(1,2)=8.533333333333
      THETA(1,2)=0.733333333333
C
C      PE/F (PART 1)
      K(1,3)=1.8027E-5
      TAU(1,3)=0.006
C
C      PE/F (PART 2)
      K(1,4)=-8.1276E-5

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C      TAU(1,4)=0.06
C
C      PE/F      (PART 3)
C      K(1,5)=4.3947E-5
C      TAU(1,5)=13.27
C      THETA(1,5)=0.6
C
C      PE/PC
C      K(1,6)=0.99980
C
C      PE/TF      (PART 1)
C      K(1,7)=6.6555E-3
C      TAU(1,7)=0.06
C
C      PE/TF      (PART 2)
C      K(1,8)=-7.6052E-4
C      TAU(1,8)=11.26666667
C      THETA(1,8)=0.6
C
C      PE/XFA      (PART 1)
C      K(1,9)=16.457
C
C      PE/XFA      (PART 2)
C      K(1,10)=-22.993
C      TAU(1,10)=1.2
C
C      PE/XFA      (PART 3)
C      K(1,11)=0.41820
C      TAU(1,11)=5.1
C      THETA(1,11)=11.66666667
C
C      PE/XFS      (PART 1)
C      K(1,12)=2.1396E-2
C
C      PE/XFS      (PART 2)
C      K(1,13)=-3.4532E-2
C      TAU(1,13)=6.46666667
C
C      SG/F
C      K(2,1)=-1.2187E-4
C      TAU(2,1)=12.75
C
C      SG/FS
C      K(2,2)=1.2615E-4
C      TAU(2,2)=8.22
C
C      SG/PC
C      K(2,3)=-2.6955E-4
C
C      SG/TF
C      K(2,4)=2.9067E-3
C      TAU(2,4)=11.3
C
C      SG/XFA      (PART 1)
C      K(2,5)=35.892
C      TAU(2,5)=1.0
C
C      SG/XFA      (PART 2)
C      K(2,6)=-1.7220
C      TAU(2,6)=13.0
C      THETA(2,6)=9.46666667

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C
C   SG/XFS
   K(2,7)=0.091326
   TAU(2,7)=5.63
C
C   T/F
   K(3,1)=-5.0820E-3
   TAU(3,1)=13.0
C
C   T/FS
   K(3,2)=4.7915E-3
   TAU(3,2)=8.0
C
C   T/PC
   K(3,3)=0.12530
C
C   T/TF
   K(3,4)=0.11875
   TAU(3,4)=11.23
C
C   T/XFA (PART 1)
   K(3,5)=3771.8
   TAU(3,5)=2.733333333
C
C   T/XFA (PART 2)
   K(3,6)=-36.450
   TAU(3,6)=5.5
   THETA(3,6)=12.533333333
C
C   T/XFS
   K(3,7)=8.1782
   TAU(3,7)=6.0
C
C   B/F (PART 1)
   K(4,1)=1.4788
C
C   B/F (PART 2)
   K(4,2)=-0.43114
   TAU(4,2)=13.26
C
C   B/FS (PART 1)
   K(4,3)=-1.8898
   TAU(4,3)=0.05
C
C   B/FS (PART 2)
   K(4,4)=0.65248
   TAU(4,4)=8.4666667
   THETA(4,4)=0.733333333
C
C   B/PC (PART 1)
   K(4,5)=111.12
C
C   B/PC (PART 2)
   K(4,6)=-110.42
   TAU(4,6)=0.1
C
C   B/TF (PART 1)
   K(4,7)=-32.664
   TAU(4,7)=0.07
C
C   B/TF (PART 2)

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```

      K(4,8)=11.592
      TAU(4,8)=11.26666667
      THETA(4,8)=0.6
C
C      B/XFA      (PART 1)
      K(4,9)=-4.6816E5
      TAU(4,9)=0.035
C
C      B/XFA      (PART 2)
      K(4,10)=4.9569E5
      TAU(4,10)=1.2
      THETA(4,10)=0.33333333
C
C      B/XFA      (PART 3)
      K(4,11)=-5401.3
      TAU(4,11)=6.0
      THETA(4,11)=13.066666667
C
C      B/XFS      (PART 1)
      K(4,12)=-608.46
      TAU(4,12)=0.06
C
C      B/XFS      (PART 2)
      K(4,13)=656.43
      TAU(4,13)=4.0
      THETA(4,13)=0.46666667
C
C      V/F        (PART 1)
      K(5,1)=0.041237
C
C      V/F        (PART 2)
      K(5,2)=-0.18501
      TAU(5,2)=0.1
C
C      V/F        (PART 3)
      K(5,3)=0.099686
      TAU(5,3)=12.66
      THETA(5,3)=0.6
C
C      V/FS       (PART 1)
      K(5,4)=1.3832
      TAU(5,4)=0.1
C
C      V/FS       (PART 2)
      K(5,5)=-0.14639
      TAU(5,5)=8.5333333
      THETA(5,5)=0.7333333
C
C      V/PC       (PART 1)
      K(5,6)=-26.367
C
C      V/PC       (PART 2)
      K(5,7)=25.643
      TAU(5,7)=0.08
C
C      V/TF       (PART 1)
      K(5,8)=23.680
      TAU(5,8)=0.06
C
C      V/TF       (PART 2)
      K(5,9)=-2.6587

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      TAU(5,9)=21.26666667
      THETA(5,9)=0.6
C
C      V/XFA      (PART 1)
      K(5,10)=5.8997E4
      TAU(5,10)=0.035
C
C      V/XFA      (PART 2)
      K(5,11)=-8.2850E4
      TAU(5,11)=1.2
      THETA(5,11)=0.33333333
C
C      V/XFA      (PART 3)
      K(5,12)=1533.2
      TAU(5,12)=4.5
      THETA(5,12)=11.6
C
C      V/XFS      (PART 1)
      K(5,13)=77.654
      TAU(5,13)=0.06
C
C      V/XFS      (PART 2)
      K(5,14)=-125.35
      TAU(5,14)=4.0
      THETA(5,14)=0.46666667
C
C      H/F        (PART 1)
      K(6,1)=1.8832E-4
      TAU(6,1)=0.08
C
C      H/F        (PART 2)
      K(6,2)=-1.6191E-5
      TAU(6,2)=13.26
      THETA(6,2)=0.8
C
C      H/FS       (PART 1)
      K(6,3)=-3.1537E-4
      TAU(6,3)=0.086
C
C      H/FS       (PART 2)
      K(6,4)=3.7280E-5
      TAU(6,4)=8.5
      THETA(6,4)=0.8666666667
C
C      H/PC       (PART 1)
      K(6,5)=1.6404E-2
C
C      H/PC       (PART 2)
      K(6,6)=-1.6174E-2
      TAU(6,6)=0.15
C
C      H/TF       (PART 1)
      K(6,7)=-4.4761E-3
      TAU(6,7)=0.07
C
C      H/TF       (PART 2)
      K(6,8)=4.9699E-4
      TAU(6,8)=11.27
      THETA(6,8)=0.73333333
C
C      H/XFA      (PART 1)

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```

      K(6,9)=-50.216
      TAU(6,9)=0.03
C
C      H/XFA (PART 2)
      K(6,10)=39.418
      TAU(6,10)=1.5
      THETA(6,10)=0.333333333
C
C      H/XFS (PART 1)
      K(6,11)=-9.1994E-2
      TAU(6,11)=0.053
C
C      H/XFS (PART 2)
      K(6,12)=5.6490E-2
      TAU(6,12)=6.0
      THETA(6,12)=0.53333333
C
C      STEADY STATES FOR OUTPUT VARIABLES
      PESS=407.6002089
      SGSS=1.335693172
      TSS=224.3048734
      BSS=4274.031793
      VSS=11618.96638
      HSS=90.06348338
      FSS=15893.0
      HHATSS=9.960553288
      F1SS=FSS
      HSETSS=90.06348338
      FSSS=10000.0
C
C      STEADY STATES FOR INPUT VARIABLES
      F1=15893.0
      FS=10000.0
      PC=406.0
      TF=175.0
      XFA=0.005
      XFS=0.105
      TIME=0.0
C
C      INITIALIZE M'S
      DO 11 JJ=1,6
      DO 12 JK=1,6000
      M(JJ,JK)=0.0
12  CONTINUE
11  CONTINUE
C
C      BEGIN SIMULATION
C
C      WRITE HEADING FOR DATA
      WRITE(05,700)
C
C      CALCULATE CONSTANTS FOR Z-TRANSFORM EQUATIONS
      DO 10 L=1,6
      DO 20 M1=1,14
      X(L,M1)=0.0
      CALL JOE(TAU(L,M1),DT,K(L,M1),A1(L,M1),B1(L,M1),
1          THETA(L,M1),N(L,M1))
C      WRITE(05,900)L,M1,a1(I,M1),b1(I,M1),N(L,M1)
20  CONTINUE
10  CONTINUE
C

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C      CONSTANTS FOR Z-TRANSFORM HAT EQUATIONS
      A1F=-EXP(-DT/TAUF)
      B1F=KF*(1.0+A1F)
      A1H=-EXP(-DT/TAUH)
      B1H=KH*(1.0+A1H)

C
C      WRITE HEADING FOR DATA
C      WRITE(05,800)
C      WRITE(20,800)

C
C      WRITE STEADY STATE VALUES
C      WRITE(05,1000)TIME,PESS,SGSS,TSS,BSS,VSS,HSS,HHATSS,F1SS,FSS
C      1      ,HSETSS,sgss,sgss
C      WRITE(20,1000)TIME,PESS,SGSS,TSS,BSS,VSS,HSS,HHATSS,F1SS,FSS
C      1      ,HSETSS,sgss,sgss
C      I=1

C
C      BEGINNING OF LOOP
C      F1M=F1-F1SS
C      IF(TIME.GT.2.0)F=15098.35
C      IF(TIME.GT.2.0)FS=9500.0
C      IF(TIME.GT.2.0)PC=405.9
C      IF(TIME.GT.2.0)TF=195.0
C      IF(TIME.GT.2.0)XFA=0.01
C      IF(TIME.GT.2.0)XFS=0.2
C      IF(TIME.GT.2.0)PESET=410.0
C      IF(TIME.GT.2.0)HSET=95.0
C
C      HAT SIMULATION
      DELHH=B1H*F1M-A1H*OHAT
      IF(DELHH.LT.-HHATSS)DELHH=-HHATSS
      DELF=B1F*F1M-A1F*OFEEED
      IF(DELF.LT.-FSS)DELF=-FSS
      F=FSS+DELF
      HHAT=HHATSS+DELHH
      OFEEED=DELF
      OHAT=DELHH

C
C      CALCULATE DEVIATION VARIABLES
      M(1,1)=F-15893.0
      M(2,1)=FS-10000.0
      M(3,1)=PC-406.0
      M(4,1)=TF-175.0
      M(5,1)=XFA-0.005
      M(6,1)=XFS-0.105

C
C      EFFECT ON PE OF FS (PART 1)
      INDEX=I-1-N(1,1)
      IF(I-1-N(1,1).LE.0)INDEX=1
      OX(1,1)=X(1,1)
      X(1,1)=B1(1,1)*M(2,INDEX)-A1(1,1)*OX(1,1)

C
C      EFFECT ON PE OF FS (PART 2)
      INDEX=I-1-N(1,2)
      IF(INDEX.LE.0)INDEX=1
      OX(1,2)=X(1,2)
      X(1,2)=B1(1,2)*M(2,INDEX)-A1(1,2)*OX(1,2)

C
C      EFFECT ON PE OF F (PART 1)
      INDEX=I-1-N(1,3)
      IF(INDEX.LE.0)INDEX=1

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```

      OX(1,3)=X(1,3)
      X(1,3)=B1(1,3)*M(1,INDEX)-A1(1,3)*OX(1,3)
C
C      EFFECT ON PE OF F (PART 2)
      INDEX=I-1-N(1,4)
      IF(INDEX.LE.0) INDEX=1
      OX(1,4)=X(1,4)
      X(1,4)=B1(1,4)*M(1,INDEX)-A1(1,4)*OX(1,4)
C
C      EFFECT ON PE OF F (PART 3)
      INDEX=I-1-N(1,5)
      IF(INDEX.LE.0) INDEX=1
      OX(1,5)=X(1,5)
      X(1,5)=B1(1,5)*M(1,INDEX)-A1(1,5)*OX(1,5)
C
C      EFFECT ON PE OF PC
      INDEX=I-1-N(1,6)
      IF(INDEX.LE.0) INDEX=1
      OX(1,6)=X(1,6)
      X(1,6)=B1(1,6)*M(3,INDEX)-A1(1,6)*OX(1,6)
C
C      EFFECT ON PE OF TF (PART 1)
      INDEX=I-1-N(1,7)
      IF(INDEX.LE.0) INDEX=1
      OX(1,7)=X(1,7)
      X(1,7)=B1(1,7)*M(4,INDEX)-A1(1,7)*OX(1,7)
C
C      EFFECT ON PE OF TF (PART 2)
      INDEX=I-1-N(1,8)
      IF(INDEX.LE.0) INDEX=1
      OX(1,8)=X(1,8)
      X(1,8)=B1(1,8)*M(4,INDEX)-A1(1,8)*OX(1,8)
C
C      EFFECT ON PE OF XFA (PART 1)
      INDEX=I-1-N(1,9)
      IF(INDEX.LE.0) INDEX=1
      OX(1,9)=X(1,9)
      X(1,9)=B1(1,9)*M(5,INDEX)-A1(1,9)*OX(1,9)
C
C      EFFECT ON PE OF XFA (PART 2)
      INDEX=I-1-N(1,10)
      IF(INDEX.LE.0) INDEX=1
      OX(1,10)=X(1,10)
      X(1,10)=B1(1,10)*M(5,INDEX)-A1(1,10)*OX(1,10)
C
C      EFFECT ON PE OF XFA (PART 3)
      INDEX=I-1-N(1,11)
      IF(INDEX.LE.0) INDEX=1
      OX(1,11)=X(1,11)
      X(1,11)=B1(1,11)*M(5,INDEX)-A1(1,11)*OX(1,11)
C
C      EFFECT ON PE OF XFS (PART 1)
      INDEX=I-1-N(1,12)
      IF(INDEX.LE.0) INDEX=1
      OX(1,12)=X(1,12)
      X(1,12)=B1(1,12)*M(6,INDEX)-A1(1,12)*OX(1,12)
C
C      EFFECT ON PE OF XFS (PART 2)
      INDEX=I-1-N(1,13)
      IF(INDEX.LE.0) INDEX=1
      OX(1,13)=X(1,13)

```

```

      X(1,13)=B1(1,13)*M(6,INDEX)-A1(1,13)*OX(1,13)
C
C      EFFECT ON SG OF F
      INDEX=I-1-N(2,1)
      IF(INDEX.LE.0) INDEX=1
      OX(2,1)=X(2,1)
      X(2,1)=B1(2,1)*M(1,INDEX)-A1(2,1)*OX(2,1)
C
C      EFFECT ON SG OF FS
      INDEX=I-1-N(2,2)
      IF(INDEX.LE.0) INDEX=1
      OX(2,2)=X(2,2)
      X(2,2)=B1(2,2)*M(2,INDEX)-A1(2,2)*OX(2,2)
C
C      EFFECT ON SG OF PC
      INDEX=I-1-N(2,3)
      IF(INDEX.LE.0) INDEX=1
      OX(2,3)=X(2,3)
      X(2,3)=B1(2,3)*M(3,INDEX)-A1(2,3)*OX(2,3)
C
C      EFFECT ON SG OF TF
      INDEX=I-1-N(2,4)
      IF(INDEX.LE.0) INDEX=1
      OX(2,4)=X(2,4)
      X(2,4)=B1(2,4)*M(4,INDEX)-A1(2,4)*OX(2,4)
C
C      EFFECT ON SG OF XFA (PART 1)
      INDEX=I-1-N(2,5)
      IF(INDEX.LE.0) INDEX=1
      OX(2,5)=X(2,5)
      X(2,5)=B1(2,5)*M(5,INDEX)-A1(2,5)*OX(2,5)
C
C      EFFECT ON SG OF XFA (PART 2)
      INDEX=I-1-N(2,6)
      IF(INDEX.LE.0) INDEX=1
      OX(2,6)=X(2,6)
      X(2,6)=B1(2,6)*M(5,INDEX)-A1(2,6)*OX(2,6)
C
C      EFFECT ON SG OF XFS
      INDEX=I-1-N(2,7)
      IF(INDEX.LE.0) INDEX=1
      OX(2,7)=X(2,7)
      X(2,7)=B1(2,7)*M(6,INDEX)-A1(2,7)*OX(2,7)
C
C      EFFECT ON T OF F
      INDEX=I-1-N(3,1)
      IF(INDEX.LE.0) INDEX=1
      OX(3,1)=X(3,1)
      X(3,1)=B1(3,1)*M(1,INDEX)-A1(3,1)*OX(3,1)
C
C      EFFECT ON T OF FS
      INDEX=I-1-N(3,2)
      IF(INDEX.LE.0) INDEX=1
      OX(3,2)=X(3,2)
      X(3,2)=B1(3,2)*M(2,INDEX)-A1(3,2)*OX(3,2)
C
C      EFFECT ON T OF PC
      INDEX=I-1-N(3,3)
      IF(INDEX.LE.0) INDEX=1
      OX(3,3)=X(3,3)
      X(3,3)=B1(3,3)*M(3,INDEX)-A1(3,3)*OX(3,3)

```

```

C
C   EFFECT ON T OF TF
      INDEX=I-1-N(3,4)
      IF(INDEX.LE.0) INDEX=1
      OX(3,4)=X(3,4)
      X(3,4)=B1(3,4)*M(4,INDEX)-A1(3,4)*OX(3,4)
C
C   EFFECT ON T OF XFA (PART 1)
      INDEX=I-1-N(3,5)
      IF(INDEX.LE.0) INDEX=1
      OX(3,5)=X(3,5)
      X(3,5)=B1(3,5)*M(5,INDEX)-A1(3,5)*OX(3,5)
C
C   EFFECT ON T OF XFA (PART 2)
      INDEX=I-1-N(3,6)
      IF(INDEX.LE.0) INDEX=1
      OX(3,6)=X(3,6)
      X(3,6)=B1(3,6)*M(5,INDEX)-A1(3,6)*OX(3,6)
C
C   EFFECT ON T OF XFS
      INDEX=I-1-N(3,7)
      IF(INDEX.LE.0) INDEX=1
      OX(3,7)=X(3,7)
      X(3,7)=B1(3,7)*M(6,INDEX)-A1(3,7)*OX(3,7)
C
C   EFFECT ON B OF F (PART 1)
      INDEX=I-1-N(4,1)
      IF(I-1-N(4,1).LE.0) INDEX=1
      OX(4,1)=X(4,1)
      X(4,1)=B1(4,1)*M(1,INDEX)-A1(4,1)*OX(4,1)
C
C   EFFECT ON B OF F (PART 2)
      INDEX=I-1-N(4,2)
      IF(INDEX.LE.0) INDEX=1
      OX(4,2)=X(4,2)
      X(4,2)=B1(4,2)*M(1,INDEX)-A1(4,2)*OX(4,2)
C
C   EFFECT ON B OF FS (PART 1)
      INDEX=I-1-N(4,3)
      IF(INDEX.LE.0) INDEX=1
      OX(4,3)=X(4,3)
      X(4,3)=B1(4,3)*M(2,INDEX)-A1(4,3)*OX(4,3)
C
C   EFFECT ON B OF FS (PART 2)
      INDEX=I-1-N(4,4)
      IF(INDEX.LE.0) INDEX=1
      OX(4,4)=X(4,4)
      X(4,4)=B1(4,4)*M(2,INDEX)-A1(4,4)*OX(4,4)
C
C   EFFECT ON B OF PC (PART 1)
      INDEX=I-1-N(4,5)
      IF(INDEX.LE.0) INDEX=1
      OX(4,5)=X(4,5)
      X(4,5)=B1(4,5)*M(3,INDEX)-A1(4,5)*OX(4,5)
C
C   EFFECT ON B OF PC (PART 2)
      INDEX=I-1-N(4,6)
      IF(INDEX.LE.0) INDEX=1
      OX(4,6)=X(4,6)
      X(4,6)=B1(4,6)*M(3,INDEX)-A1(4,6)*OX(4,6)
C

```

```

C      EFFECT ON B OF TF (PART 1)
        INDEX=I-1-N(4,7)
        IF (INDEX.LE.0) INDEX=1
        OX(4,7)=X(4,7)
        X(4,7)=B1(4,7)*M(4,INDEX)-A1(4,7)*OX(4,7)
C
C      EFFECT ON B OF TF (PART 2)
        INDEX=I-1-N(4,8)
        IF (INDEX.LE.0) INDEX=1
        OX(4,8)=X(4,8)
        X(4,8)=B1(4,8)*M(4,INDEX)-A1(4,8)*OX(4,8)
C
C      EFFECT ON B OF XFA (PART 1)
        INDEX=I-1-N(4,9)
        IF (INDEX.LE.0) INDEX=1
        OX(4,9)=X(4,9)
        X(4,9)=B1(4,9)*M(5,INDEX)-A1(4,9)*OX(4,9)
C
C      EFFECT ON B OF XFA (PART 2)
        INDEX=I-1-N(4,10)
        IF (INDEX.LE.0) INDEX=1
        OX(4,10)=X(4,10)
        X(4,10)=B1(4,10)*M(5,INDEX)-A1(4,10)*OX(4,10)
C
C      EFFECT ON B OF XFA (PART 3)
        INDEX=I-1-N(4,11)
        IF (INDEX.LE.0) INDEX=1
        OX(4,11)=X(4,11)
        X(4,11)=B1(4,11)*M(5,INDEX)-A1(4,11)*OX(4,11)
C
C      EFFECT ON B OF XFS (PART 1)
        INDEX=I-1-N(4,12)
        IF (INDEX.LE.0) INDEX=1
        OX(4,12)=X(4,12)
        X(4,12)=B1(4,12)*M(6,INDEX)-A1(4,12)*OX(4,12)
C
C      EFFECT ON B OF XFS (PART 2)
        INDEX=I-1-N(4,13)
        IF (INDEX.LE.0) INDEX=1
        OX(4,13)=X(4,13)
        X(4,13)=B1(4,13)*M(6,INDEX)-A1(4,13)*OX(4,13)
C
C      EFFECT ON V OF F (PART 1)
        INDEX=I-1-N(5,1)
        IF (I-1-N(5,1).LE.0) INDEX=1
        OX(5,1)=X(5,1)
        X(5,1)=B1(5,1)*M(1,INDEX)-A1(5,1)*OX(5,1)
C
C      EFFECT ON V OF F (PART 2)
        INDEX=I-1-N(5,2)
        IF (INDEX.LE.0) INDEX=1
        OX(5,2)=X(5,2)
        X(5,2)=B1(5,2)*M(1,INDEX)-A1(5,2)*OX(5,2)
C
C      EFFECT ON V OF F (PART 3)
        INDEX=I-1-N(5,3)
        IF (INDEX.LE.0) INDEX=1
        OX(5,3)=X(5,3)
        X(5,3)=B1(5,3)*M(1,INDEX)-A1(5,3)*OX(5,3)
C
C      EFFECT ON V OF FS (PART 1)

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```

INDEX=I-1-N(5,4)
IF (INDEX.LE.0) INDEX=1
OX(5,4)=X(5,4)
X(5,4)=B1(5,4)*M(2,INDEX)-A1(5,4)*OX(5,4)
C
C EFFECT ON V OF FS (PART 2)
INDEX=I-1-N(5,5)
IF (INDEX.LE.0) INDEX=1
OX(5,5)=X(5,5)
X(5,5)=B1(5,5)*M(2,INDEX)-A1(5,5)*OX(5,5)
C
C EFFECT ON V OF PC (PART 1)
INDEX=I-1-N(5,6)
IF (INDEX.LE.0) INDEX=1
OX(5,6)=X(5,6)
X(5,6)=B1(5,6)*M(3,INDEX)-A1(5,6)*OX(5,6)
C
C EFFECT ON V OF PC (PART 2)
INDEX=I-1-N(5,7)
IF (INDEX.LE.0) INDEX=1
OX(5,7)=X(5,7)
X(5,7)=B1(5,7)*M(3,INDEX)-A1(5,7)*OX(5,7)
C
C EFFECT ON V OF TF (PART 1)
INDEX=I-1-N(5,8)
IF (INDEX.LE.0) INDEX=1
OX(5,8)=X(5,8)
X(5,8)=B1(5,8)*M(4,INDEX)-A1(5,8)*OX(5,8)
C
C EFFECT ON V OF TF (PART 2)
INDEX=I-1-N(5,9)
IF (INDEX.LE.0) INDEX=1
OX(5,9)=X(5,9)
X(5,9)=B1(5,9)*M(4,INDEX)-A1(5,9)*OX(5,9)
C
C EFFECT ON V OF XFA (PART 1)
INDEX=I-1-N(5,10)
IF (INDEX.LE.0) INDEX=1
OX(5,10)=X(5,10)
X(5,10)=B1(5,10)*M(5,INDEX)-A1(5,10)*OX(5,10)
C
C EFFECT ON V OF XFA (PART 2)
INDEX=I-1-N(5,11)
IF (INDEX.LE.0) INDEX=1
OX(5,11)=X(5,11)
X(5,11)=B1(5,11)*M(5,INDEX)-A1(5,11)*OX(5,11)
C
C EFFECT ON V OF XFA (PART 3)
INDEX=I-1-N(5,12)
IF (INDEX.LE.0) INDEX=1
OX(5,12)=X(5,12)
X(5,12)=B1(5,12)*M(5,INDEX)-A1(5,12)*OX(5,12)
C
C EFFECT ON V OF XFS (PART 1)
INDEX=I-1-N(5,13)
IF (INDEX.LE.0) INDEX=1
OX(5,13)=X(5,13)
X(5,13)=B1(5,13)*M(6,INDEX)-A1(5,13)*OX(5,13)
C
C EFFECT ON V OF XFS (PART 2)
INDEX=I-1-N(5,14)

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      IF (INDEX.LE.0) INDEX=1
      OX(5,14)=X(5,14)
      X(5,14)=B1(5,14)*M(6,INDEX)-A1(5,14)*OX(5,14)
C
C   EFFECT ON H OF F (PART 1)
      INDEX=1-1-N(6,1)
      IF (1-1-N(6,1).LE.0) INDEX=1
      OX(6,1)=X(6,1)
      X(6,1)=B1(6,1)*M(1,INDEX)-A1(6,1)*OX(6,1)
C
C   EFFECT ON H OF F (PART 2)
      INDEX=1-1-N(6,2)
      IF (INDEX.LE.0) INDEX=1
      OX(6,2)=X(6,2)
      X(6,2)=B1(6,2)*M(1,INDEX)-A1(6,2)*OX(6,2)
C
C   EFFECT ON H OF FS (PART 1)
      INDEX=1-1-N(6,3)
      IF (INDEX.LE.0) INDEX=1
      OX(6,3)=X(6,3)
      X(6,3)=B1(6,3)*M(2,INDEX)-A1(6,3)*OX(6,3)
C
C   EFFECT ON H OF FS (PART 2)
      INDEX=1-1-N(6,4)
      IF (INDEX.LE.0) INDEX=1
      OX(6,4)=X(6,4)
      X(6,4)=B1(6,4)*M(2,INDEX)-A1(6,4)*OX(6,4)
C
C   EFFECT ON H OF PC (PART 1)
      INDEX=1-1-N(6,5)
      IF (INDEX.LE.0) INDEX=1
      OX(6,5)=X(6,5)
      X(6,5)=B1(6,5)*M(3,INDEX)-A1(6,5)*OX(6,5)
C
C   EFFECT ON H OF PC (PART 2)
      INDEX=1-1-N(6,6)
      IF (INDEX.LE.0) INDEX=1
      OX(6,6)=X(6,6)
      X(6,6)=B1(6,6)*M(3,INDEX)-A1(6,6)*OX(6,6)
C
C   EFFECT ON H OF TF (PART 1)
      INDEX=1-1-N(6,7)
      IF (INDEX.LE.0) INDEX=1
      OX(6,7)=X(6,7)
      X(6,7)=B1(6,7)*M(4,INDEX)-A1(6,7)*OX(6,7)
C
C   EFFECT ON H OF TF (PART 2)
      INDEX=1-1-N(6,8)
      IF (INDEX.LE.0) INDEX=1
      OX(6,8)=X(6,8)
      X(6,8)=B1(6,8)*M(4,INDEX)-A1(6,8)*OX(6,8)
C
C   EFFECT ON H OF XFA (PART 1)
      INDEX=1-1-N(6,9)
      IF (INDEX.LE.0) INDEX=1
      OX(6,9)=X(6,9)
      X(6,9)=B1(6,9)*M(5,INDEX)-A1(6,9)*OX(6,9)
C
C   EFFECT ON H OF XFA (PART 2)
      INDEX=1-1-N(6,10)
      IF (INDEX.LE.0) INDEX=1

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      OX(6,10)=X(6,10)
      X(6,10)=B1(6,10)*M(5,INDEX)-A1(6,10)*OX(6,10)
C
C   EFFECT ON H OF XFS (PART 1)
      INDEX=I-1-N(6,11)
      IF(INDEX.LE.0)INDEX=1
      OX(6,11)=X(6,11)
      X(6,11)=B1(6,11)*M(6,INDEX)-A1(6,11)*OX(6,11)
C
C   EFFECT ON H OF XFS (PART 2)
      INDEX=I-1-N(6,12)
      IF(INDEX.LE.0)INDEX=1
      OX(6,12)=X(6,12)
      X(6,12)=B1(6,12)*M(6,INDEX)-A1(6,12)*OX(6,12)
C
C   DEVIATIONS
      DELPE=0.0
      DELSG=0.0
      DELT=0.0
      DELB=0.0
      DELV=0.0
      DELH=0.0
      DO 110 II=1,14
      DELPE=DELPE+X(1,II)
      DELSG=DELSG+X(2,II)
      DELT=DELT+X(3,II)
      DELB=DELB+X(4,II)
      DELV=DELV+X(5,II)
      DELH=DELH+X(6,II)
110  CONTINUE
      PE=PESS+DELPE
      SG=SGSS+DELSG
      T=TSS+DELT
      B=BSS+DELB
      IF(B.LT.0.0)B=0.0
      V=VSS+DELV
      IF(V.LT.0.0)V=0.0
      H=HSS+DELH
      IF(H.LT.89.75)H=89.75
      IF(PE.LT.406.0)PE=406.0
C
C   HAT CONTROLLER
      ERRORH=hset-HHAT
      DF1=KCH*ERRORH
      OF1=F1
      F1=F1SS+DF1
      IF(F1.GT.20000.0)F1=20000.0
      IF(F1.LT.0.0)F1=0.0
      itaeH=itaeH+abs(ERRORH)
C
C   noise added to specific gravity
      sgnoiz=0.006*(rans(1)-0.5)
      sgclen=sg
      sg=sg+sgnoiz
C
C   filter to decrease noise on specific gravity
      osgfil=sgfil
      osg=sg
      sgfil=-afil*osgfil+bfil*osg

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c
c      specific gravity controller
      errorsg=sgset-sgfil
      ernoiz=sgset-sg+sgnoiz
      error=sgset-sgclen
      sumsg=sumsg+errorsg*dt*kcsG/tisg
      ohtset=hset
      hset=kcsG*errorsg+sumsg
      itaesg=itaesg+abs(errorsg)*time
      iaesg=iaesg+abs(errorsg)
      isesg=isesg+(errorsG**2)
      conac=conac+abs(ohtset-hset)

c
c      MATERIAL BALANCE
      FINT=FINT+(F*DT)
      FSINT=FSINT+(FS*DT)

c
      I=I+1
      ICOUNT=ICOUNT+1
      TIME=TIME+DT
c      IF(ICOUNT.EQ.60)WRITE(05,1000)TIME,PE,SG,T,B,V,H,HHAT,F1,F,HSET
c      1      ,sgfil,sgclen
      IF(icount.EQ.1)WRITE(20,1000)TIME,PE,SG,T,B,V,H,HHAT,F1,F,HSET
      1      ,sgfil,sgclen
      IF(ICOUNT.EQ.1)ICOUNT=0
      IF(TIME.GT.15.0)GOTO 33
      GOTO 1
33      cost=itAesg+alpha*conac
      write(5,4444)fint,fsint
4444      format(' ',fint=' ',g15.8,5x,'fsint=' ',g15.8)
      write(5,*)cost
      stop
700      FORMAT(1X,'OUT',3X,'IN',15X,'A1',23X,
      1      'B1',12X,'NDEAD',//)
800      FORMAT(///,12X,'TIME',21X,'PE',23X,'SG',22X,'T',23X,
      1      'B',/,13X,'V',23X,'H',22X,'HHAT',22X,'F1',
      2      22X,'F',31X,'HSET',22X,'FS',22X,'PESET',//)
900      FORMAT(13,3X,13,3X,2G24.10,3X,13)
1000     FORMAT(5G24.10,/,5G24.10,/,3G24.10,/)
2222     FORMAT(' itaesG = ',G15.8,' FOR KCSG = ',G15.8)
2223     format(' itaeT = ',G15.8,' FOR KCT = ',G15.8)
2224     FORMAT(' USING ',G15.8,' LBS. OF STEAM FOR ',G15.8,
      1      ' LBS OF FEED ')
2225     FORMAT(' SGSET = ',G15.8,5X,' TSET = ',G15.8)
2226     FORMAT(' FINAL SG = ',G15.8,' FINAL T = ',G15.8)
2227     FORMAT(' RSGSET = ',G15.8,' FINAL RSG = ',G15.8)
2228     FORMAT(' RTSET = ',G15.8,' FINAL RT = ',G15.8,/)
      END
      SUBROUTINE JOE(TAU,DT,K,A1,B1,THETA,N)
      REAL K
          A1=0.0
          IF(TAU.NE.0.0)A1=-EXP(-DT/TAU)
          B1=K*(1.0+A1)
          N=IFIX(THETA/DT)
          RETURN
      END

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VITA

Lawrence Paul MacIntyre was born in Oak Ridge, Tennessee on January 7, 1959. He graduated from Oak Ridge High School in June 1976. In September 1976 he began classes at The University of Tennessee in Knoxville. He entered the co-operative program in June 1977, working first for C. F. Industries in Harrison, Tennessee, and then for E. I. DuPont at the Savannah River Plant in Aiken, South Carolina. He graduated with a Bachelor of Science degree in Chemical Engineering in December 1981 and entered graduate school at The University of Tennessee in January 1982. He was married to the former Patricia Lee in May 1983 and they now reside in North Brunswick, New Jersey. He graduated with a Master of Science degree in Chemical Engineering in March 1983.

The author is a member of Phi Eta Sigma, Alpha Chi Sigma, Tau Beta Pi, and the American Institute of Chemical Engineers. He was awarded the Albert Cooper Memorial Scholarship by Alpha Chi Sigma as a senior.