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I am submitting herewith a thesis written by Robert Joseph Bryant entitled "Computer Simulation of Interpolating Techniques for Generating a Realtime EEG Potential Contour Display." I recommend that it be accepted in partial fulfillment of the requirements for the degree of Master of Science, with a major in Computer Science.

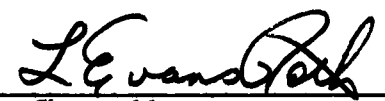

J. M. Moshell, Major Professor

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COMPUTER SIMULATION OF INTERPOLATING TECHNIQUES FOR GENERATING
A REALTIME EEG POTENTIAL CONTOUR DISPLAY

A Thesis
Presented for the
Master of Science
Degree
The University of Tennessee, Knoxville

Robert Joseph Bryant

March 1978

1356493

ACKNOWLEDGMENTS

I would like to express my appreciation to Dr. J. M. Moshell for his encouragement and direction in the preparation of this paper. I would also like to thank Mr. Bill Baird and West High School for the use of their photographic facilities.

Thank you also goes out to my family and all my friends for providing the much needed moral support.

ABSTRACT

This study is concerned with evaluating the feasibility of using hardware adaptable interpolation techniques for approximating the EEG potential field extending over the human scalp. The criteria require that the technique be realizable by analog components and that the approximations be as reliable as that achieved from Bilinear interpolation. A successful interpolation routine would allow the construction of an analog device capable of receiving voltage signals from electrodes and producing a realtime gray-scale contour map of the EEG potential field on a video display screen. A device of this type would be particularly useful in the area of biofeedback research.

A computer program was written to simulate the activity of several interpolation techniques. Voltage data presented to the program consisted of specific test pattern data and real EEG data records. A TV monitor was used to display the resulting contour maps which were photographed to permit direct image comparisons among the several techniques.

The results show that the Inverse-square radius weighting technique produces images similar to that of the Bilinear, but it contains some undesirable features. The use of a smearing technique substantially reduced these features. The success of the combined Inverse-square and smearing technique and their adaptability to analog components suggest their use in constructing a realtime EEG potential contour display device.

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CHAPTER I

INTRODUCTION

Research in the area of electroencephalography is aimed at obtaining a better understanding of how the brain functions. Standard clinical EEG measurements are made using electrodes placed directly on the scalp surface. These measurements provide two types of information about the electrical fields generated by the human brain, frequency of the voltage variations and differences in the voltage variations between two points on the scalp surface (Daube and Lake, 1972). The data collected can then be subjected to a variety of analysis techniques.

Data collected in this manner poses the problem of data redundancy. To illustrate this, consider the amount of data collected during a standard clinical EEG recording session. Using six to eight channels at 3600 cycles per second over a span of 20 minutes can result in excess of one-half billion numbers. However, the activity measured may, quite often, be explained in just a few sentences (Walter and Shipton, 1951).

An approach to the problem of redundant data was demonstrated as early as 1947 at the First International EEG Congress. The device is known as the Toposcope. It was constructed using a single cathode-ray tube connected to electrodes placed on the subject's scalp. The electron beam was modulated at different positions on the screen to reflect the relative intensity of the voltage level recorded by correspondingly located electrodes. The Toposcope was a simple device and quite limited in resolution, but it did provide a pleasant

demonstration of topographic detail. Unfortunately, the limitation of then current technology prevented significant improvements in the display technique (Walter and Shipton, 1951).

This technique did, however, spark sufficient interest to encourage others to pursue research in the area of spatio-temporal display of EEG data. This is indicated by work in the early 1950's by Cohen, Marko and Petsche, and W. G. Walter and Shipton and in the 1960's by Shipton, Remond and D. O. Walter (Shaw, 1970). Until recently, many of the efforts were centered around devices similar to the original toposcope or generation of potential contour maps that were either hand-drawn or produced on computer printout forms.

More recently, improvements have been made possible due to technological advances, notably the EEG Computerized Display by T. Estrin and R. Uzgalis, 1969. The technique utilized improvements in analog-digital conversion, high-speed computers and graphic display systems. The recorded electrical activity was stored on magnetic tape. It was later processed on the computer to generate a separate potential contour map on a cathode-ray tube for each time instant recorded. The cathode-ray tube was then photographed under computer control. The film produced could then be viewed later, primarily for study of alpha wave bursts (Estrin and Uzgalis, 1969).

Another research effort reported by Daube and Lake in 1972 resulted in a technique which produced a computer generated, three dimensional display of potential fields for single time instants. Two separate electrode arrangements were involved, from which data was recorded and

stored on magnetic tape. The three dimensional display requires selection of the time instant and one of several analytical options. It also allows orientation and size alteration along with suppression or enhancement of certain characteristics.

These two efforts, and others not mentioned, indicate the vast improvements achieved since the introduction of the first toposcope. However, none have been able to display the potential field distribution information in real time, such as would be required for standard clinical electroencephalography.

This presentation investigates the feasibility of constructing a special purpose hardware system to display, in real time, a two dimensional contour map of the potential fields on the scalp surface on a video display screen. This means that a visual evaluation of the potential field over the scalp would be possible while the EEG data is recorded.

This type of display would aid the electroencephalographer in increasing his awareness of the oscillating potential continuum that extends across the scalp. Visualizing such an image has been a problem for electroencephalographers, since most tend to think in terms of one dimensional traces, displaying potential difference as amplitude against time as abscissa (Petsche, 1970). An area in which this would be of special interest is biofeedback research.

Harris, 1967, placed sixteen electrodes along a great circle over the scalp surface to determine the minimum number of electrodes required to approximate the voltage curve along these sixteen electrodes. He

selected n successive electrodes and estimated the curve by an $n - 1$ degree polynomial. The criteria for a successful approximation require that all the minimal and maximal points be detected. His results indicate that an average of five and a maximum of nine electrodes are required. From this, it is reasonable to assume that the 5×5 electrode grid used in the research will, on the average, reliably sample the electrical activity.

The Bilinear interpolation scheme, explained in Chapter III, is the basic standard against which the interpolation techniques present here will be compared. Adoption of this technique is supported by its wide use for interpolating between random points on a surface (McLain, 1976) and Remond's discussion of its utility in 1968.

CHAPTER II

THE SIMULATION APPROACH

The EEG potential display system under investigation, as shown in Figure 1, is composed of three main components: EEG data collection, hardware interpolation, and video display. The hardware interpolation device is the portion of consequence, as the remaining parts are currently available.

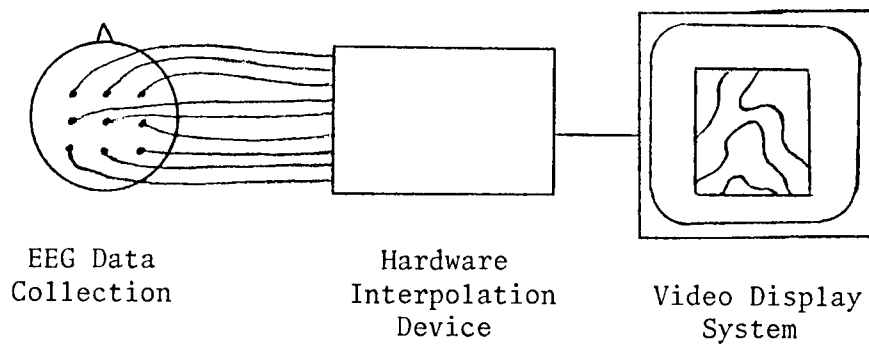


Figure 1. Schematic of the EEG display system.

The interpolation device calculates an approximation of the potential fields existing between the electrode positions which are then used as input to the video display system. Use of a general purpose mini-computer to generate the data for display on a TV screen would not be possible in a real time environment. To illustrate this, let us consider the number of operations that would be required per second. A standard TV screen is approximately a 500 by 500 picture element array, or has 2.5×10^5 positions, and it requires 30 new images per second.

Therefore, the computer must calculate 7.5×10^6 picture elements per second. Now, using one of the most simple interpolation routines, in terms of computations per picture element, there are five computations required per picture element. This totals to approximately 37.5 million operations per second without regard to any logical operations, such as determining which electrodes are to be used in the current computation. Even with current technology, the computation rate required to perform this many operations per second is beyond the capability of general purpose mini-computers. Therefore, a special purpose hardware device would be required to process the input signals from the electrodes and to produce the video brightness signals for the display system.

However, a special purpose device could not be easily modified should the interpolation algorithm implemented be found to be unsatisfactory. Therefore, a computer program has been written to simulate the activity of this hardware component.

The software simulation program has been used to evaluate several interpolation techniques. After initial testing of each routine, modifications were made to compensate for characteristics found to be undesirable and to enhance those that were desirable. Changes at this stage of the investigation are much easier and more quickly completed than after the device has been built.

This software package consists of several interpolation routines to be evaluated. Each routine, in turn, has input parameters that adjust its operation such that there is a large number of possible interpolation routines. Evaluation of these routines included the use of

artificial test data, whose potential contour maps were known, and the use of actual EEG recordings. To complete this simulation and to provide a visual evaluation of the success of the interpolation routines, a video display system has been provided.

The evaluation of the success of each interpolation routine is based upon intuitive knowledge of what the image should look like. This approach has been taken due to the lack of knowledge concerning the actual potential fields (Lehmann, 1971). A contributing factor to this lack of knowledge is the nonhomogeneous nature of the human head, that is, the convoluted brain and the inconsistent thickness of the skull. This is complicated by the lack of certainty concerning the number and location of EEG generators (Lehmann, 1971). However, since the scalp is also known to be an averager of the potentials generated by the cortex (Daube and Lake, 1972), it is believed that the continual display of the electrical patterns that are observed will provide an insight to the actual potential activity.

CHAPTER III

DISCUSSION OF INTERPOLATION PROCEDURES

Bilinear Interpolation

The concern of interpolation algorithms is the computation of "close" approximations to continuous functions using points for which the actual values are known. In this study, the value of the points sampled are voltage signals which are collected using physiological electrodes placed on the surface of the subject's scalp in regular array patterns. Figure 2 represents such an arrangement using four electrodes labelled A, B, C and D, with corresponding instantaneous voltages V_a , V_b , V_c and V_d .

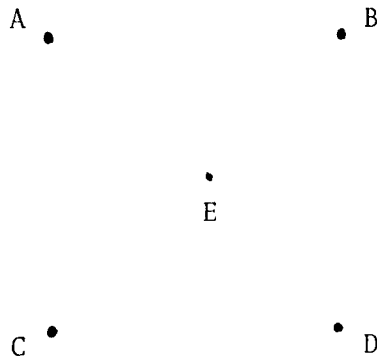


Figure 2. Sample arrangement of four electrodes.

A fundamental technique for approximating the voltage of point E that is equally distant from all four electrodes is

$$V_e = \frac{V_a + V_b + V_c + V_d}{4}$$

which is the average. However, as point E moves closer to some electrodes than others, the use of weighting factors is required to reflect the degree of contribution of each electrode to V_e . The Bilinear interpolation technique accomplishes this weighting function by computing point values relative to the distance between each point and the surrounding electrodes.

Initially, two Bilinear routines were considered, termed "X-first" and "Y-first." The difference between these two routines lie with the order in which the interpolation is performed and not in the general algorithm. An evaluation of these two routines shows them to be equivalent; they can be reduced to a common set of equations which were used in the research. Further details pertaining to the "X-first" and "Y-first" routines are found in Appendix A.

The Bilinear technique incorporated in the software program consists of two cases. The first case (see Figure 3) involves points which occur on line segments between two electrodes. Points P and Q lie on vertical line segments, whereas points R and S lie on horizontal line segments. The corresponding voltages are computed by

$$V_p = V_a + (V_c - V_a) (y_1/y_2)$$

$$V_q = V_b + (V_d - V_b) (y_1'/y_2)$$

$$V_r = V_a + (V_b - V_a) (x_1/x_2)$$

$$V_s = V_c + (V_c - V_d) (x_1'/x_2)$$

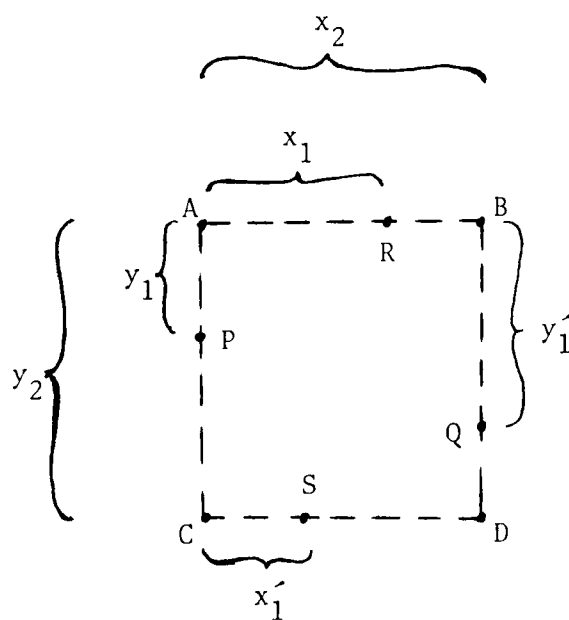


Figure 3. Location of points for case 1 of Bilinear interpolation.

The second case (see Figure 4) involves points, such as T, that lie on the interior of the region described by the four electrodes and whose voltages are computed by

$$\begin{aligned}
 V_t = & V_a \cdot (1 - x_1/x_2 - y_1/y_2 + (x_1/x_2 \cdot y_1/y_2)) + \\
 & V_b \cdot (y_1/y_2 - (x_1/x_2 \cdot y_1/y_2)) + \\
 & V_c \cdot (x_1/x_2 - x_1/x_2 \cdot y_1/y_2)) + \\
 & V_d \cdot (x_1/x_2 \cdot y_1/y_2)
 \end{aligned}$$

As indicated, the Bilinear technique considers only four electrodes at any one time, but the arrangement typically involves more than four. Interpolation of an arrangement with more than four electrodes is handled by segmenting it into several regions. Each region is the area bounded by four electrodes joined by straight line segments. For example, an arrangement of 25 electrodes would be segmented into 16 interpolation regions (see Figure 5). The effect of this is twofold: interpolation over the entire electrode net is continuous, but its first derivative is not (McLain, 1974); and noise generated by region switching, in a hardware system, would interfere with the brightness data generating the image.

Processing regions separately results in an image with "creases" (discontinuities of the first derivative) along region boundaries. This is most apparent when adjacent electrodes have readings that vary significantly. Hardware implementation of the Bilinear method would require that electronic circuits be provided to perform the region

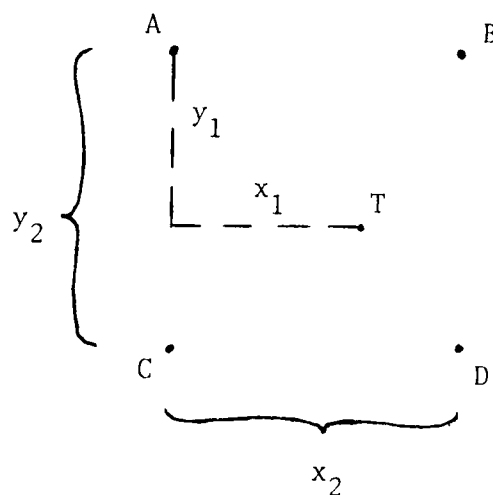


Figure 4. Location of points for case 2 of Bilinear interpolation.

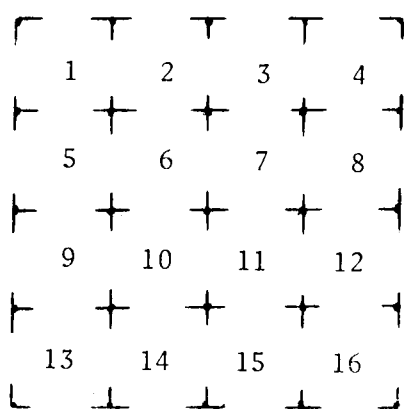


Figure 5. Identification of regions for Bilinear interpolation.

switching function. This switching event occurs with the transition from region to region and is accompanied by a certain amount of noise, which when injected into the video brightness signal would form a straight line or checkerboard pattern on the TV screen and would obscure the image. If the noise generated could be made regular then there would be possibilities for using it as a coordinate system to locate the electrode sites. However, as it is, the result of electronic noise, its shape and appearance on the screen, would be difficult to control. This switching problem is the major obstacle to hardware construction of Bilinear interpolation.

Continuous Interpolation

A desirable alternative to the Bilinear method would be the use of a continuous interpolation function that utilizes every electrode in the interpolation of each point. This would eliminate the concern over which region the current point is located and the associated discontinuities along region boundaries.

The question now is what weighting factor can be applied which will best emphasize the contribution of electrodes located close to the current point and minimize the contribution of more distant electrodes. For the moment, let w_i represent the weighting factor. The interpolated voltage, V_e , of some point E would then be calculated by

$$V_e = \sum_{i=1}^n w_i v_i$$

where n is the number of electrodes.

Two promising candidates, as weighting factors, are the Inverse radius and the Inverse-square radius. Both will be discussed in further detail in Chapter IV.

Physiological Justification

One might ask: Do we not take a risk in arbitrarily "guessing" what activity is actually occurring between the electrodes? The answer is obviously yes, but then so does the Bilinear method, which will be shown in Chapter V, to contain characteristic features that do not correspond to actual activity. Let us consider for a moment two basic questions: What type of information are we really able to produce and how can it be applied?

As discussed in Chapter II, there are several physiological problems associated with the reconstruction of bioelectrical fields that are far from being solved. Keeping these problems in mind, the best that can be realistically hoped for is a surface mapping of potential fields that provide a basic indication of where the predominant activity occurs.

An area in which this type of potential field display is of immediate interest is biofeedback research. Here, the exact numerical magnitude of the underlying phenomenon is only of secondary interest. What the biofeedback trainer desires is that the images presented exhibit a range of distinguishable patterns corresponding to different electrical states of the brain. When the trainer detects a desirable state, by traditional methods, the subject will be able to recognize that state, as well as similar states. The recognition is not the

result of a highly accurate model of underlying brain activity, but is the result that similar brain activities will yield similar visual images. This is the key to the utility of such a display device for biofeedback training.

CHAPTER IV

NONLINEAR INTERPOLATION

Inverse and Inverse-Square Radius

Consider the arrangement of electrodes as being represented by an $N \times M$ array, where N and M may or may not be equal. Let $K = N \times M$ be the total number of electrodes and let the position of the i^{th} electrode in some Cartesian coordinate system be represented by $e_i = (x_i, y_i)$. Also, let $p = (p_x, p_y)$ represent any point within the convex polygon enclosing the K electrode sites. The radius, R_i , of p from any electrode e_i , is then defined as

$$R_i = \sqrt{(x_i - p_x)^2 + (y_i - p_y)^2}$$

For any weighting function of the radius, $W(R_i)$ and some assignment of voltage values, v_i , to e_i , the voltage at p is defined to be

$$V = \sum_{i=1}^K W(R_i) \cdot v_i$$

The value of V is then merely the sum of each electrode weighted in accordance to its distance from p .

The two main weighting functions used in this research are the Inverse radius and the Inverse-square radius, where $W(R_i) = 1/R_i$ and $W(R_i) = 1/R_i^2$, respectively. Using the Inverse radius as an example, the voltage at p would then be

$$V = \sum_{i=1}^K \left(\frac{1}{R_i} \right) \cdot v_i$$

Normalization

As point p approaches the location of any electrode, the radius decreases, causing the weighting factor, whether it be $1/R_i^2$ or $1/R_i$, to approach infinity. Subsequently, the voltage at point p will also approach infinity. This problem is alleviated by using the normalized value of p, whereby the voltage at point p becomes

$$V_N = \frac{V}{\sum_{i=1}^K W(R_i)} = \frac{\sum_{i=1}^K W(R_i) \cdot v_i}{\sum_{i=1}^K W(R_i)}$$

The following illustrates the effect of normalization. When point p is relatively distant from any electrode, e_i , the radius is relatively large resulting in a normalizing factor that is small, close to one, and has no significant effect upon the resulting interpolated value. However, as point p approaches an electrode site, the normalizing factor approaches infinity as does the weighting factor and effectively limits the voltage at p to v_i . In other words, as the radius approaches zero, both the weighting factor and the normalizing factor approach infinity. They then cancel each other leaving a maximum interpolation value equal to v_i .

Problems with Inverse Normalized Displays

During initial testing, contrived electrode voltages were presented to the software package to identify undesirable image characteristics

attributable to the Inverse-normalized interpolation routines. Two such characteristics were exhibited by both the Inverse and Inverse-square routines. Due to a lack of better terminology, these image flaws were called "knobs" and "ripples."

Knobs tend to occur around electrode sites which lie near brightness boundaries. Figure 6 illustrates the occurrences of knobs in an image that ideally would have been represented by a set of concentric circles. Ripples were noticed in images where each horizontal row of electrodes were assigned the same voltage (see Figure 7). Preferably, the image would have shown various brightness levels separated by nearly straight horizontal lines.

Two possible solutions were implemented in an effort to reduce these incongruous features and to provide a smoother image.

Face-centered point generation. In an effort to minimize the knobs and ripples, the Face-centered point generation routine was used to compute additional voltages for "pseudo-electrodes" which were interspersed in a regular fashion among the original electrodes. By doing this, the distance over which each interpolation is performed is decreased and the interaction of adjacent electrodes and "pseudo-electrodes" is increased, leading to smoother contour lines. The effect of this technique can be seen by comparing Figures 7 and 8. Note that ripples still occur, but that, overall, the image has generally straighter lines.

An array that is originally $n \times m$ is expanded by a single generation to an $n(n-1) \times m(m-1)$ array; the expansion is performed in

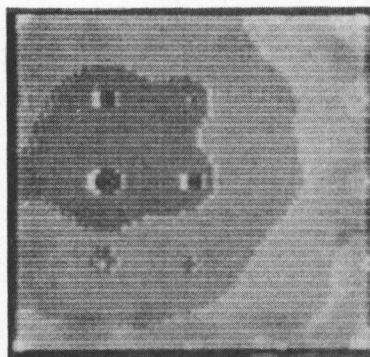


Figure 6. Occurrence of knobs.

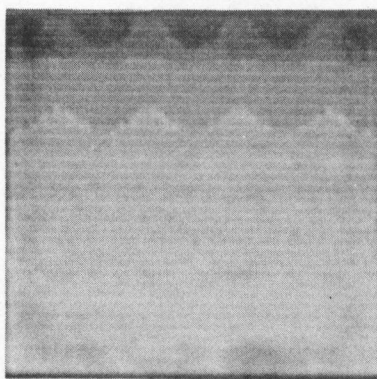


Figure 7. Occurrence of ripples.

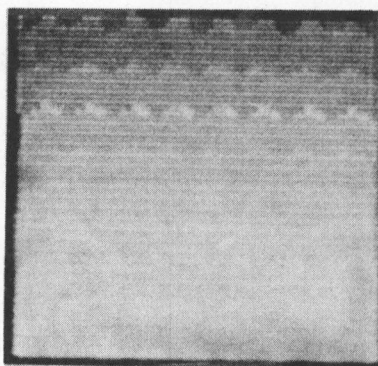


Figure 8. Application of Face-centered point generation to reduce occurrence of ripples.

two steps. The first step computes a value for each set of four commonly adjacent electrodes (see Figure 9). This "pseudo-electrode" is equally distant from the four surrounding electrodes; its voltage is computed by

$$V = \frac{V_1 + V_2 + V_3 + V_4}{4}$$

which is the numerical average. The second step computes the remaining points, involving two cases where the electrodes contributing to the value of the centered point are located above, below, and to either side. In the first case, the centered points are along the perimeter as in Figure 10. There are only three values that may be used since the fourth point is outside the sampling area. The value is computed by

$$V = \frac{V_1 + V_2 + V_3}{3}$$

In case two, all the remaining points are computed (see Figure 11) and again the four points are averaged using

$$V = \frac{V_1 + V_2 + V_3 + V_4}{4}$$

Any number of generations may be performed, resulting in an increasingly dense array of voltage points.

Originally, the addition of "pseudo-electrodes" via the Face-centered point generation routine were to be included as the result of both calculation steps. However, as development progressed it was

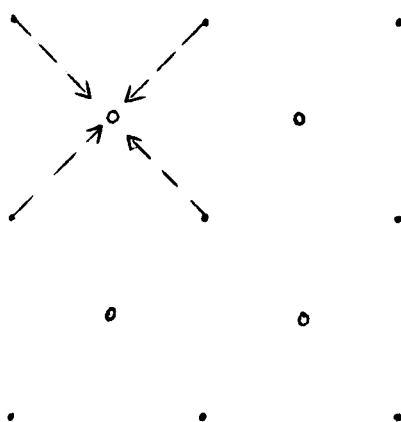


Figure 9. Case 1 example: electrode sites contributing to centered "pseudo-electrode."

• represents original electrode sites

o represents "pseudo-electrode" sites

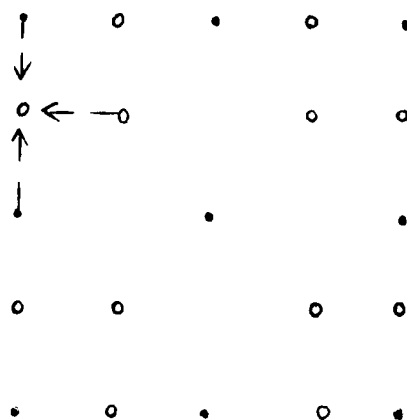


Figure 10. Case 2 example: electrode sites contributing to perimeter "pseudo-electrode."

• represents original electrode site

o represents "pseudo-electrode" site

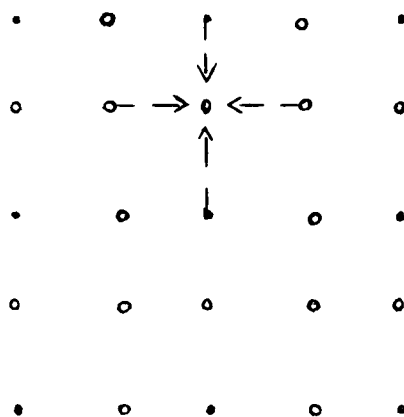


Figure 11. Case 2 example: electrode sites contributing to centered "pseudo-electrode."

• represents original electrode site

o represents "pseudo-electrode" site

decided to allow "pseudo-electrodes" to be included as the result of the first calculation step and become known as a "half-generation." Therefore, the Face-centered point generation routine can be applied in terms of one-half generations, which allow the effect of "pseudo-electrodes" to be studied in greater detail.

"Smear" technique. A second approach taken to reduce the knobs and ripples is the "smear" technique. As the name suggests, this technique is aimed at extending the influence of each electrode slightly to effect a contour smoothing operation. This might also be thought of as "blurring" the image where some of the fine details are lost, yet retaining the areas showing extreme potentials and rapidly changing potentials.

In essence, this technique says that all points lying within a specified "smear" radius of any electrode will be evaluated equally with respect to that electrode. The smear radius has as a maximum value of one-half the distance between any two adjacent electrodes.

Figure 12 illustrates how two points, A and B, would be evaluated with respect to electrode e_i having a smear radius of r_s . Point B clearly has a radius, r_B , that is less than r_s . Therefore, the radius for point B with respect to e_i would be r_s instead of r_B . Point A, on the other hand, lies outside the smear radius and so its radius relative to e_i would be r_A and not r_s .

The effect of the Smear technique can be seen in Figures 13, 14, and 15. As the minimum radius value increases, indicated by the increasing "smear factor," the ripples become less noticeable. In the

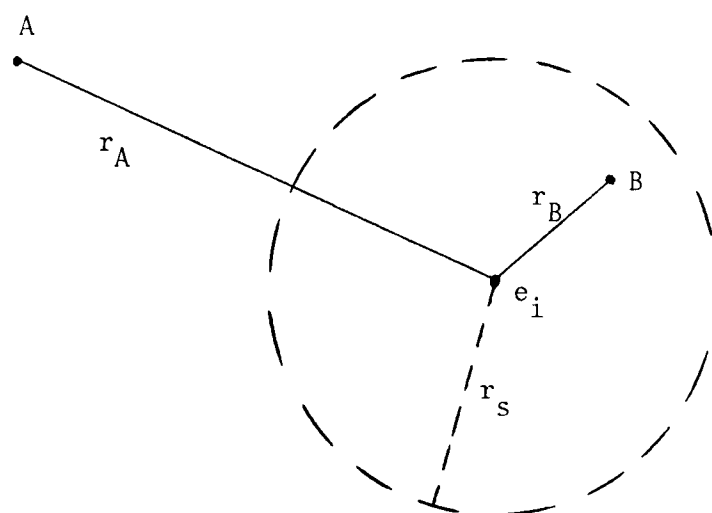


Figure 12. Illustration of "smear radius."

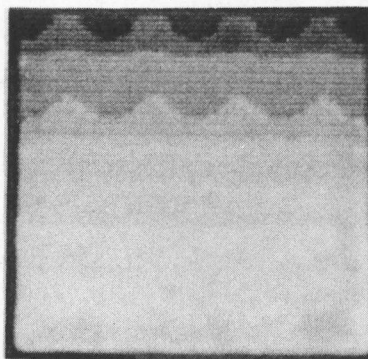


Figure 13. Smear technique with smear factor = .1, straight line data.

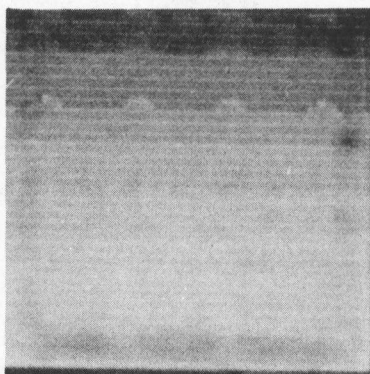


Figure 14. Smear technique with smear factor = .3, straight line data.

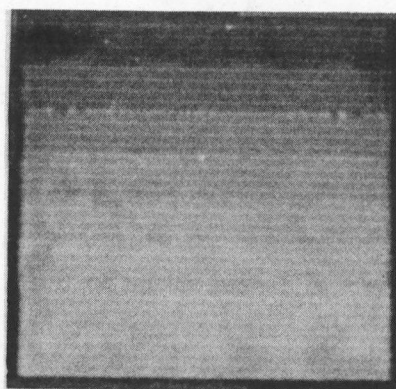


Figure 15. Smear technique with smear factor = .4,
straight line data.

case of knobs, Figures 16 and 17 show that, as the minimum radius increases, considerable smoothing takes place.

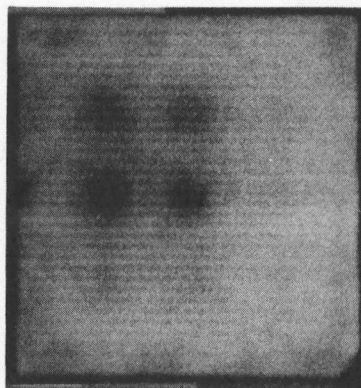


Figure 16. Smear technique with smear factor = .1, conical data.

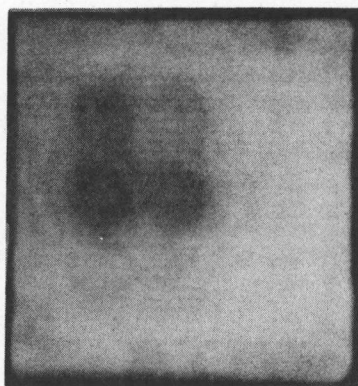


Figure 17. Smear technique with smear factor = .3, conical data.

CHAPTER V

THE INTERPOLATION INVESTIGATION

The Computer Program

The computer program used to simulate the proposed hardware system is presented in three segments: specification of the desired interpolation routine and other required program parameters, performance of the interpolation subroutines, and production of the video image. The interpolation routine to be performed is determined by responses that the operator makes to prompting messages issued by the main program. The requested interpolation routine is performed by one or more subroutines. The video image is produced by another subroutine which converts the data, computed by the interpolation routine, into a form that is acceptable for display on the television screen.

The function of the main computer program is to assist the operator in correctly specifying the current simulation conditions, including the arrangement of the electrodes and their value assignments, as well as the desired interpolation technique and the value of any associated parameters. This is achieved in two ways. First, prompting messages are sent to the operator and contain, whenever possible, a list of allowable responses and a short explanation of each selection. Second, the specific prompting messages that are sent to the operator depend upon selections made to previous requests. Therefore, the operator knows that any requested input is required to assure proper operation

of the simulation program. This frees him from having to screen out messages irrelevant to current needs.

Description of the physical properties of the electrode arrangement is completed with the assignment of the electrode values. This may be accomplished by one of two different methods. The first method is by direct specification from the terminal. The operator is requested to input the value for each electrode position separately. The electrode positions are numbered by row and column according to standard array ordering.

The second method employs real EEG recordings that were stored on a disk pack and were input under program control. Standard operation is sequential input of consecutive time frame recordings. However, an option is available that allows selection of every n^{th} time frame recording. Each record was recorded at standard time intervals, and using this option, one may sample a series of recordings at equal time intervals.

The size of the image produced on the video screen is determined by the number of individual points to be interpolated between any pair of horizontally or vertically spaced electrodes. This value, known as the "interelectrode distance," divides the actual distance between electrodes into a series of discrete points for which values are computed and then displayed. If a large image is desired, then a larger number of points between electrodes should be specified.

The maximum number of gray levels that can be displayed by the current program is sixteen. Any number of levels up to and including

sixteen may be specified by the operator in order to tailor the output image to specific needs.

Before the video image may be generated, the interpolation values must be scaled and assigned a corresponding gray level value. There are two methods for scaling the interpolation values and both may be applied to either terminal or disk input data. The first consists of segmenting the range from the minimum to the maximum values into equal intervals. This is termed equipotential gray level mapping and has been the standard practice in this research. The second method allows one to specify the individual minimum and maximum values for each gray level. This provides the ability to display several levels over a small range of computed values for a more detailed image within that range. A disadvantage of both techniques is that they require advance knowledge of the expected minimum and maximum electrode values. Advance knowledge is required since interpolation, scaling and display activities are performed one line at a time. However, this is not a problem when providing data from the terminal and is only a small inconvenience when using the actual EEG data from disk. The effect of an incorrect specification of the expected minimum and maximum values is the appearance of dark areas where the computed values fall outside the allowable range.

The basic interpolation routines examined in this presentation are the Bilinear, the Inverse-square radius and the Inverse radius. A fourth routine, known as Face-centered point generation, may be used in combination with any of the three basic interpolation algorithms.

The three interpolation routines compute values for each row of picture elements one at a time, beginning with the top row. As processing for each row is completed, the display routine is initiated to include that row in the video image. Control is then returned to the interpolation routine for additional row computations. This sequence continues until the last row in the image is completed, at which time control is returned to the main program. This interpolation and display procedure is used because the memory of the mini-computer is not sufficiently large to contain the entire video image at once.

The EEG data supplied to each interpolation routine is a two dimensional array containing the potential values recorded at each electrode site at a single time instant. The position where each value is found in the array reflects the location of the corresponding electrode on the scalp. The first row in the array represents the electrode row nearest the forehead of the subject with the last row representing the row farthest from the forehead. The resulting video image is oriented in the same manner. The observer is given a top view of the scalp with the nose of the subject centered at the top of the image.

There is one more common feature among the three interpolation routines that needs to be mentioned. The value of points that lie on electrode sites reflect the actual value recorded by the electrode, not some computed value.

The electrode arrangement for the Bilinear algorithm, INTERP, is divided into a set of regions. Each region is defined by four electrodes,

such that each lie in one corner of the region. As the current interpolation point moves from one region to the next, the associated electrode values to be used in the calculation must be updated. To simplify this process, a 2×2 array is maintained which always contains the electrode values associated with the region in which the current interpolation point occurs. It is the elements of this array that are used for calculating the interpolation value, regardless of which one of the three equations is required.

The Inverse radius and Inverse-square radius are two nonlinear techniques that utilize every electrode reading in computing each interpolation value. These two subroutines are operationally identical and, for this reason, the following discussion is applicable to both.

Unlike the Bilinear subroutine which requires knowledge of in which electrode region the interpolation point is located, the Inverse routines have no such requirement. The same electrode values are used to compute interpolation point values, regardless of their location with respect to the current interpolation point.

Due to the above feature of the Inverse subroutines, use of the Face-centered point generation subroutine may include half-generations. When half-generations are performed, extremely high values are assigned to the missing pseudo-electrode sites. These are detected by the Inverse subroutines and calculations that would normally incorporate them are bypassed.

Use of the Smear technique discussed earlier requires that the operator specify the value of the "smear factor." The input parameter

should have a value less than .5 and greater than zero. In the event that the effect of the Smear technique is not desired, a value of .001 should be entered. The subroutine will perform its calculations in the same manner regardless of the value of the "smear factor," but a value of .001 will effectively cause the Smear technique to be nullified.

The Face-centered point generation subroutine, FACE, computes "pseudo-electrode" values that are used, in addition to the original electrode values, as input to the requested interpolation subroutine. The number and location of the values computed depend upon a value provided by the operator, which indicates the number of generations. This value consists of two digits separated by a period. The digit to the left of the period indicates the number of complete generations, and the digit to the right indicates whether the first half of the next generation is to be computed. Using the number of generations requested, the subroutine generates an array of the proper dimensions to contain all the original electrode values plus the ones to be computed. If a half-generation is requested, then the array values for the second half of the incomplete generation are set to an extremely high value so that they will not be used in computations by the interpolation routines. At the completion of FACE, control is returned to the main program which immediately executes the requested interpolation.

If the Face-centered point generation subroutine is used in combination with the Bilinear, then no half-generations may be allowed. This is due to the fact that the Bilinear assumes that all elements in the electrode array are present. If any array elements are missing due to a half-generation, then the resulting video image will be invalid.

Two routines, written in assembler language for the PDP 11/40, are used to interface the FORTRAN IV routines with the video display unit. One subroutine, CLEAR, erases whatever image may have previously been on the video screen and prepares the system to accept the incoming data. The second routine, DISPLY, transforms the gray level numbers generated by the interpolation subroutines into a binary string acceptable to the video system.

The technique employed to produce the video image requires the use of two of the four available output channels. One channel is associated with the lower intensity eight gray levels while the other channel is associated with the remaining eight higher intensity gray levels. The binary string generated reflects this separation and incorporates video system instructions to display both channels on the same image line resulting in sixteen gray levels. The length of each image line and the number of lines in the image are independent of this subroutine and are only limited by the size of the screen.

Photographic and Computer Hardware Description

The computer system consists of a PDP 11/40 with 32K words of memory and runs under the single user operating system RT-11. The peripheral equipment used includes one RK05 disk pack, a DEC VT05 alphanumeric terminal, a desk top line printer, and a Data Disc 6600 Series video display system. The simulation program and EEG test data are stored on the disk. The desk top line printer is available for printing the results of computations performed by the program. Figure 18 illustrates the equipment configuration.

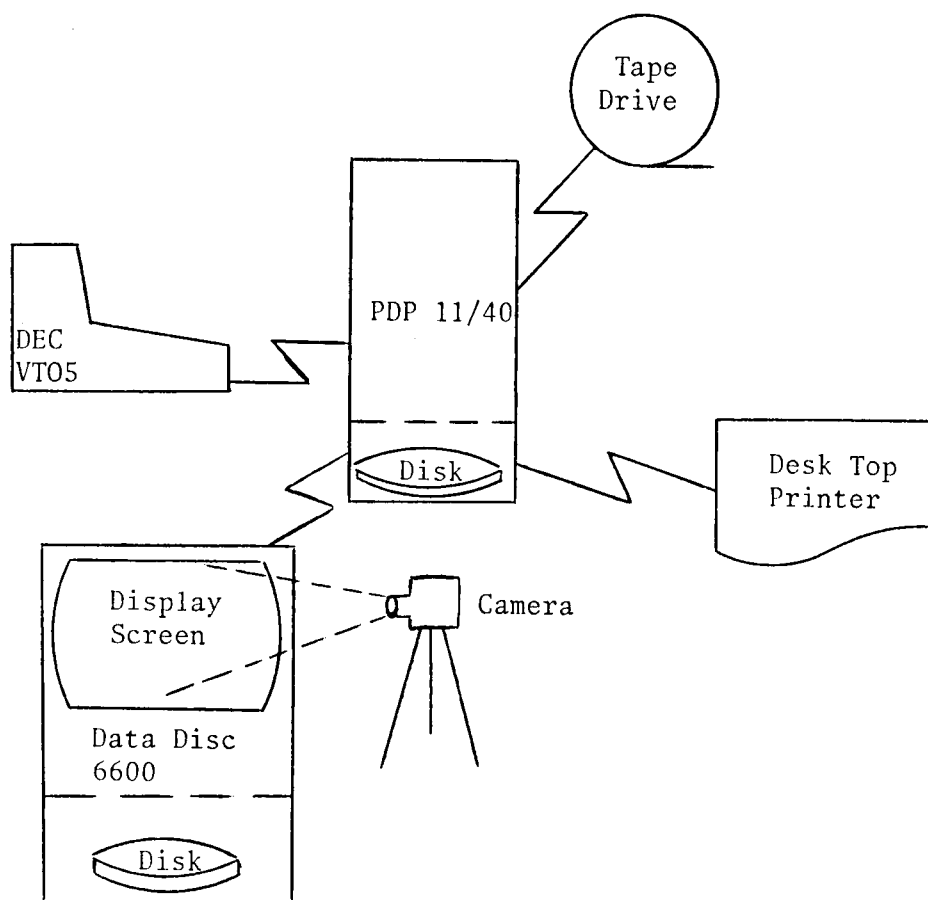


Figure 18. Schematic of computer and photographic equipment.

The video display system consists of two video screens or TV monitors, one color and one black and white, and a video data storage disk. The following discussion of the TV monitor will refer to only the black and white monitor since the color monitor was not used during the experiment. Appendix C addresses the conversion to a color display.

Data is stored on the video disk relative to the order in which it will be displayed. The TV monitors use an interlaced scan, meaning that all the even-numbered lines are displayed and then all the odd-numbered lines are displayed, and so on in an alternating fashion. This is achieved by storing data for the even-numbered display lines or even field on one half of the disk and the odd-numbered data lines or odd field on the other half.

TV monitors have no provisions for storing images on the screen and therefore require continual refreshing. The refreshing is performed by a constant transfer of display data from the disk to the video screen and is accomplished once during each complete revolution of the disk. The disk revolves at a rate of 30 times per second thus the entire TV image is refreshed 30 times each second. This refresh rate is fast enough so that before the brightness level of any point decays to a level perceptible by the human eye, the point has already been refreshed. This is why the image appears to be fixed and free of any distracting flicker.

Several types of data may be displayed on the video screen. The generation of images requires that instructions be presented to the video system prior to the data to be displayed. Alphanumeric characters

of varying sizes may be displayed by specifying the character and the screen location. Straight lines and right rectangles may also be drawn by indicating the correct location parameters. The fourth type of data that may be displayed is called graphic byte. It permits addressing of individual picture elements or pixels, which are singular display points whose screen positions are indicated by row and column numbers. There are 480 rows and 640 columns of addressable points. The rows are numbered 0 to 479 from top to bottom and the columns are numbered 0 to 639 from left to right. The last method was chosen primarily because of the flexibility it allows in generating an image and because of its simplicity. Data written to the screen may be in the form of either black and white or gray scale. Use of the gray scale option allows pixels to be assigned various brightness or light intensity levels ranging from black to white.

Data is transferred from the storage disk to the screen through what are called I/O channels. There are four channels, each of which may individually display up to four different gray levels. The gray level is determined by the value of a two digit binary number. The four possible combinations are 00, 01, 10 and 11. In addition, each channel has a different base line intensity. Thus, the four binary combinations will each display a different gray level when used with different channels, resulting in sixteen different levels. To increase the number of possible gray levels, multiple channels may be used simultaneously to display one pixel. If two channels are used, then a four digit binary number is used to describe one of sixteen possible gray level combinations. The same is true for the use of three and four channels

simultaneously. Three channels yield a six digit binary number and 64 possible gray levels, while four channels yield an eight digit binary number and 256 possible gray levels.

The equipment used to photograph the image on the video screen consists of a Minolta SRT-100 camera fitted with a No. 2 close-up lens. The lens was positioned 9.75 inches from the screen with an aperture of 5.6f and a shutter speed of 1/8 second. These settings were standard during each picture taking session to insure consistency in the quality of the pictures taken between different sessions. An entire picture taking session, using a series of images, was devoted to determining the settings best suited for photographing the TV monitor.

The shutter speed of 1/8 second allows for approximately four complete traces of the image during each exposure. At other shutter speeds the last image retrace was not completed due to the rotational speed of the video disk. This resulted in the portion of the image with the additional retrace appearing darker than the portion of the image without the additional retrace. Minor adjustments of the brightness and contrast controls on the video screen were made from time to time to enhance desired characteristics of the image.

The Experiment

Determination of the interpolation routine to be suggested for hardware implementation is, at this point, based upon the quality of the image produced. Data presented to the simulation program consists of specific patterns of contrived electrode voltages and a full second of real EEG potential recordings. Unless otherwise specified, all data

patterns consist of 25 electrodes arranged in a regular 5×5 array pattern and are equally spaced, both horizontally and vertically. The contrived voltage patterns were specifically designed to test the flexibility of the Inverse and Inverse-square routines and the images produced were compared to the image generated by the Bilinear routine.

The two test patterns are referred to as "straight line" and "conical." Every electrode in each row of the straight line pattern is assigned the same voltage. The voltage assigned to the top row was 10 millivolts and was increased by 10 for each successive row, so that the bottom row had a value of 50 millivolts. The expected gray scale image would be a series of straight or nearly straight horizontal lines. The electrode sites for the conical pattern were assigned values to simulate the occurrence of a single voltage source which would generate a series of concentric circles. As seen in Figures 19 and 20, the Bilinear interpolation method approximates both these regions quite well. However, Figure 19, in particular, shows the straight lines that are characteristic of the Bilinear technique when it is used to approximate continuous regions.

The EEG data was supplied by Dr. Lehmann, Neurologische Universitätsklinik und Poliklinik, Kantonsspital Zurich, Switzerland. The data used during the testing phases was real time spontaneous alpha EEG recorded using 48 channels, some of which were not always connected or became unusable during the recording session. The readings were made at constant time intervals of 4 milliseconds, allowing 250 samples per second. The data supplied was on a magnetic tape, and was not directly

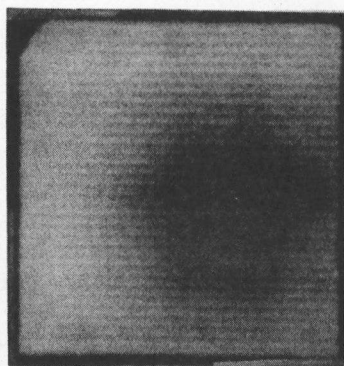


Figure 19. Bilinear interpolation of conical data.

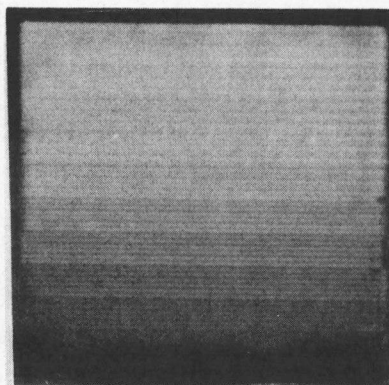


Figure 20. Bilinear interpolation of straight line data.

usable. A special program was written to read the data from the tape and write it to the mini-computer RK05 disk in a format acceptable to the simulation program. During this research, only 25 of the original 48 channels were used. Of the 250 time instants available, every tenth one was selected for investigation providing 25 equally spaced samples.

The experiment consisted of three phases: a pilot study, the main investigation, and a final concentrated study. The goal for Phase I was the determination of undesirable characteristics in the images generated by the Inverse radius and the Inverse-square radius interpolation routines and the selection of possible techniques for correcting these deficiencies. As discussed in Chapter IV, the characteristics observed were knobs and ripples and the contour smoothing techniques were the Face-centered point generation and Smear techniques.

An additional feature that became evident during Phase I is called a singularity. It appears as a small dot located at electrode sites and is completely surrounded by a different gray level, as in Figure 21. Each singularity is composed of the electrode site and one or more interpolated points around it. The occurrence of singularities indicate that the potential value of an electrode is not sufficiently large to affect many, if any, of the interpolated values of nearby points. In fact, the values of the points contained in the singularity may be quite close to the values of the points around it, but due to the particular range of values associated with each gray level, they are assigned different brightness values. Generally, the size of the singular region directly reflects the degree to which it differs with the surrounding

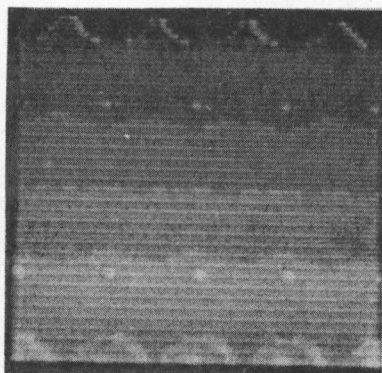


Figure 21. Illustration of singularities.

region. The smaller the singularity, the smaller the difference between the actual electrode voltage and the value of the interpolated points outside the singularity.

During Phase II, the smoothing techniques were implemented. To evaluate these techniques, another series of images using the test data were photographed for both the Inverse radius and Inverse-square radius routines.

When the Face-centered point generation routine was used with the conical data, additional singularities were observed toward the center of the image instead of a general smoothing of the contours (see Figure 22). The number of generations ranged from one-half to one and one-half with similar results in all cases. However, the Inverse-square image did have smoother contours than the Inverse, but that was due to the difference in the routines, not as a result of the Face-centered point generation. When straight line data was used, the results were somewhat better for both inverse routines in that the amplitude of the waves were noticeably reduced.

The Smear technique, when applied to the conical data, was quite successful considering the severe nature of the data. Figures 23 and 24 show that adjacent gray levels tend to form common gray level regions as the smear factor increases.

The Smear technique was also successful against the straight line data in terms of decreasing the amplitude of the wave form. In fact, for a smear factor of .4, the Inverse-square image, Figure 25, was very similar to that generated by the Bilinear, Figure 20 (page 41).

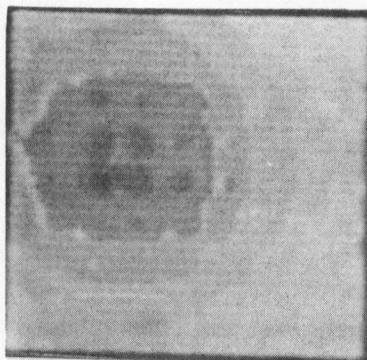


Figure 22. Inverse-square radius with one generation of Face-centered technique, conical data.

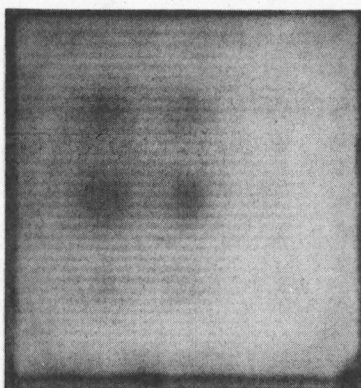


Figure 23. Inverse-square radius with a smear factor = .1, conical data.

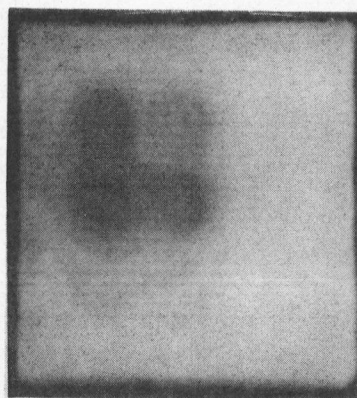


Figure 24. Inverse-square radius with smear factor = .3,
conical data.

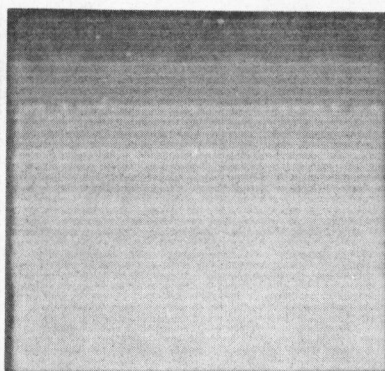


Figure 25. Inverse-square radius with smear factor = .4,
straight line data.

Noting the singularities in Phase I, a more intensive study was conducted regarding their occurrence and effect. Singularities were found in both the Inverse radius and the Inverse-square radius images of real EEG data. There were no noticeable deficiencies in the Inverse-square images, but the number of visible gray levels in the Inverse image were markedly less than in the same image generated using the Bilinear routine.

Application of the Face-centered point generation routine to reduce the occurrence of singularities was totally ineffective. The result was not fewer singularities, but more, for both the inverse routines. On the other hand, the Smear technique was quite effective in decreasing the size of the singularities and in some cases removing them completely. In either case, the basic problem is not with the occurrence of singularities, but rather the decreased number of visible gray levels exhibited by the Inverse radius images.

At this point, it became evident that the Inverse-square radius is a more promising technique than the Inverse radius and that additional investigation of the combination of the Inverse-square with both the Face-centered and Smear techniques should be pursued. During this phase, a large number of different images were used, most of which exhibited similar features. Therefore, a representative few were selected for use in Phase III.

The scope of the third and final phase is limited to the Inverse-square routine and images selected following Phase II. Considering the success of the Face-centered point generation in the

straight line test data and the increased amount of data it provides the interpolation routine, plus the singularity removal success of the Smear technique, the two were combined with the Inverse-square radius. The combination of these two techniques with the Inverse-square produced several different routines resulting from the various degrees to which the Face-centered point generation and Smear techniques were applied.

As expected, singularities were generated and were quite noticeable for low smear factor values, but as the value of the smear factor increased nearly all the singularities were removed. This was the case regardless how many generations of Face-centered point generations were performed. A comparison of the Inverse-square in combination with Face-centered point generation and the Smear technique against the Inverse-square with only Smear does not show any great differences. The only point of conflict is the occasional singularities caused by the Face-centered point generation. Therefore, of the two routines, the Inverse-square with Smear would be preferable.

To compare the Bilinear, the Inverse-square and the Inverse-square with various smear factor values, three time instants have been selected (Figures 26 through 34). It is evident from this series of images that the three routines produce very similar images. However, the Inverse-square with a smear factor in the range of .2 to .3 exhibits smoother contours than the Inverse-square without the Smear technique.

Figure 26. EEG data time frame 70, Bilinear interpolation.

Figure 27. EEG data time frame 70, Inverse-square radius interpolation.

Figure 28. EEG data time frame 70, Inverse-square radius interpolation with a smear factor = .3.

Figure 29. EEG data time frame 160, Bilinear interpolation.

Figure 30. EEG data time frame 160, Inverse-square radius interpolation.

Figure 31. EEG data time frame 160, Inverse-square radius with a smear factor = .3.

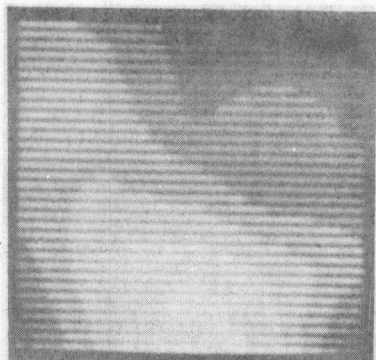


Figure 26

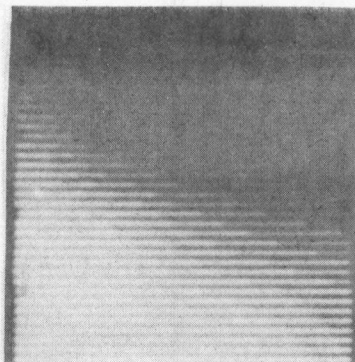


Figure 29



Figure 27

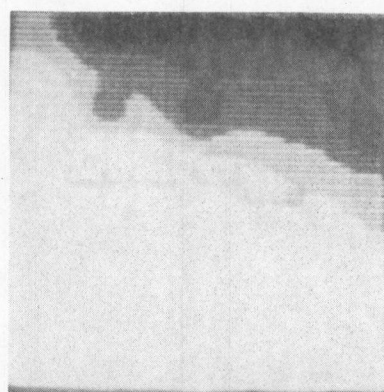


Figure 30

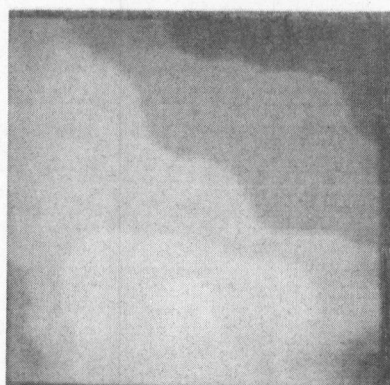


Figure 28



Figure 31

Figure 32. EEG data time frame 230, Bilinear interpolation.

Figure 33. EEG data time frame 230, Inverse-square radius interpolation.

Figure 34. EEG data time frame 230, Inverse-square radius with a smear factor = .3.

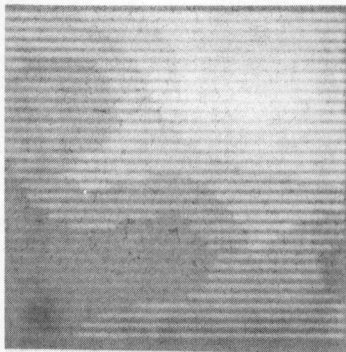


Figure 32

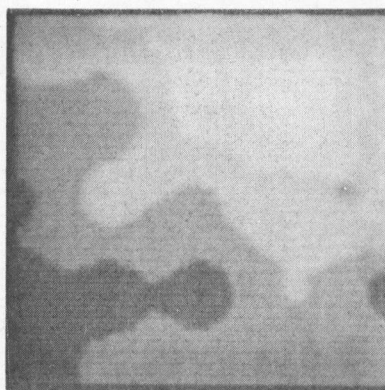


Figure 33

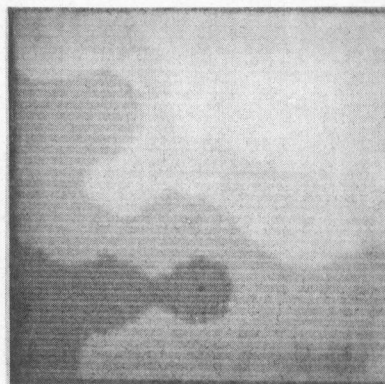


Figure 34

CHAPTER VI

CONCLUSION

The feasibility of constructing a hardware system capable of producing a real time two-dimensional contour map of the potential field over the human scalp on a TV screen is dependent upon three factors: the availability of an acceptable interpolation routine, the adaptability of that interpolation routine to electronic components, and the availability of the components.

Results from the experiment show that the Inverse-square radius interpolation when combined with the Smear technique is capable of producing an image that is very similar to that generated by the Bilinear interpolation routine. The simplicity of the calculations performed by the Inverse-square radius routine make it adaptable to hardware components which are available due to continuing technological advancements in electronic circuitry. Having fulfilled these requirements, the Inverse-square radius interpolation with the Smear capability should be considered as a viable option for hardware construction.

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LIST OF REFERENCES

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APPENDIXES

APPENDIX A

BILINEAR INTERPOLATION EQUATIONS

Equations for the "X-first" and "Y-first" Bilinear algorithm follow. The voltage for any point G is denoted $f(G)$. Electrode sites are A, B, C and D.

X-first:

$$f_x(P) = f(A) + (f(B) - f(A)) (x_1/x_2)$$

$$f_x(R) = f(C) + (f(D) - f(C)) (x_1/x_2)$$

$$f_x(Q) = f(P) + (f(R) - f(P)) (y_1/y_2)$$

Y-first:

$$f_y(P_1) = f(A) + (f(C) - f(A)) (y_1/y_2)$$

$$f_y(R_1) = f(B) + (f(D) - f(B)) (y_1/y_2)$$

$$f_y(Q) = f(P_1) + (f(R_1) - f(P_1)) (x_1/x_2)$$

The interpolated values for points on the perimeter are computed by taking the difference between the two electrodes on either side and reducing the difference by a factor of the distance between them. The result is then added to the voltage of the electrode from which the point is measured. The point in question is Q and it will be shown in the following that $f_x(Q)$ is equivalent to $f_y(Q)$.

Expand $f_x(Q)$:

$$\begin{aligned}
 f_x(Q) &= f(P) + (f(R) - f(P)) (y_1/y_2) \\
 f_x(Q) &= [f(A) + (f(B) - f(A)) (x_1/x_2)] + \\
 &\quad [(f(C) + (f(D) - f(C)) (x_1/x_2)) - \\
 &\quad (f(A) + (f(B) - f(A)) (x_1/x_2))] (y_1/y_2) \\
 f_x(Q) &= f(A) + f(B) (x_1/x_2) - f(A) (x_1/x_2) + \\
 &\quad [(f(C) + f(D) (x_1/x_2) - f(C) (x_1/x_2)) - \\
 &\quad (f(A) + f(B) (x_1/x_2) - f(A) (x_1/x_2))] (y_1/y_2) \\
 f_x(Q) &= f(A) + f(B) (x_1/x_2) - f(A) (x_1/x_2) + \\
 &\quad f(C) (y_1/y_2) + f(D) (x_1/x_2) (y_1/y_2) - \\
 &\quad f(C) (x_1/x_2) (y_1/y_2) - f(A) (y_1/y_2) - \\
 &\quad f(B) (x_1/x_2) (y_1/y_2) + f(A) (x_1/x_2) (y_1/y_2) \\
 f_x(Q) &= f(A) [1 - (x_1/x_2) - (y_1/y_2) + (x_1/x_2) (y_1/y_2)] + \\
 &\quad f(B) [(x_1/x_2) - (x_1/x_2) (y_1/y_2)] + \\
 &\quad f(C) [(y_1/y_2) - (x_1/x_2) (y_1/y_2)] + \\
 &\quad f(D) [(x_1/x_2) (y_1/y_2)] \tag{A-1}
 \end{aligned}$$

Expand $f_y(Q)$:

$$\begin{aligned}
 f_y(Q) &= f(P_1) + (f(R_1) - f(P_1)) (x_1/x_2) \\
 f_y(Q) &= [f(A) + (f(C) - f(A)) (y_1/y_2)] + \\
 &\quad [(f(B) + ((f(D) - f(B)) (y_1/y_2)) - \\
 &\quad (f(A) + (f(C) - f(A) (y_1/y_2)) (x_1/x_2) \\
 f_y(Q) &= f(A) + f(C) (y_1/y_2) - f(A) (y_1/y_2) + \\
 &\quad [f(B) + f(D) (y_1/y_2) - f(B) (y_1/y_2) - \\
 &\quad f(A) - f(C) (y_1/y_2) + f(A) (y_1/y_2)] (x_1/x_2)
 \end{aligned}$$

$$\begin{aligned}
f_y(Q) &= f(A) + f(C) (y_1/y_2) - f(A) (y_1/y_2) + \\
&\quad f(B) (x_1/x_2) + f(D) (y_1/y_2) (x_1/x_2) - \\
&\quad f(B) (y_1/y_2) (x_1/x_2) - f(A) (x_1/x_2) - \\
&\quad f(C) (y_1/y_2) (x_1/x_2) + f(A) (y_1/y_2) (x_1/x_2) \\
f_y(Q) &= f(A) [1 - (y_1/y_2) - (x_1/x_2) + (y_1/y_2) (x_1/x_2)] + \\
&\quad f(B) [(x_1/x_2) - (y_1/y_2) (x_1/x_2)] + \\
&\quad f(C) [(y_1/y_2) - (y_1/y_2) (x_1/x_2)] + \\
&\quad f(D) [(y_1/y_2) (x_1/x_2)] \tag{A-2}
\end{aligned}$$

Comparing equations (A-1) and (A-2), it is clear that they are equivalent.

APPENDIX B

COMPUTER PROGRAM LISTING

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0001      COMMON ERANGE(17), ELECTR(21,21), ISPACE, IROW, ICOL,
          * MAXCOL, NUMLEV, IDEBUG, MAXROW, INTVAL(400)
C ** COMMON BLOCK FOR SUBROUTINE FACE
0002      COMMON /BLOCK1/EXPAND(21,21), ISETS, SETS, ISIZE, JSIZE, JDEBUG
C ** COMMON BLOCK FOR SUBROUTINE ISGRAD AND SUBROUTINE INVRAD
0003      COMMON /BLOCK3/EVAL(400), CLEAR
0004      DIMENSION LOCATE(48,3), EDATA(48)

C
C ***** VARIABLE DEFINITIONS *****
C
C      IROW - # OF ROWS IN ELECTRODE NET
C      ICOL - # OF COLUMNS IN ELECTRODE NET
C      NUMLEV - # OF POTENTIAL LEVELS (GRAY LEVELS) --- CURRENTLY EQUAL SPACING
C      ISPACE - # OF POINTS BETW/ EACH ELECTRODE --- CURRENTLY EQUAL SPACING
C      ELECTR(21,21) - VALUES FOR EACH ELECTRODE
C      ERANGE(17) - BOUNDARY VALUES FOR POTENTIAL LEVELS
C      EMAX - MAXIMUM POTENTIAL LEVEL VALUE
C      EMIN - MINIMUM POTENTIAL LEVEL VALUE
C      STEP - ABSOLUTE RANGE OF EACH LEVEL
C      MAXROW - TOTAL # OF ROWS IN THE DISPLAY
C      MAXCOL - TOTAL # OF COLUMNS IN THE DISPLAY
C      NUMROW - # OF CURRENT ROW
C
C *****
C
C
C THE CALL TO SUBROUTINE CLEAR RESULTS IN BLANKING THE
C VIDEO SCREEN PRIOR TO EACH DISPLAY
C
0005      1      CALL CLEAR
0006      ICHNGE = 10
0007      NPASS = 0
C
C ----> INITIALIZE MAX & MIN ELECTRODE POTENTIALS
0008      EMAX = -1000.
0009      EMIN = 1000.
0010      WRITE(7,50)
0011      50      FORMAT(' DO YOU WANT TO SEE DEBUG MESSAGES ? ' /
          *5X, ' 0 = NO'/5X, ' 1 = TERMINAL MESSAGES'/5X, ' 2 = PRINTER',
          *'/ MESSAGES'/5X, ' 3 = ALL MESSAGES')
0012      READ(5,200) IDEBUG
C
C --> INPUT SIZE OF ELECTRODE NET (IROW, ISIZE)
0013      WRITE(7,100)
0014      100     FORMAT(' INPUT # OF ROWS IN ELECTRODE NET')
0015      READ(5,200) IROW
0016      200     FORMAT(I3)
0017      WRITE(7,300)
0018      300     FORMAT(' INPUT # OF COLUMNS IN ELECTRODE NET')
0019      READ(5,200) ICOL
C
C --> KROW & KCOL ARE USED LATER TO DETERMINE WHICH ELECTRODE
C READINGS ARE USABLE
0020      KROW = IROW

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0021      KCOL = ICOL
      C
      C ---> SPECIFY # OF INTERPOLATION POINTS BETWEEN EACH PAIR OF ELECTRODES
0022      WRITE(7,400)
0023      400  FORMAT(' INPUT # OF POINTS BETW/ EACH ELECTRODE')
0024      READ(5,200) ISPACE
      C
      C ---> SELECT ELECTRODE DATA SOURCE
0025      WRITE(7,404)
0026      404  FORMAT(' INDICATE SOURCE OF EEG DATA//
      * 5X, ' 0 = TERMINAL//5X, ' 1 = DISK FILE')
0027      READ(7,200) INPUT
0028      IF (INPUT .EQ. 1) GO TO 970
      C
      C ---> INPUT ELECTRODE VALUES FROM TERMINAL
0030      DO 500 I = 1, IRCW
0031      DO 500 J = 1, ICOL
0032      WRITE(7,600) I, J
0033      600  FORMAT(' INPUT ELECTRODE POTENTIAL FOR POSITION (' , I2, ', ' , I2, ')')
0034      READ(5,700) ELECTR(I,J)
0035      700  FORMAT('F4.2)
0036      IF (ELECTR(I,J) .GT. EMAX) EMAX = ELECTR(I,J)
0038      IF (ELECTR(I,J) .LT. EMIN) EMIN = ELECTR(I,J)
0040      500  CONTINUE
0041      GO TO 971
      C
      C ---> THE FOLLOWING CODE READS THE ELECTRODE POSITION VALUES FROM DISK
      C
      C      1. INPUT ELECTRODE POSITIONS AND SET INDICATOR WHICH
      C          SPECIFIES WHETHER OF NOT THE SPECIFIC
      C          RECORDING POSITION IS USABLE.
      C
      C ---> ASSIGN 1 AS THE LOGICAL UNIT # FOR THE DISK FILE
0042      970  CALL ASSIGN(1, 'TEST1.DAT')
      C
      C ---> SPECIFY THE NTH RECORD WHICH IS TO BE SELECTED FROM THE
      C          AVAILABLE DATA BY INDICATING N AT THE TERMINAL
      C          (ONLY USED WITH DISK DATA)
0043      WRITE(7,931)
0044      931  FORMAT(' SELECT EVERY NTH EEG RECORD FROM AVAILABLE',
      * ' TIME FRAME - SPECIFY N (I3)')
0045      READ(7,200) NTHREC
0046      DO 979 K = 1, 48
0047      READ(1,980) (LOCATE(K,J), J=1,2)
      C
      C LOCATE(K,3) IS THE USABLE INDICATOR FOR EACH PAIR OF ELECTRODE COORDINATES
0048      LOCATE(K,3) = 1
0049      IF (LOCATE(K,1) .EQ. 0 .AND. LOCATE(K,2) .EQ. 0) LOCATE(K,3)=0
0051      979  CONTINUE
0052      980  FORMAT(30X, 2(8X, I2))
      C
      C ---> OUTPUT LOCATE VALUES ONLY WHEN DEBUGGING ERRORS
0053      IF (IDBUG .NE. 2) GO TO 1980
0055      DO 909 K = 1, 48

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0056      WRITE(6,976) K, (LOCATE(K,J),J=1,3)
0057 909  CONTINUE
0058 976  FORMAT(' LOCATE VALUES (K =',I2,', J = 1, 2, 3)',3(5X,I2))
      C
      C READ REMAINDER OF CURRENT DATA BLOCK (SKIP OVER NEXT 2 RECORDS)
0059 1980 READ(1,981) I, J
0060 981  FORMAT(I2/I2)
      C
      C ---> INDICATE WHETHER OR NOT A PAUSE FOLLOWING EACH COMPLETED DISPLAY
      C OUTPUT IS TO OCCUR (ONLY WHEN READING EEG DATA FROM DISK FILE)
0061      WRITE(7,1984)
0062 1984  FORMAT(' SHOULD I PAUSE AFTER EACH COMPLETED DISPLAY ?'/
      * 5X, / 0 = NO'/5X, / 1 = YES')
0063      READ(7,200) IPAUSE
      C
      C ---> INPUT # OF GRAY LEVELS TO BE DISPLAYED
0064 971  WRITE(7,800)
0065 800  FORMAT(' INPUT # OF POTENTIAL LEVELS')
0066      READ(5,200) NUMLEV
      C
      C ---> SPECIFY METHOD FOR LEVEL RANGE SETTING
      C (IRANGE = 0 CANNOT BE USED W/ DISK DATA)
0067      WRITE(7,1925)
0068 1925  FORMAT(' INDICATE METHOD FOR SETTING POTENTIAL',
      * ' LEVEL RANGE VALUES'/5X, / 0 = EQUI-POTENTIAL',
      * ' RANGES BETWEEN MIN & MAX INPUT VALUES'/5X, / 1 = INPUT',
      * ' SPECIFIC RANGES (CONTINUOUS)'/5X, / 2 = SPECIFY MIN & MAX',
      * ' VALUES (EQUI-POTENTIAL)')
0069      READ(7,200) IRANGE
0070      IF (IRANGE .EQ. 0) GO TO 1800
0072      IF (IRANGE .EQ. 1) GO TO 1926
      C
      C ---> INPUT SPECIFIC MIN & MAX VALUES TO BE DISPLAYED
0074      WRITE(7,1801)
0075 1801  FORMAT(' INPUT MIN POTENTIAL VALUE TO BE DISPLAYED (F12.8)')
0076      READ(7,1831) EMIN
0077      WRITE(7,1803)
0078 1803  FORMAT(' INPUT MAX POTENTIAL VALUE TO BE DISPLAYED (F12.8)')
0079      READ(7,1831) EMAX
      C
      C ----> CALCULATE EQUI-POTENTIAL RANGE VALUES
      C STEP - CONSTANT INCREMENT BETWEEN EACH LEVEL
      C ERANGE(1) = MINIMUM POTENTIAL LEVEL VALUE (MIN
      C ELECTRODE VALUE)
      C ERANGE(NUMLEV+1) = MAXIMUM POTENTIAL LEVEL VALUE
0080 1800  STEP = (EMAX - EMIN) / NUMLEV
0081      ERANGE(1) = EMIN
0082      ERANGE(NUMLEV+1) = EMAX
0083      WRITE(7,78) STEP,EMAX,EMIN
0084 78    FORMAT(' STEP=',F8.3, / EMAX=',F8.3, / EMIN=',F8.3)
0085      DO 900 I = 2, NUMLEV
0086      K = I - 1
0087      ERANGE(I) = ERANGE(K) + STEP
0088 900  CONTINUE

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0089      GO TO 72
      C
      C --> SPECIFY MIN & MAX VALUE FOR EACH LEVEL (CONTINUOUS)
0090 1826 WRITE(7,1827)
0091 1827 FORMAT(' INPUT MIN DATA VALUE TO BE ANALYZED (F12.8)')
0092      READ(7,1828) EMIN
0093 1828 FORMAT(F12.7)
0094      ERANGE(1) = EMIN
0095      DO 1829 K = 1, NUMLEV
0096          WRITE(7,1830) K
0097          READ(7,1831) EMAX
0098          ERANGE(K+1) = EMAX
0099 1829 CONTINUE
0100 1830 FORMAT(' INPUT MAX VALUE (F12.8) FOR LEVEL ',I2)
0101 1831 FORMAT(F12.8)
0102      WRITE(6,556) EMIN, EMAX
0103 556  FORMAT(' EMIN = ',E20.6,' , EMAX = ',E20.6)
      C
      C --> OUTPUT TO TERMINAL THE RESULTING LEVEL RANGES
0104 72   DO 73 K = 1, NUMLEV
0105      WRITE(7,74) K, ERANGE(K)
0106 73   CONTINUE
0107      WRITE(7,74) K, ERANGE(K)
0108 74   FORMAT(' ERANGE(',I2,') = ',F12.7)
      C
      C --> READ EEG DATA FROM DISK FILE
      C      (IF INPUT = 0 THEN DATA HAS ALREADY BEEN INPUT FROM TERMINAL)
0109      IF (INPUT .NE. 1) GO TO 545
      C
      C --> DETERMINE ROW & COLUMN INCREMENT VALUES W. R. T. ELECTRODE NET SIZE
      C      (INCRJ = COLUMN INCREMENT)
      C      (INCRI = ROW INCREMENT)
0111      INCRI = -1
0112      IF (KCOL .EQ. 2) INCRJ = 4
0114      IF (KCOL .EQ. 3) INCRJ = 2
0116      IF (KCOL .EQ. 5) INCRJ = 1
0118      INCRI = -1
0119      IF (KROW .EQ. 2) INCRI = 4
0121      IF (KROW .EQ. 3) INCRI = 2
0123      IF (KROW .EQ. 5) INCRI = 1
0125      IF (INCRI .GT. 0 .AND. INCRJ .GT. 0) GO TO 1832
0127      IF (INCRI .LT. 0) WRITE(6,3210) KROW
0129      IF (INCRJ .LT. 0) WRITE(6,3110) KCOL
0131 3110 FORMAT(' INVALID # OF COLUMNS IN ELECTRODE NET ',I2,
      *      ' ; PGM. TERMINATING')
0132 3210 FORMAT(' INVALID # OF ROWS IN ELECTRODE NET ',I2,
      *      ' ; PGM. TERMINATING')
0133      STOP
      C
      C --> INPUT 1 SET OF EEG READINGS FROM CURRENT TIME FRAME
      C
      C --> SELECT EVERY NTH EEGRECORD FROM THE DATA SOURCE
0134 1832 DO 9888 IR = 1, NTHREC
0135      READ(1,982,END=1557) (EDATA(I),I=1,43)

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0136 9888 CONTINUE
0137 982  FORMAT(4E20.6)
      C WRITE(6,2788) (EDATA(I),I=1,48)
C2788 FORMAT(' '////'THE FOLLOWING IS EEG DATA DIRECTLY FROM DISK'
      C * //(12(5X,4E20.6//))////)
      C
      C --> INITIALIZE ARRAY ELECTR TO 100.
0138      DO 8210 IR = 1, 5
0139      DO 8220 IC = 1, 5
0140      ELECTR(IR,IC) = 100.
0141 8220 CONTINUE
0142 8210 CONTINUE
      C
      C --> INITIALIZE EEG DATA ARRAY FOR PROCESSING OF CURRENT DATA
0143      DO 983 K = 1, 48
0144      IC = -2
0145      IR = 2
0146      DO 984 I = 1, 5, INCRI
0147      IF (LOCATE(K,1) .EQ. IR) GO TO 987
0148      IR = IR + INCRI
0150 984 CONTINUE
0151      GO TO 983
0152 987 DO 986 J = 1, 5, INCRJ
0153      IF (LOCATE(K,2) .EQ. IC) GO TO 988
0155      IC = IC + INCRJ
0156 986 CONTINUE
0157      GO TO 983
0158 988 I = LOCATE(K,1) - 1
0159      J = LOCATE(K,2) + 3
0160      ELECTR(I,J) = EDATA(K)
      C WRITE(6,992) K, LOCATE(K,1), K, LOCATE(K,2), I, J, ELECTR(I,J)
C992  FORMAT(' LOCATE(',12,',1) = ',12,', LOCATE(',12,',2) = ',
      C * 12,', INITIALLY POSITIONED AT ELECTR(',12,',',12,',) = ',E20.7)
0161      IF (ELECTR(I,J) .GT. EMAX) EMAX = ELECTR(I,J)
0163      IF (ELECTR(I,J) .LT. EMIN) EMIN = ELECTR(I,J)
0165 983 CONTINUE
      C
      C --> COMPRESS THE SELECTED ELECTRODE POSITIONS TO ACTUAL SIZE OF ELECTR(*,*)
0166      IREAL = IROW + (IROW - 1) * (INCRI - 1)
0167      JREAL = ICOL + (ICOL - 1) * (INCRJ - 1)
0168      I = 1
0169      DO 8230 IR = 1, IREAL, INCRI
0170      J = 1
0171      DO 8240 IC = 1, JREAL, INCRJ
0172      ELECTR(I,J) = ELECTR(IR,IC)
0173      J = J + 1
0174 8240 CONTINUE
0175      I = I + 1
0176 8230 CONTINUE
      C --> FOLLOWING CODE OUTPUTS ELECTR(*,*) TO PRINTER FOR
      C DEBUGGING PURPOSES
0177 545 CONTINUE
0178      DO 552 IR = 1, IROW
0179      DO 553 IC = 1, ICOL

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      C      WRITE(6,554) IR, IC, ELECTR(IR, IC)
0180 553  CONTINUE
0181 552  CONTINUE
0182 554  FORMAT(' ELECTR(', I2, ', ', I2, ') = ', E20.6)
      C
      C ----> INDICATE WHETHER OR NOT FACE-CENTERED POINT
      C      GENERATION IS TO BE PERFORMED
      C      BEFORE FIRST IMAGE PRODUCED:
      C      ICHNGE = 10 (INITIAL VALUE)
      C      AFTER FIRST IMAGE PRODUCED:
      C      ICHNGE = 0 (NO INTERPOLATION ROUTINE CHANGE ON CURRENT DATA)
      C      ICHNGE = 1 (CHANGE INTERPOLATION ROUTINE FROM PREVIOUS)
0183 991  IF (INPUT .GT. 0 .AND. NPASS .GT. 0) GO TO 2000
0185     IF (ICHNGE .LT. 1) GO TO 2000
0187     WRITE(7,1000)
0188 1000  FORMAT(' PERFORM FACE-CENTERED POINT GENERATION ROUTINE ?'
      * //, 5X, ' 0 = NO' //, 5X, ' 1 = YES')
0189     READ(5,200) IFACE
0190 2000  IF (IFACE .NE. 1) GO TO 1005
0192     IF (INPUT .GT. 0 .AND. NPASS .GT. 0) GO TO 2001
0194     WRITE(7,1010)
0195 1010  FORMAT(' INPUT # OF COMPLETE GENERATIONS - FORMAT IS F3.1')
0196     READ(5,201) SETS
0197 201   FORMAT(F3.1)
      C
      C --> EXECUTE FACE-CENTERED POINT GENERATION ROUTINE
0198 2001  CALL FACE
      C
      C ----> SET ELECTRODE ARRAY EQUAL TO FACE-CENTERED POINT
      C      GENERATION EXPAND ARRAY
0199     DO 1200 I = 1, ISIZE
0200     DO 1300 J = 1, JSIZE
0201     ELECTR(I,J) = EXPAND(I,J)
0202 1300  CONTINUE
0203 1200  CONTINUE
      C
      C --> ADJUST # OF POINTS BETW EACH GENERATED ROW & COLUMN POSITION
      C      RESULTING FROM FACE-CENTERED POINT GENERATION ROUTINE
      C      (APPROXIMATION ONLY)
0204     ISPACE = (ISPACE * (IROW - 1) / (ISIZE - 1))
      C
      C ----> SAVE THE ROW & COLUMN VALUES OF THE ORIGINAL ELECTRODE NET
0205     ITRW = IROW
0206     ITCOL = ICOL
      C
      C --> RESET # OF ROWS AND COLUMNS IN ELECTRODE ARRAY TO # OF ROWS
      C      AND COLUMNS IN EXPANDED ARRAY
0207     IROW = ISIZE
0208     ICOL = JSIZE
      C
      C ----> INDICATE WHICH INTERPOLATION ROUTINE IS TO BE PERFORMED
0209 1005  IF (INPUT .GT. 0 .AND. NPASS .GT. 0) GO TO 2100
0211     IF (ICHNGE .LT. 1) GO TO 2100
0213 1006  WRITE(7,1020)

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0214 1020 FORMAT(' INDICATE INTERPOLATION ROUTINE'/5X,' 1 = TERMINATE',
* 'CURRENT PGM'/5X,' 2 = BILINEAR'/5X,' 3 = INVERSE-SQUARE',
* 'RADIUS'/5X,' 4 = INVERSE RADIUS')
0215      READ(7,200) INTER
0216      IF (INTER .GE. 1 .AND. INTER .LE. 4) GO TO 7170
0218      WRITE(7,1023)
0219 1023 FORMAT(' INVALID INTERPOLATION SPECIFIED - TRY AGAIN?')
0220      GO TO 1006
C ----> SPECIFY MIN. RADIUS FACTOR FOR INVERSE & INVERSE SQUARE RADIUS
C      INTERPOLATION ROUTINES
0221 7170 IF (INTER .LT. 3) GO TO 1022
C - SMEAR = FRACTION BETWEEN 0 & .5, USED TO CALC. MIN.
C           RADIUS THAT ANY INTERPOLATION POINT IS TO ASSUME
C           FROM ANY ELECTRODE POSITION
0223      WRITE(7,7171)
0224 7171 FORMAT(' PLEASE INPUT MIN-NONZERO RADIUS FACTOR (F2.1)')
0225      READ(7,7172) SMEAR
0226 7172 FORMAT(F6.4)
0227      WRITE(7,7173) SMEAR
0228 7173 FORMAT(' SMEAR = ',F6.3)
C
C ----> DETERMINE MAX ROW & COLUMN DISPLAY VALUES
0229 1022 MAXROW = (ISPACE * (IROW - 1)) + IROW
0230      MAXCOL = (ISPACE * (ICOL - 1)) + ICOL
C
C ----> CHECK ON DIMENSIONS OF DISPLAY ARRAY TO BE WITHIN LIMITS
0231      IF (MAXROW .LE. 449) GO TO 1415
0233      WRITE (6,1410) MAXROW
0234 1410 FORMAT(' ROWS TO BE DISPLAYED = ',I3,' IS TOO LARGE AND',
* ' WILL BE RESET TO 449')
0235      MAXROW = 449
0236 1415 IF (MAXCOL .LE. 609) GO TO 1400
0238      WRITE(6,1420) MAXCOL
0239 1420 FORMAT(' COLUMNS TO BE DISPLAYED = ',I3,' IS TOO LARGE AND',
* ' WILL BE RESET TO 609')
0240      MAXCOL = 609
C
C ----> CALCULATE BEGINNING ROW AND COLUMN DISPLAY POSITIONS ----> CAUSE
C      DISPLAY TO BE CENTERED ON SCREEN
0241 1400 IROWB = (479 - MAXROW) / 2
0242      ICOLB = (639 - MAXCOL) / 2
C
C ----> CALL REQUESTED INTERPOLATION ROUTINES
0243 2100 IF (INTER .EQ. 1) STOP
0245      IF (INTER .EQ. 2) CALL INTERP(IROWB,ICOLB)
0247      IF (INTER .EQ. 3) CALL ISQRAD(IROWB,ICOLB)
0249      IF (INTER .EQ. 4) CALL INVRAD(IROWB,ICOLB)
C
C ----> COUNT # OF IMAGES DISPLAYED
0251      NPASS = NPASS + 1
C
C ----> RESET ROW & COLUMN VARIABLES TO THE ORIGINAL VALUES
0252      IF (IACE .LT. 1) GO TO 2101
0254      IROW = IROW

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0255      ICOL = ITCOL
C
C --> BEGIN PROCEDURE TO MAKE CHANGES IN CURRENT DATA
C      INPUT = 0      MANUAL OPERATION
C      INPUT = 1      SEMI-AUTOMATIC OPERATION (DISK EEG DATA)
0256 2101 IF (INPUT .LE. 0) GO TO 1607
C
C --> IPAUSE = 0      CONTINUOUS PGM. EXECUTION AFTER DISPLAY OUTPUT
C      IPAUSE = 1      PAUSE UNTIL INSTRUCTED TO CONTINUE
0258      IF (IPAUSE .LE. 0) GO TO 1832
0260 1611 WRITE(7,1609)
0261 1609 FORMAT(' OPERATOR, MAY I CONTINUE ?//4X,' -1 = 'TERMINATE ME//
      * 5X,' 0 = NO//5X,' 1 = YES')
0262      READ(7,200) IGO
0263      IF (IGO .GT. 0) GO TO 1832
0265      IF (IGO .GE. 0) GO TO 1611
0267      WRITE(7,1607)
0268 1607 FORMAT(' THE EEG POTENTIAL DISPLAY PGM. (      )',
      * ' HAS FINISHED')
0269      STOP
0270 1557 WRITE(7,1556)
0271 1556 FORMAT(' **** END OF FILE ****')
0272 1609 WRITE(7,1610)
0273 1610 FORMAT(' DO YOU WANT TO CONTINUE WITH THE CURRENT DISPLAY ?//
      * 5X,' 0 = NO//5X,' 1 = YES')
0274      READ(7,200) ICONT
0275      IF (ICONT .GT. 0) GO TO 1612
0277      WRITE(7,1613)
0278 1613 FORMAT(' DO YOU WANT TO RESTART THE ENTIRE PROGRAM//
      * 5X,' 0 = NO//5X,' 1 = YES')
0279      READ(7,200) ISTART
0280      IF (ISTART .GT. 0) GO TO 1
0282      WRITE(7,1607)
0283      STOP
0284 1612 WRITE(7,1600)
0285 1600 FORMAT(' ANY POTENTIALS TO BE CHANGED ?//5X,' 0 = NO'
      * '/5X,' 1 = YES')
0286      READ(7,200) ICHNGE
0287      IF (ICHNGE .EQ. 0) GO TO 2550
0289      WRITE(7,1650)
0290 1650 FORMAT(' INPUT FORMAT FOR I, J, CHANGE FOLLOWS// 12,12,F7.3')
0291 1900 READ(7,1700) I, J, CHANGE
0292 1700 FORMAT(12,12,F7.3)
0293      IF (I .LT. 1 .OR. J .LT. 1) GO TO 2400
0295      IF (I .GT. IROW .OR. J .GT. ICOL) GO TO 2200
0297      ELECTR(I,J) = CHANGE
0298      GO TO 1900
0299 2200 WRITE(7,2300)
0300 2300 FORMAT(' ERROR: # ROWS = ',12,' # COLUMNS = ',12//5X,
      * ' EITHER I = ',12,' OR J = ',12,
      * ' ARE TOO LARGE - IGNORING CHANGE, TRY AGAIN')
0301      GO TO 1900
0302 2400 WRITE(7,2500)
0303 2500 FORMAT(' POTENTIAL CHANGES COMPLETE')

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0304 2550 WRITE(7,2600)
0305 2600 FORMAT(' DO YOU WANT TO CHANGE THE INTERPOLATION ROUTINE ?'/
              *  ',5X,' 0 = NO',5X,' 1 = YES')
0306      READ(7,200) ICHANGE
0307      GO TO 1800
0308      STOP
0309      END
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0001      SUBROUTINE INTERP(IROWB,ICOLB)
0002      COMMON ERANGE(17), ELECTR(21,21), ISPACE, IROW,ICOL, MAXCOL,
*      NUMLEV, IDEBUG, MAXROW, INTVAL(400)
0003      DIMENSION TELECT(2,2)
0004      IF (IDEBUG .EQ. 2 .OR. IDEBUG .EQ. 3)
*      WRITE(6,123)
0006 123  FORMAT(' SUBROUTINE INTERP ENTERED')
0007      NSPACE = ISPACE + 1
0008      IBEGIN = 1
0009      ILAST = IROW - 1
0010      JLAST = ICOL - 1
C ***** SET THE ROW POSITION VALUES - ISTART, IEND
0011      ISTART = 0
0012      IEND = NSPACE
C
C  LOOP THRU THE SUBROUTINE ONE TIME FOR EACH ROW
C  KROW = CURRENT ROW BEING PROCESSED
C
0013      DO 22222 NUMROW = 1, MAXROW
0014      KROW = NUMROW - 1
0015      IRESET = 1
C
C --> DETERMINE WHICH SET OF 4 ADJACENT ELECTRODES CONTAIN THE CURRENT POINT
C ***** SET THE COLUMN POSITION VALUES - JSTART, JEND
0016      JSTART = 0
0017      JEND = NSPACE
0018      DO 100 1 = IBEGIN, ILAST
0019      IF (KROW .GE. ISTART .AND. KROW .LE. IEND) GO TO 200
0021      ISTART = IEND
0022      IEND = IEND + NSPACE
0023      IRESET = 1
0024 100  CONTINUE
0025      WRITE(7,1) IROW, ISTART, IEND, 1
0026 1      FORMAT(' UNABLE TO DETERMINE CORRECT ROW INTERVAL: ',/, 'IROW=',
*      '14,4X,' ISTART=',14,4X,' IEND=',14,4X,' I=',12,4X,' PGM END')
0027      STOP
C
C --> BEGIN LOOP CONTROLLED BY KTEMP - CURRENT COLUMN
C
0028 200  JBEGIN = 1
0029      IBEGIN = 1
0030      DO 300 KTEMP = 1, MAXCOL
0031      KCOL = KTEMP - 1
0032      DO 400 J = JBEGIN, JLAST
0033      IF (KCOL .GE. JSTART .AND. KCOL .LE. JEND) GO TO 500
0035      IRESET = 1
0036      JSTART = JEND
0037      JEND = JEND + NSPACE
0038 400  CONTINUE
0039      WRITE(7,2) KCOL, JSTART, JEND, J
0040 2      FORMAT(' UNABLE TO DETERMINE CORRECT COLUMN INTERVAL: ',/,
*      ' KCOL=',14,4X,' JSTART=',14,4X,' JEND=',14,4X,' J=',12,4X,
*      ' PGM END')
0041      STOP

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0042 500  IF (IRESET .NE. 1) GO TO 600
0044      JBEGIN = J
      C
      C --> SET THE VALUES OF THE TEMPORARY ELECTRODE ARRAY
      C
0045      J1 = J + 1
0046      I1 = 1 + 1
0047      TELECT(1,1) = ELECTR(1,J)
0048      TELECT(1,2) = ELECTR(1,J1)
0049      TELECT(2,1) = ELECTR(11,J)
0050      TELECT(2,2) = ELECTR(11,J1)
0051      IRESET = 0
0052      IF (1DEBUD .EQ. 2 .OR. 1DEBUD .EQ. 3)
      *WRITE(6,66) TELECT(1,1),TELECT(1,2),TELECT(2,1),TELECT(2,2)
0054 66  FORMAT(' TELECT(1,1)=' ,F7.3, ' TELECT(1,2)=' ,F7.3,
      * ' TELECT(2,1)=' ,F7.3, ' TELECT(2,2)=' ,F7.3)
      C
      C --> DETERMINE THE RELATIVE POSITION OF THE CURRENT POINT AND THE
      C ASSOCIATED POTENTIAL CALCULATION SCHEME
      C
      C ***** DETERMINE IF CURRENT POINT IS STRICTLY WITHIN PERIMETER
      C OF TEMPORARY ARRAY - BRANCH TO 1200 IF YES
      C
0055 600  IF (KROW .GT. ISTART .AND. KROW .LT. IEND .AND.
      * KCOL .GT. JSTART .AND. KCOL .LT. JEND) GO TO 1010
0057      IVAL = 1
      C ***** DETERMINE WHERE THE CURRENT POINT IS LOCATED ON
      C PERIMETER OF TEMPORARY ARRAY - IF NOT DETERMINED, THEN
      C OUTPUT ERROR MESSAGE AND TERMINATE PGM.
      C
0058      ITEMP5 = ISTART
0059      JTEMP5 = JSTART
0060      ITEMP6 = IEND
0061      JTEMP6 = JEND
0062      JTEMP = JSTART
0063      DO 700 I1 = 1, 2
0064          IF (KROW .EQ. ITEMP5) IVAL = 2
0065          IF (KCOL .EQ. JTEMP) IVAL = 3
0066          DO 800 IJ = 1, 2
0067              IF (KROW .EQ. ITEMP5 .AND. KCOL .EQ. JTEMP5) GO TO 4000
0071              JTEMP5 = JTEMP6
0072 800  CONTINUE
0073          JTEMP5 = JTEMP
0074          JTEMP6 = JTEMP6
0075          ITEMP5 = ITEMP6
0076          GO TO (700, 1000, 2000) , IVAL
0077 700  CONTINUE
0078      WRITE(6,7) KROW, KCOL, ITEMP5, ITEMP6, JTEMP5, JTEMP6
0079 7  FORMAT(' ERROR: CANNOT DETERMINE LOCATION OF CURRENT POINT' /
      * ' KROW = ',I3,' , KCOL = ',I3,' , ITEMP5 = ',I3,' , ITEMP6 = ',
      * ' I3,' , JTEMP5 = ',I3,' , JTEMP6 = ',I3)
0080      STOP
      C
      C --> THE FOLLOWING IS EXECUTED WHEN THE CURRENT POINT IS ON THE

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      C      INTERIOR OF THE TEMPORARY ARRAY
      C
0081 1010  X1 = KROW
0082 1100  IF (X1 .LE. NSPACE) GO TO 900
0084       X1 = X1 - NSPACE
0085       GO TO 1100
0086 900   Y1 = KCOL
0087 1300  IF (Y1 .LE. NSPACE) GO TO 1200
0089       Y1 = Y1 - NSPACE
0090       GO TO 1300
0091 1200  X1DX2 = X1 / NSPACE
0092       Y1DY2 = Y1 / NSPACE
0093       XMULTY = X1DX2 * Y1DY2
0094       EPOTEN = TELECT(1,1) * (1 - X1DX2 - Y1DY2 + XMULTY)
      *          + TELECT(1,2) * (Y1DY2 - XMULTY)
      *          + TELECT(2,1) * (X1DX2 - XMULTY)
      *          + TELECT(2,2) * XMULTY
0095       GO TO 9000
      C
      C --> THE FOLLOWING CODE IS EXECUTED WHEN THE CURRENT POINT IS ON THE
      C      FIRST OR LAST ROW OF THE TEMPORARY ARRAY
      C
0096 1000  Y1 = KCOL
0097 1500  IF (Y1 .LT. NSPACE) GO TO 1400
0099       Y1 = Y1 - NSPACE
0100       GO TO 1500
0101 1400  EPOTEN = TELECT(11,1)
      *          + ((TELECT(11,2) - TELECT(11,1)) * (Y1 / NSPACE))
0102       GO TO 9000
      C
      C --> THE FOLLOWING CODE IS EXECUTED WHEN THE CURRENT POINT IS ON THE
      C      FIRST OR LAST COLUMN OF THE TEMPORARY ARRAY
      C
0103 2000  X1 = KROW
0104 1700  IF (X1 .LT. NSPACE) GO TO 1600
0106       X1 = X1 - NSPACE
0107       GO TO 1700
0108 1600  EPOTEN = TELECT(1,11)
      *          + ((TELECT(2,11) - TELECT(1,11)) * (X1 / NSPACE))
0109       GO TO 9000
      C
      C --> THE FOLLOWING CODE IS EXECUTED ONLY WHEN THE CURRENT POINT IS
      C      LOCATED AT ONE OF THE TEMPORARY ELECTRODE POSITIONS
      C
0110 4000  EPOTEN = TELECT(11,11)
      C
      C --> THIS CODE EQUATES THE CURRENT POINT POTENTIAL VALUE TO THE
      C      CORRESPONDING GRAY LEVEL VALUE
      C
0111 2000  DO 1800 IM = 1, NUMLEV
0112       IN = IM + 1
0113       IF (EPOTEN .GE. ERANGE(IM) .AND. EPOTEN .LT. ERANGE(IN))
      *
0115 1800  CONTINUE                                GO TO 1900

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0116      IM = NUMLEV
0117      IF (EPOTEN .GE. ERANGE(IN) .AND. EPOTEN .LT.
          * ERANGE(IN) + .1) GO TO 1200
0119      IM = 0
0120      IF (IDEBUG .EQ. 1 .OR. IDEBUG .EQ. 3)
          * WRITE(7,3) EPOTEN, IVAL
0122  3      FORMAT(' UNABLE TO DETERMINE A VALID GRAY LEVEL FOR EPOTEN = ',
          *      ,E20.7,' , IVAL = ',I3,' ; PGM END')
0123  1200    INTVAL(KTEMP) = IM
0124      IF (IDEBUG .EQ. 2 .OR. IDEBUG .EQ. 3)
          *WRITE(6,60) KTEMP,INTVAL(KTEMP), EPOTEN, KCOL, KROW
0126  60      FORMAT(' INTVAL(',I4,') = ',I4, 5X,'EPOTEN = ',F7.3,
          * 5X,' KCOL=',I3,5X,' KROW=',I3)
0127  300    CONTINUE
          C
          C --> INSERT 99 AT END OF CALCULATED GRAY LEVELS TO INDICATE END OF DATA
0128      INTVAL(KTEMP) = 99
0129      IF (IDEBUG .EQ. 2 .OR. IDEBUG .EQ. 3)
          * WRITE(6,61) KROW, MAXCOL, IROWB, ICOLB
0131  61      FORMAT(' KROW = ',I3,5X,'MAXCOL = ',I3,5X,'IROWB = ',I3,
          * 5X,'ICOLB = ',I3)
0132      CALL DISPLY(KROW,MAXCOL,IROWB,ICOLB,INTVAL)
0133  99999   CONTINUE
0134      RETURN
0135      END

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0001      SUBROUTINE ISQRAD(IROWB,ICOLB)
0002      COMMON ERANGE(17), ELECTR(21,21),ISPACE, IROW, ICOL, MAXCOL,
      * NUMLEV, IDEBUG, MAXROW, INTVAL(400)
0003      COMMON /BLOCK3/EVAL(400), SHEAR
      C      WRITE(7,123)
      C123 FORMAT(' SUBROUTINE ISQRAD ENTERED')
      C
      C ----> INVERSE-SQUARE RADIUS INTERPOLATION ROUTINE
      C
      C      EACH EXECUTION OF THIS ROUTINE COMPUTES THE INTERPOLATION
      C      VALUE FOR EVERY POINT FOR AN ENTIRE LINE. THE DISPLAY IS
      C      CREATED ONE LINE AT A TIME AFTER EACH IS COMPUTED.
      C
      C --> DISTANCE BETWEEN POINTS IS RELATIVE TO INPUT SCALE VALUE 'SCALE'
      C
      C *** VARIABLES:
      C      YDIST - VERTICLE DISTANCE COMPONENT
      C      XDIST - HORIZONTAL DISTANCE COMPONENT
      C      IPOINT -- CURRENT ROW NUMBER
      C      JPOINT - CURRENT COLUMN NUMBER
      C      MAXCOL - MAX. NUMBER ELEMENTS / ROW
      C      EVAL(*) - INTERPOLATED VALUES
      C      SCALE - DISTANCE SCALE FACTOR FROM POINT TO POINT
      C
0004      IREPLC = 1
0005      IREROW = 1
0006      INCREM = ISPACE + 1
0007      RSMINV = 1 / ((INCREM * SHEAR) ** 2)
0008      DO 100 IPOINT = 1, MAXROW
      C
      C ----> ZERO FILL POTENTIAL ARRAY EVAL(400)
0009      DO 10 I = 1, MAXCOL
0010          EVAL(I) = 0.
0011          INTVAL(I) = 0
0012      10 CONTINUE
0013      DO 200 JPOINT = 1, MAXCOL
0014          IPOS = 1
0015          WT = 0.0
0016          DO 300 I = 1, MAXROW, INCREM
0017              JPOS = 1
      C
      C --> CALCULATE X, Y DISTANCES
0018      DO 400 J = 1, MAXCOL, INCREM
      C
      C ----> TEST FOR 'ELECTRODE' NOT TO BE INCLUDED IN CALCULATIONS -
      C      RESULTING FROM FACE SUBROUTINE
0019      IF (ELECTR(IPOS,JPOS) .GT. 999.) GO TO 350
      C
      C --> COMPUTE DISTANCE FROM INTERPOLATION POINT TO CURRENT
      C      ELECTRODE
0021      YDIST = FLOAT(IPOINT - I)
0022      XDIST = FLOAT(JPOINT - J)
0023      IF (YDIST .EQ. 0. .AND. XDIST .EQ. 0.) YDIST = 1
      C

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      C ----> COMPUTE INTERPOLATION VALUE
0025      RSQINV = 1 / (YDIST ** 2 + XDIST ** 2)
0026      IF (RSMINV .LT. RSQINV) RSQINV = RSMINV
0028      WT = WT + RSQINV
0029      EVAL(JPOINT) = EVAL(JPOINT) + ELECTR(IPOS,JPOS) *
      *      RSQINV
0030      IF (IDEBUG .EQ. 2 .OR. IDEBUG .EQ. 3)
      *      WRITE(6,1001) RSQINV, IPOS, JPOS, MAXROW, MAXCOL, INCREM,
      *      IPOINT, JPOINT, EVAL(JPOINT), 1, J, ELECTR(IPOS,JPOS), WT
0032 350      JPOS = JPOS + 1
0033 400      CONTINUE
0034      IPOS = IPOS + 1
0035 300      CONTINUE
0036      EVAL(JPOINT) = EVAL(JPOINT) / WT
0037 1001  FORMAT(' RSQINV = ',F7.2,' IPOS = ',I2,' JPOS = ',I2,
      *      MAXROW = ',I3,' MAXCOL = ',I3,' INCREM = ',I3,
      *      IPOINT = ',I3,' JPOINT = ',I3,' EVAL(JPOINT) = ',F7.3/
      *      I = ',I3,' J = ',I3,' ELECTR(IPOS,JPOS) = ',F7.3,
      *      WT = ',F7.5)
0038 200      CONTINUE
0039      IF (IDEBUG .EQ. 2 .OR. IDEBUG .EQ. 3)
      *      WRITE(6,1010) JPOINT, IPOINT, (EVAL(I),I=1,MAXCOL)
0041 1010  FORMAT(' JPOINT = ',I3,5X,'EVAL(*) FOR ROW #',I3/23(' ',I3F7.3/))
      C
      C ----> AFTER COMPUTING VALUES FOR EACH ROW, CHECK TO SEE IF ORIGINAL
      C      ELECTRODE VALUES SHOULD BE INSERTED - IF SO, THEN DO AND
      C      INCREMENT IREPLC
0042      IF (IPOINT .NE. IREPLC) GO TO 450
0044      JK = 1
0045      DO 475 J = 1, MAXCOL, INCREM
0046      EVAL(J) = ELECTR(IREROW,JK)
0047      JK = JK + 1
0048 475      CONTINUE
0049      IREPLC = IREPLC + INCREM
0050      IREROW = IREROW + 1
      C
      C ----> AFTER EACH ROW IS COMPLETED - SET EACH CORRESPONDING POSITION IN
      C      INTVAL EQUAL TO THE ASSOCIATED GRAY LEVEL VALUE
0051 450      DO 500 I = 1, MAXCOL
0052      DO 600 IM = 1, NUMLEV
0053      IN = IM + 1
0054      IF (EVAL(I) .GE. ERANGE(IM) .AND. EVAL(I) .LT.
      *      ERANGE(IN)) GO TO 700
0056 600      CONTINUE
0057      IF (EVAL(I) .GE. ERANGE(IN) .AND. EVAL(I) .LT. (ERANGE(IN) + 1.))
      *      GO TO 700
0059      IF (EVAL(I) .LT. ERANGE(1)) INTVAL(I) = 1
0061      IF (EVAL(I) .GT. ERANGE(IN)) INTVAL(I) = NUMLEV
0063      IM = 0
0064      IF (IDEBUG .EQ. 2 .OR. IDEBUG .EQ. 3)
      *      WRITE(6,800) I, EVAL(I), IPOINT
0066 800      FORMAT(' UNABLE TO DETERMINE EVAL(',I3,') = ',F7.3,
      *      ' IN ROW ',I3)
0067      GO TO 500

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0068 700    INTVAL(1) = 1M
0069 500    CONTINUE
0070        INTVAL(JPOINT) = 99
0071        IF (IDEDUC .EQ. 2 .OR. IDEBUG .EQ. 3)
*        WRITE(6,1000) IPPOINT, (EVAL(K), INTVAL(K), K=1,MAXCOL)
0073 1000    FORMAT(' EVAL(*), INTVAL(*) FOR ROW #',I3/
*        250(' ',F7.3,5X,I2/))
C        WRITE(7,124)
C124        FORMAT(' 100RAD EXIT, ENTERING DISPLY')
0074        CALL DISPLY(IPPOINT,MAXCOL,IROWB,ICOLB,INTVAL)
0075 100    CONTINUE
0076        RETURN
0077        END
```

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0001      SUBROUTINE FACE
0002      COMMON ERANGE(17), ELECTR(21,21), ISPACE, IROW, ICOL,
      *MAXCOL, NUMLEV, IDEBUG, MAXROW, INTVAL(400)
0003      COMMON /BLOCK1/EXPAND(21,21), ISETS, SETS, ISIZE, JSIZE, JDEBUG
0004      LOGICAL BTWEN
0005      WRITE(7,123)
0006      123      FORMAT(' SUBROUTINE FACE ENTERED')
      C
      C SUBROUTINE FACE PERFORMS THE FACE-CENTERED POINT GENERATION, CONSISTS OF
      C 2 OPERATIONS: 1-THE VALUE AT THE CENTER OF EACH SET OF 4 ADJACENT
      C ORIGINAL POINTS IS CALCULATED - SUM VALUE OF EACH POINT
      C & DIVIDE BY 4. 2-THE POINTS ON BOTH, ABOVE & BELOW OF EACH NEW POINT
      C ARE ALSO CALCULATED. THE RESULT IS AN ARRAY WITH (N-1) ADDITIONAL
      C ROWS & COLUMNS. THE PROCEDURE COULD BE PERFORMED AS MANY TIMES
      C AS DESIRED - UNTIL THE REQUIRED DENSITY IS ACHIEVED.
      C
      C INPUT TO THE ROUTINE:
      C ELECTR(21,21) - ARRAY CONTAINING THE ORIGINAL ELECTRODE POINT VALUES
      C IROW - # OF ROWS IN THE ORIGINAL ELECTRODE ARRAY
      C ICOL - # OF COLUMNS IN THE ORIGINAL ELECTRODE ARRAY
      C ISETS - # OF TIMES THE PROCEDURE IS TO BE PERFORMED
      C
      C OUTPUT FROM THE ROUTINE:
      C EXPAND(*,*) - THE EXPANDED (HIGHER DENSITY) ARRAY
      C CONTAINING ALL THE ORIGINAL AND CALCULATED POINT VALUES
      C
      C OTHER IMPORTANT VARIABLES:
      C ISKIP - THE # OF POINTS INSERTED BETWEEN EACH 2 ROW OR COLUMN
      C POINTS
      C NTIMES - # OF TIMES THE PROCEDURE IS EXECUTED
      C
      C ----> REMAINING VARIABLES ARE DEFINED IN THE SECTIONS THEY APPEAR
      C
      C ***** CURRENT MAXIMUM # OF GENERATIONS ALLOWED IS 2 FOR AN ORIGINAL 6X6
      C ELECTRODE ARRAY. IF RESULTING EXPANDED ARRAY IS LARGER THAN ALLOWED
      C A WARNING IS OUTPUT AND A REDUCTION OF ISETS IS PERFORMED
      C UNTIL AN ACCEPTABLE VALUE IS FOUND. THE OPERATOR IS
      C INFORMED OF THE NEW VALUE OF ISETS.
      C
      C --> SET DEBUG FLAG
0007      ISETS = SETS + .5
0008      GO TO 400
0009      300      WRITE(7,500) SETS
0010      500      FORMAT(' THE # OF GENERATIONS, ', F3.1, ', IS TOO LARGE',
      *' AND WILL BE REDUCED BY 1')
0011      ISETS = ISETS - 1
0012      SETS = SETS - 1.
0013      400      ISKIP = 0
      C ----> COMPUTE TOTAL # OF ELEMENTS INSERTED BTWN POINTS IN ORIGINAL ARRAY
0014      DO 600 K = 1, ISETS
0015      ISKIP = (2 * ISKIP) + 1
0016      600      CONTINUE

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0017      IPLUS = ISKIP + 1
C -----> DETERMINE IF EXPANSION ARRAY IS LARGER THAN ALLOWED
C      ISIZE - # OF RESULTING ROWS IN EXPANDED ARRAY
C      JSIZE - # OF RESULTING COLUMNS IN EXPANDED ARRAY
C
0018      ISIZE = ((IROW - 1) * ISKIP) + IROW
0019      JSIZE = ((ICOL - 1) * ISKIP) + ICOL
0020      IF (ISIZE .GT. 21 .OR. JSIZE .GT. 21) GO TO 300
C -----> DIMENSIONS OF EXPANDED ARRAY ARE ACCEPTABLE
0022      WRITE(7,610) SETS
0023 610   FORMAT(' THE # OF GENERATIONS PERFORMED IS ',F3.1)
C
C -----> ZERO FILL EXPAND(*,*)
C
0024      DO 606 I = 1, 21
0025      DO 607 J = 1, 21
0026          EXPAND(I,J) = 999.99
0027 607   CONTINUE
0028 606   CONTINUE
C
C -----> POSITION ORIGINAL ARRAY IN THE EXPANDED ARRAY
C      IK,JK -- ROW, COLUMN (RESPECTIVELY) POSITIONS IN THE EXPANDED ARRAY
C      I, J -- ORIGINAL ARRAY ROW, COL VALUES PLACED AT IK,JK IN
C              EXPANDED ARRAY
C      IPLUS - INCREMENT FROM POINT TO POINT IN EXPANDED ARRAY
0029      IK = 1
0030      DO 700 I = 1, IROW
0031      JK = 1
0032      DO 800 J = 1, ICOL
0033          EXPAND(IK,JK) = ELECTR(I,J)
0034          JK = JK + IPLUS
0035 800   CONTINUE
0036      IK = IK + IPLUS
0037 700   CONTINUE
0038      IF (IDEBUG .NE. 2 .AND. IDEBUG .NE. 3) GO TO 720
0040      WRITE(6,703)
0041 703   FORMAT(' CURRENT EXPAND ARRAY')
0042      DO 701 ITEST = 1, 21
0043          WRITE(6,702) (EXPAND(ITEST,JTEST),JTEST=1,21)
0044 702   FORMAT(' ',21(F5.2,1X))
0045 701   CONTINUE
C
C -----> COMPUTE AND POSITION THE CENTER OF EACH SET OF 4 POINTS
C      INEW - ROW POSITION OF CENTER POINT
C      JNEW - COLUMN POSITION OF CENTER POINT
C      IEND - # OF ROW CENTER POINTS TO BE CALCULATED (1 LESS
C              THAN # CALCULATED IN PREVIOUS GENERATION)
C      JEND - # OF COLUMN CENTER POINTS TO BE
C              CALCULATED (1 LESS THAN # CALCULATED IN
C              PREVIOUS GENERATION)
0046 720   IEND = ISIZE - IPLUS
0047      JEND = JSIZE - IPLUS
0048      DO 99999 NTIMES = 1, ISETS
0049      IK = 1

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0050      DO 900  I = 1, IEND, IPLUS
0051          JK = 1
0052          IKLAST = IK + IPLUS
0053          DO 1000 J = 1, JEND, IPLUS
0054              JKLAST = JK + IPLUS
0055              INEW = (IK + IKLAST) / 2
0056              JNEW = (JK + JKLAST) / 2
0057              EXPAND(INEW, JNEW) = (EXPAND(IK, JK) + EXPAND(IK, JKLAST)
*              + EXPAND(IKLAST, JK) + EXPAND(IKLAST, JKLAST)) / 4
0058          JK = JKLAST
0059      1000  CONTINUE
0060          IK = IKLAST
0061      900  CONTINUE
0062          IF (IDEBUG .NE. 2 .AND. IDEBUG .NE. 3) GO TO 920
0064          WRITE(6,903)
0065      903  FORMAT(' CENTER POINTS  EXPAND ARRAY')
0066          DO 901 ITEST = 1, 21
0067              WRITE(6,902) (EXPAND(ITEST, JTEST), JTEST=1, 21)
0068      902  FORMAT(' ', 21(F5.2, 1X))
0069      901  CONTINUE
0070      C
0071      C ---> TEST FOR LAST GENERATION TO BE ONLY FOR CENTER OF EACH SET OF 4
0072      C      ADJACENT 'ELECTRODES'
0073      SETS = SETS - 1.0
0074      IF (SETS .LT. 0.) RETURN
0075      C
0076      C **** COMPUTE THE REMAINING ELEMENTS OF EXPAND IN ORDER TO COMPLETELY FILL
0077      C      THE ARRAY
0078      C
0079      C -----> NEWINC - INCREMENT REQUIRED TO GET FROM CURRENT CALCULATED ELEMENT
0080      C      TO THE NEXT
0081      920  NEWINC = IK - INEW
0082      IF (NEWINC .GT. 0) GO TO 1100
0083      IF (IDEBUG .EQ. 1 .OR. IDEBUG .EQ. 3) WRITE(7,1200) NEWINC
0084      1200  FORMAT(' NEWINC=', I2, ' AND PGM IS TRYING TO EXECUTE --- STOP')
0085      STOP
0086      C -----> SECTION 1: COMPUTE THE PERIMETER VALUES - ONLY 3 NEIGHBORING
0087      C      VALUES ARE USED INSTEAD OF THE USUAL 4
0088      1100  INCREM = 2 * NEWINC
0089      C -----> COMPUTE FIRST AND LAST ROW PERIMETER VALUES
0090      INEXT = 1 + NEWINC
0091      IPREV = ISIZE - NEWINC
0092      JBEGIN = 1 + NEWINC
0093      IEND = ISIZE - NEWINC
0094      JEND = JSIZE - NEWINC
0095      DO 1600 JVAL = JBEGIN, JEND, INCREM
0096          JPREV = JVAL - NEWINC
0097          JNEXT = JVAL + NEWINC
0098      C **** FIRST ROW
0099      EXPAND(1, JVAL) = (EXPAND(1, JPREV) + EXPAND(1, JNEXT) +
*      EXPAND(INEXT, JVAL)) / 3
0100      C **** LAST ROW
0101      EXPAND(ISIZE, JVAL) = (EXPAND(ISIZE, JPREV) + EXPAND(ISIZE, JNEXT)
*      + EXPAND(IPREV, JVAL)) / 3

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0091 1400 CONTINUE
      C
      C ----> COMPUTE FIRST AND LAST COLUMN PERIMETER VALUES
0092      JNEXT = 1 + NEWINC
0093      JPREV = JSIZE - NEWINC
0094      IBEGIN = 1 + NEWINC
0095      DO 1500 IVAL = IBEGIN, IEND, INCREM
0096      IPREV = IVAL - NEWINC
0097      INEXT = IVAL + NEWINC
      C **** FIRST COLUMN
0098      EXPAND(IVAL,1) = (EXPAND(IPREV,1) + EXPAND(INEXT,1) +
      *                      EXPAND(IVAL,JNEXT)) / 3
      C **** LAST COLUMN
0099      EXPAND(IVAL,JSIZE) = (EXPAND(IPREV,JSIZE) + EXPAND(INEXT,JSIZE)
      *                      + EXPAND(IVAL,JPREV)) / 3
0100 1500 CONTINUE
0101      IF (IDEBUG .NE. 2 .AND. IDEBUG .NE. 3) GO TO 1550
0103      WRITE(6,1303)
0104 1303 FORMAT(' PERIMETER VALUES  EXPAND ARRAY')
0105      DO 1301 ITEST = 1, 21
0106      WRITE(6,1302) (EXPAND(ITEST,JTEST),JTEST=1,21)
0107 1302 FORMAT(' ',21(F5.2,1X))
0108 1301 CONTINUE
      C ----> SECTION 2: COMPUTE ALL THE SECOND LEVEL INTERNAL POINTS
      C **** NO INTERNAL POINTS TO CALCULATE WHEN ORIGINAL ARRAY
      C          HAS ONLY 2 COLUMNS AND NTIMES = 1
0109 1550 IF (ICOL .EQ. 2 .AND. NTIMES .EQ. 1) GO TO 2200
0111      BETWEN = .TRUE.
0112      IVAL = IK - NEWINC
0113      JVAL = JK - NEWINC
0114      IPOSIT = NEWINC + 1
      C ----> EVERY TIME THROUGH THE ROUTINE THE BEGINNING COLUMN VALUE
      C          IS RESET, DEPENDING ON THE VALUE OF BETWEN (TRUE OR FALSE)
0115      DO 1800 IVAL = IPOSIT, IVAL, NEWINC
0116      INEXT = IVAL + NEWINC
0117      IPREV = IVAL - NEWINC
      C ----> SET VALUE OF JSTART DEPENDING UPON BETWEN (TRUE OR FALSE)
0118      IF (.NOT. BETWEN) GO TO 1900
0120      JSTART = (2 * NEWINC) + 1
0121      BETWEN = .FALSE.
0122      GO TO 2000
0123 1900 JSTART = NEWINC + 1
0124      BETWEN = .TRUE.
0125 2000 DO 2100 JVAL = JSTART, JVAL, INCREM
0126      JPREV = JVAL - NEWINC
0127      JNEXT = JVAL + NEWINC
0128      EXPAND(IVAL,JVAL) = (EXPAND(IVAL,JPREV) + EXPAND(IVAL,JNEXT)
      *                      + EXPAND(IPREV,JVAL) + EXPAND(INEXT,JVAL)) / 4.
0129 2100 CONTINUE
0130 1800 CONTINUE
0131 2200 IPLUS = IPLUS / 2
0132      IF (IDEBUG .NE. 2 .AND. IDEBUG .NE. 3) GO TO 1820
0134      WRITE(6,1303) NTIMES
0135 1803 FORMAT(' GENERATION ',12,' COMPLETE  EXPAND ARRAY')

```

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```
0136            DO 1801 ITEST = 1, 21
0137            WRITE(6,1802) (EXPAND(ITEST,JTEST),JTEST=1,21)
0138            1802    FORMAT(' ',21(F5.2,1X))
0139            1801    CONTINUE
0140            1820    IEND = ISIZE - 1PLUS
0141            JEND = JSIZE - 1PLUS
0142            99999    CONTINUE
0143            RETURN
0144            END
```

```

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0001      SUBROUTINE INVRAD(IROWB,ICOLB)
0002      COMMON CRANGE(17), ELECTR(21,21),ISPACE, IROW, ICOL, MAXCOL,
      * NUMLEV, IDEBUG, MAXROW, INTVAL(400)
0003      COMMON /BLOCK3/EVAL(400), SMEAR
      C      WRITE(7,123)
      C123 FORMAT(' SUBROUTINE INVRAD ENTERED')
      C
      C ----> INVERSE-SQUARE RADIUS INTERPOLATION ROUTINE
      C
      C      EACH EXECUTION OF THIS ROUTINE COMPUTES THE INTERPOLATION
      C      VALUE FOR EVERY POINT FOR AN ENTIRE LINE.  THE DISPLAY IS
      C      CREATED ONE LINE AT A TIME AFTER EACH IS COMPUTED.
      C
      C --> DISTANCE BETWEEN POINTS IS RELATIVE TO INPUT SCALE VALUE 'SCALE'
      C
      C *** VARIABLES:
      C      YDIST - VERTICLE DISTANCE COMPONENT
      C      XDIST - HORIZONTAL DISTANCE COMPONENT
      C      IPGINT - CURRENT ROW NUMBER
      C      JPOINT - CURRENT COLUMN NUMBER
      C      MAXCOL - MAX. NUMBER ELEMENTS / ROW
      C      EVAL(*) - INTERPOLATED VALUES
      C      SCALE - DISTANCE SCALE FACTOR FROM POINT TO POINT
      C
0004      IREPLC = 1
0005      IRRROW = 1
0006      INCREM = ISPACE + 1
0007      RINVMX = 1 / (INCREM * SMEAR)
0008      DO 100 IPGINT = 1, MAXROW
      C
      C ----> ZERO FILL POTENTIAL ARRAY EVAL(400)
0009      DO 10 I = 1, MAXCOL
0010          EVAL(I) = 0.
0011          INTVAL(I) = 0
0012      10 CONTINUE
0013      DO 200 JPOINT = 1, MAXCOL
0014          IPGOS = 1
0015          WT = 0.0
0016          DO 300 I = 1, MAXROW, INCREM
0017              JPOS = 1
      C
      C --> CALCULATE X, Y DISTANCES
0018      DO 400 J = 1, MAXCOL, INCREM
      C
      C ----> TEST FOR CURRENT 'ELECTRODE' NOT TO BE INCLUDED IN CALCULATION -
      C      RESULTING FROM FACE SUBROUTINE
0019      IF (ELECTR(IPGOS,JPOS) .GT. 999.) GO TO 350
      C
      C --> COMPUTE DISTANCE FROM INTERPOLATION POINT TO CURRENT
      C      ELECTRODE
0021          YDIST = FLOAT(IPGINT - I)
0022          XDIST = FLOAT(JPOINT - J)
0023          IF (YDIST .EQ. 0. .AND. XDIST .EQ. 0.) YDIST = 1
      C

```

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      C ----> COMPUTE INTERPOLATION VALUE
0025      RADINV = 1 / SORT(YDIST ** 2 + XDIST ** 2)
0026      IF (RINVMX .LT. RADINV) RADINV = RINVMX
0026      WT = WT + RADINV
0027      EVAL(JPOINT) = EVAL(JPOINT) + ELECTR(IPOS,JPOS) *
      *      RADINV
0030      IF (IDEBUG .EQ. 2 .OR. IDEBUG .EQ. 3)
      *      WRITE(6,1001) RADINV, IPOS, JPOS, MAXROW, MAXCOL, INCREM,
      *      IPPOINT, JPOINT, EVAL(JPOINT), 1, J, ELECTR(IPOS,JPOS), WT
0032 350      JPOS = JPOS + 1
0033 400      CONTINUE
0034      IPPOS = IPPOS + 1
0035 300      CONTINUE
0036      EVAL(JPOINT) = EVAL(JPOINT) / WT
0037 1001  FORMAT(' RADINV = ',F7.2,' IPPOS = ',12,' JPOS = ',12,
      *      ' MAXROW = ',13,' MAXCOL = ',13,' INCREM = ',13,
      *      ' IPPOINT = ',13,' JPOINT = ',13,' EVAL(JPOINT) = ',F7.3/
      *      ' 1 = ',13,' J = ',13,' ELECTR(IPOS,JPOS) = ',F7.3,
      *      ' WT = ',F7.5)
0038 200      CONTINUE
0039      IF (IDEBUG .EQ. 2 .OR. IDEBUG .EQ. 3)
      *      WRITE(6,1010) JPOINT, IPPOINT, (EVAL(I),I=1,MAXCOL)
0041 1010  FORMAT(' JPOINT = ',13,5X,' EVAL(*) FOR ROW #',13/23(' ',18F7.3/))
      C
      C ----> AFTER COMPUTING VALUES FOR EACH ROW, CHECK TO SEE IF ORIGINAL
      C      ELECTRODE VALUES SHOULD BE INSERTED - IF SO, THEN DO AND
      C      INCREMENT IREPLC
0042      IF (IPPOINT .NE. IREPLC) GO TO 450
0044      JK = 1
0045      DO 475 J = 1, MAXCOL, INCREM
0046      EVAL(J) = ELECTR(IREROW,JK)
0047      JK = JK + 1
0048 475      CONTINUE
0049      IREPLC = IREPLC + INCREM
0050      IREROW = IREROW + 1
      C
      C ----> AFTER EACH ROW IS COMPLETED - SET EACH CORRESPONDING POSITION IN
      C      INTVAL EQUAL TO THE ASSOCIATED GRAY LEVEL VALUE
0051 450      DO 500 I = 1, MAXCOL
0052      DO 600 IM = 1, NUMLEV
0053      IN = IM + 1
0054      IF (EVAL(I) .GE. ERANGE(IM) .AND. EVAL(I) .LT.
      *      ERANGE(IN)) GO TO 700
0056 600      CONTINUE
0057      IF (EVAL(I) .GE. ERANGE(IN) .AND. EVAL(I) .LE. (ERANGE(IN) + 1.))
      *      GO TO 700
0059      IF (EVAL(I) .LT. ERANGE(1)) INTVAL(I) = 1
0061      IF (EVAL(I) .GT. ERANGE(IN)) INTVAL(I) = NUMLEV
0063      IM = 0
0064      IF (IDEBUG .EQ. 2 .OR. IDEBUG .EQ. 3)
      *      WRITE(6,800) I, EVAL(I), IPPOINT
0066 800      FORMAT(' UNABLE TO DETERMINE EVAL(',13,') = ',F7.3,
      *      ' IN ROW ',13)
0067      GO TO 500

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0068 700      INTVAL(I) = 1M
0069 500      CONTINUE
0070          INTVAL(JPOINT) = 99
0071          IF (IDEBUG .EQ. 2 .OR. IDEBUG .EQ. 3)
*      WRITE(6,1000) IPPOINT, (EVAL(K), INTVAL(K), K=1,MAXCOL)
0073 1000      FORMAT(' EVAL(*), INTVAL(*) FOR ROW #',I3/
*      250(' ',F7.3,5X,I2/))
C      WRITE(7,124)
0074 C124      FORMAT(' INVRAD EXIT, ENTERING DISPLY')
CALL DISPLY(IPPOINT,MAXCOL,IROWB,ICOLB,INTVAL)
0075 100      CONTINUE
0076          RETURN
0077          END
```

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```

1          .MCALL  .V2. .PRINT. .REGDEF
2          .GLOBL  DISPLY
3          ; ***** DEFINE DISPLAYINSTRUCTIONS *****
4          ;
5          164000 ICS      = 164000          ; CONTROL & STATUS FOR VIDEO DISPLAY
6          164002 IWC      = 164002          ; WORD COUNT IN INSTRUCTION BUFFER
7          164004 ICA      = 164004          ; CORE ADDRESS OF DISPLAY INSTRUCTIONS
8          024000 LX1      = 24000           ; LOAD FIRST X VALUE
9          004000 LY1      = 4000            ; LOAD FIRST Y VALUE
10         044000 LCA      = 44000           ; LOAD CHANNEL ADDRESS
11         016000 EXF      = 16000           ; BLOCK TRANSFER OF DISPLAY DATA
12         000100 BLACK    = 100             ; BLACK BACKGROUND
13         002000 LCR      = 2000            ; LOAD CONTROL REGISTER
14         076000 CLS      = 76000           ; CLEAR SYSTEM
15         000020 GRAY     = 20              ; GRAY SCALE INDICATOR
16         001400 ISFLYD   = 1400           ; DISPLAY DATA MODE
17         000010 AUDITV   = 10              ; ADDITIVE PICTURE ELEMENT
18         000040 GRAY16   = 40              ; 16 LEVELS OF GRAY
19         000020 GRAY4    = 20              ; 4 LEVELS OF GRAY
20         000000 R0=%0
21         000001 R1=%1
22         000002 R2=%2
23         000003 R3=%3
24         000004 R4=%4
25         000005 R5=%5
26         000006 SP=%6
27         000007 PC=%7
28 000000      DISPLY:
29 000000 005725      TST      (R5)+          ; SKIP OVER # OF ARGS.
30 000002 013567      MOV      @ (R5)+, CURROW ; CURRENT ROW #
31         000474
32 000006 013567      MOV      @ (R5)+, NUMCOL  ; NUMBER OF PIXELS TO BE
33         000472
34 00012 013567      MOV      @ (R5)+, ROW      ; DISPLAYED
35         000470
36 00016 013567      MOV      @ (R5)+, COL      ; SCREEN
37         000466
38 00022 011501      MOV      (R5), R1          ; LEFT OF SCREEN
39 00024 012700      MOV      #LCAINS, R0
40         000516
41 00030 012737      MOV      #-1, @#IWC       ; INITIALIZE DISPLAY WORD COUNT
42         177777
43         164002
44 00036 012703      MOV      #8, R3            ; NOW R0 -> LY1 INSRUCT.
45         000010
46 00042 012704      MOV      #SHIFT0, R4       ; 8 SHIFT VALUES
47         000364
48 00046 012705      MOV      #STACK-2, R5      ; PLACE ADDR. OF BIT SHIFT
49         000472
50 00052 012445      MOV      (R4)+, -(R5)      ; PATTERN (CHANNEL 0) IN R4
51 00054 077302      SUBR     R3, -2           ; PUT BIT SHIFT ON STACK
52                                     ; BRANCH UNTIL ALL BIT SHIFTS
53                                     ; ARE ON STACK

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48 00056 010145      MOV      R1, -(R5)          ; PLACE ADDR. OF INTEGER
49                                     ; ARRAY ON STACK
50 00060 012703      MOV      #8, R3             ; 8 SHIFT VALUES
    000010
51 00064 012704      MOV      #SHIFT1, R4        ; PLACE ADDR. OF BIT SHIFT
    000404
52                                     ; PATTERN (CHANNEL 1) IN R4
53 00070 012445      MOV      (R4)+, -(R5)       ; PUT BIT SHIFT VALUE ON STACK
54 00072 077302      SOB      R3, -2            ; BRANCH UNTIL ALL BIT SHIFTS
55                                     ; ON STACK
56 00074 010145      MOV      R1, -(R5)          ; PLACE ADDR. OF INTEGER ARRAY
57                                     ; ON STACK
58 00076 012767      MOV      #2, CHANL          ; SET DISPLAY CHANNEL TO 1
    000002
    000374
59 00104 012767      MOV      #3, CLRBIT         ; CLEAR BIT PATTERN (0011)
    000003
    000364
60 00112             NXCHNL:
61             ; BUILD LCA INSTRUCTION
62 00112 012710      MOV      #LCA, (R0)
    044000
63 00116 062710      ADD      #GRAY4, (R0)
    000020
64 00122 066720      ADD      CHANL, (R0)+
    000352
65 00126 062737      ADD      #-1, @#IWC        ; INCREMENT IWC
    177777
    164002
66             ; BUILD LX1 INSTRUCTION
67 00134 012710      MOV      #LX1, (R0)
    024000
68 00140 066720      ADD      COL, (R0)+
    000344
69 00144 062737      ADD      #-1, @#IWC        ; INCREMENT IWC
    177777
    164002
70             ; BUILD LY1 INSTRUCTION
71 00152 012710      MOV      #LY1, (R0)
    004000
72 00156 066710      ADD      ROW, (R0)          ; ADD ROW DISPLACEMENT TO LY1
    000324
73                                     ; INSTRUCTION
74 00162 066720      ADD      CURROW, (R0)+      ; ADD ARRAY ROW #, R0 -> BXF
    000314
75                                     ; INSTRUCTION
76 00166 062737      ADD      #-1, @#IWC        ; INCREMENT IWC
    177777
    164002
77 00174 010067      MOV      R0, BLKTRN        ; BLKTRN = ADDR. OF CURRENT
    000312
78                                     ; BXF DISPLAY INSTRUCT.
79 00200 012720      MOV      #BXF, (R0)+      ; INITIALIZE BXF INSTRUCT.
    016000
80 00204 062737      ADD      #-1, @#IWC        ; INCREMENT IWC
    177777
    164002

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81 00212 012501      MOV      (R5)+,R1          ;GET ADDR OF INTEGER ARRAY
82                                     ;SP -> BIT SHIFT LIST
83 00214 010567      MOV      R5,STACK          ;SAVE CURRENT STACK POINTER
      000254
84                                     ;
85                                     ; BEGIN CONSTRUCTION OF A NEW DISPLAY DATA WORD
86                                     ;
87 00220 005004 NXTWRD: CLR      R4              ; R4 = TEMP. LOC. OF DISPLAY
                                          ; DATA WORD
88                                     ; R3 = OF PIXELS/DISPLAY WORD
89 00222 012703      MOV      #8.,R3
      000010
90 00226 016705      MOV      STACK,R5          ; RESET SP TO FIRST BIT SHIFT VALUE
      000242
91                                     ;
92                                     ;
93 00232 012102 GET:   MOV      (R1)+,R2          ; GET AN INTEGER ARRAY ELEMENT
94 00234 022702      CMP      #99.,R2          ; HAS LAST PIXEL BEEN PROCESSED
      000143
95 00240 001405      BEQ      OUT              ; BRANCH IF IT HAS
96 00242 046702      BIC      CLRBIT,R2        ; CLEAR BITS
      000230
97 00246 072225      ASH      (R5)+,R2          ; SHIFT R2 AS REQUIRED
98 00250 050204      BIS      R2,R4            ; COMBINE CURRENT & PREVIOUS
99                                     ; DISPLAY WORD
100 0252 077311      SOB      R3,GET           ; BRANCH UNTIL 8 PIXELS INPUT
101                                     ;
102                                     ; ADD COMPLETE DISPLAY DATA WORD TO DISPLAY DATA BUFFER
103                                     ;
104 0254 010420 OUT:   MOV      R4,(R0)+        ; PLACE DISPLAY WORD
105                                     ; DISPLAY BUFFER
106 0256 062737      ADD      #-1.,@#1WC       ; INCREMENT DISPLAY WORD COUNT
      177777
      164002
107 0264 062777      ADD      #2.,@BLKTRN     ; INCREMENT BXF BYTE COUNT
      000002
      000220
108 0272 022761      CMP      #99.,-2(R1)     ; HAS LAST PIXEL BEEN
      000143
      177776
109                                     ; PROCESSED ?
110 0300 001347      BNE      NXTWRD          ; BRANCH TO CONSTRUCT NEXT
111                                     ; WORD IF NOT
112 0302 022767      CMP      #1.,CHANL       ; IS CURRENT CHANNEL # = 1
      000001
      000170
113 0310 001414      BEQ      INITD           ; IF YES, BRANCH TO INITIATE
114                                     ; DISPLAY
115 0312 012767      MOV      #12.,CLRBIT     ; NOT FINISHED - RESET BIT
      000014
      000156
116                                     ; CLEAR PATTERN TO (0011)
117 0320 012767      MOV      #1.,CHANL       ; CHANGE CHANNEL TO 1
      000001
      000152
118 0326 062767      ADD      #16.,STACK      ; INCREMENT CURRENT STACK ADDR.
      000020
      000140

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119 0334 016705      MOV      STACK,R5          ;SET STACK POINTER TO NEXT
      000134
120
121 0340 000664      BR       NXCHNL            ;BIT SHIFT LIST
122                                     ;GO PROCESS INTEGER ARRAY
123 0342 012737 IN1ID: MOV      #CBUFF,@#1CA    ;FOR NEW CHANNEL
      000514
      164004
124 0350 105767      TSTB     ICS                ;
      164000
125 0354 100375      BPL      -4                 ;
126 0356 005267      INC      ICS                ;
      164000
127 0362 000207      RTS      PC                 ;
128 0364 000000 SHIFT0: .WORD 0,2,4,6,8,10,12,14.
      0366 000002
      0370 000004
      0372 000006
      0374 000010
      0376 000012
      0400 000014
      0402 000016
129 0404 177776 SHIFT1: .WORD -2,0,2,4,6,8,10,12.
      0406 000000
      0410 000002
      0412 000004
      0414 000006
      0416 000010
      0420 000012
      0422 000014
130 0424      BLOCK: .BLKW 20.
131 0474 000000 STACK: .WORD 0
132 0476 000000 CLRBIT: .WORD 0
133 0500 000000 CHANL: .WORD 0
134 0502 000000 CURROW: .WORD 0
135 0504 000000 NUMCOL: .WORD 0
136 0506 000000 ROW: .WORD 0
137 0510 000000 COL: .WORD 0
138 0512 000000 BLKTRN: .WORD 0
139                                     .EVEN
140 0514 003520 CBUFF: .WORD LCR+DSPLYD+GRAY+BLACK ;LOAD CONTROL REG.
141 0516      LCAINS: .BLKW 150.                ;DISPLAY DATA INSTRUCTIONS
142      000000      .END      DISPLY

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1          .MCALL
2          .GLOBL CLEAR
3          ; ***** DEFINE VIDEO DISPLAY INSTRUCTIONS *****
4          000100 BLACK = 100          ; BLACK BACKGROUND
5          004000 LY1   = 4000         ; LOAD FIRST Y VALUE
6          010000 LY2   = 10000        ; LOAD SECOND Y VALUE
7          024000 LX1   = 24000        ; LOAD FIRST X VALUE
8          030000 LX2   = 30000        ; LOAD SECOND X VALUE
9          076000 CLS    = 76000        ; CLEAR SYSTEM
10         044000 LCA    = 44000        ; LOAD CHANNEL ADDRESS
11         002000 LCR    = 2000         ; LOAD CONTROL REGISTER
12         000040 GRAY16 = 40           ; 16 LEVELS OF GRAY
13         000200 ERASE  = 200          ; ERASE THIS CHANNEL
14         001200 GRLINE = 1200         ; GRAPHIC LINE
15         164004 ICA    = 164004       ; CORE ADDRESS OF DISPLAY INSTRUCTIONS
16         164002 IWC    = 164002       ; WORD COUNT IN INSTRUCTION BUFFER
17         164000 ICS    = 164000       ; CONTROL & STATUS REG. FOR VIDEO DISPLAY
18         001400 DSPLYD = 1400
19         000020 GRAY   = 20
20         000010 OUTLIN = 10
21         ;
22         ; ***** DEFINE REGISTERS *****
23         ;
24         000007 PC      = %7
25         ;
26         ; FOLLOWING CLEARS THE VIDEO SCREEN PRIOR TO EACH DISPLAY
27         ;
28 000000 105767 CLEAR:  TSTB    ICS
29                164000
30 000004 100375      BPL      -4
31 000006 012767      MOV      #CBLOCK, ICA
32                000030
33                164004
34 000014 012767      MOV      #-5, IWC
35                177773
36                164002
37 000022 005267      INC      ICS
38                164000
39 000026 000207      RTS      PC
40 000030 076000 CBLOCK: .WORD   CLS
41                .WORD   LCR+GRLINE+BLACK
42 000032 003300      .WORD   LCA+GRAY16+ERASE+0
43 000034 044240      .WORD   LCA+GRAY16+ERASE+1
44 000036 044241      .WORD   LCA+GRAY16+ERASE+2
45 000040 044242      .WORD   LCA+GRAY16+ERASE+2
46 000000 000000      .END    CLEAR

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```

0001      DIMENSION  Ibuff(1000), ILine(40), IChar(40)
C
C --> PURPOSE OF THIS PROGRAM IS TO (FOR SPECIFICIED FILE #)
C      1 - READ BLOCK #'S 121 & 122 AND OUTPUT TO A DISK FILE
C      2 - REWIND INPUT TAPE AND OUTPUT SPECIFIED # OF BLOCKS OF EEG DATA
C          TO SPECIFIED DISK FILENAME
C
C --> INPUT THE FOLLOWING VARIABLE VALUES FROM KEYBOARD (PROMPTED)
C      NAMEFIL - NAME OF OUTPUT DISK FILE (MAX OF 12 CHARACTERS)
C      KFILE - TAPE FILE # (1-4) FROM WHICH DATA IS TO BE READ
C      KBLK - # OF DATA BLOCKS ON TAPE TO BE WRITTEN TO DISK
0002      WRITE(7,23)
0003 23      FORMAT(' INPUT # OF BLOCKS TO BE WRITTEN TO DISK')
0004      READ(7,3) KBLK
0005 3        FORMAT(I3)
0006      WRITE(7,24)
0007 24      FORMAT(' INPUT FILE # TO BE WRITTEN TO DISK')
0008      READ(7,3) KFILE
0009      WRITE(6,4)
0010 4        FORMAT(' BEGIN PROCESSING EEG TAPE PGM. NAME -- TTAPE.FOR')
0011      WRITE(6,45) KBLK, KFILE
0012 45      FORMAT(' COPY ',I3,' BLOCKS FROM FILE #',I2,' TO ',
*           'DISK')
0013      CALL ASSIGN(2,'MT')
0014      CALL ASSIGN(1,'TEST1.DAT')
C
C
0015      IFILE = 1
0016      ITRIP = 0
C FOLLOWING CALL TO MTREAD ALLOWS PASSING OVER TAPE HEADER ONLY
0017 5        CALL MTREAD(IBUFF, IEOF)
0018 50       IBLOCK = 1
C
C
0019      WRITE(6,40) IFILE
0020 40       FORMAT('BEGIN FILE #',I2)
C
C
0021 70       CALL MTREAD(IBUFF, IEOF)
0022      IF (IEOF.NE. 0) GO TO 1000
C
C
0024      IF (IFILE.EQ.KFILE)
*           WRITE(6,50) IBLOCK
0026 50       FORMAT(' BEGIN BLOCK #',I3)
C           WRITE(6,52) IEOF
CS2        FORMAT(' END OF FILE FLAG (IEOF) = ',I2)
C
C
0027      DO 10 K = 1, 25
C      WANT TO OUTPUT BLOCK #'S 121 & 122 DURING FIRST READ OF TAPE
C --> BRANCH TO $MTL LABEL UNTIL BLOCK #121 IS REACHED DURING FIRST
C      READ OF TAPE(ITRIP = 0)

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      C      INCREMENT ITRIP BY 1 IMMEDIATELY AFTER REACHING BLOCK #121 FOR FIRST TIME
      C
0028      IF (IFILE .NE. KFILE) GO TO 65
0030      IF (ITRIP .EQ. 0 .AND. IBLOCK .LT. 121)
      *      GO TO 65
0032      IF (ITRIP .EQ. 0) ITRIP = ITRIP + 1
0034      J = (K - 1) * 40
0035      DO 20 N = 1, 40
0036      ILINE(N) = IBUFF(J + N)
0037 20    CONTINUE
0038      DECODE(80, 30, ILINE, ERR=3000) ICHAR
0039 30    FORMAT(40A2)
0040 140   IF (K .EQ. 1) WRITE(6, 130) K, (ICHAR(INDEX), INDEX=1, 40)
0042 130   FORMAT(' K = ', I4, ' : ', 40A2)
0043      WRITE(1, 30, ERR=2000) (ICHAR(INDEX), INDEX=1, 40)
      C      WRITE(6, 30) (ICHAR(INDEX), INDEX=1, 40)
0044 10    CONTINUE
      C
      C
0045      WRITE(6, 60) IBLOCK
0046 60    FORMAT(' FINISH BLOCK #', I3/)
0047 65    IBLOCK = IBLOCK + 1
0048      IF (ITRIP .EQ. 0 .AND. IBLOCK .GT. 123) GO TO 1000
      C
      C --> ITRIP = 1 AFTER BLOCK #121 IS READ FOR FIRST TIME
      C
0050      IF (ITRIP .EQ. 1 .AND. IBLOCK .GT. 122 .AND. IFILE .EQ. KFILE)
      *      GO TO 200
      C
      C --> ITRIP = 2 AT BEGINNING OF SECOND READ OF TAPE
      C
0052      IF (ITRIP .EQ. 2 .AND. IBLOCK .GT. 123) GO TO 1000
0054      IF (ITRIP .EQ. 2 .AND. IBLOCK .GT. KBLK .AND. IFILE .EQ. KFILE)
      *      GO TO 4000
0056      GO TO 70
0057 1000  WRITE(6, 80) IFILE, IEOF
0058 80    FORMAT(' FINISH FILE #', I2, ' , IEOF = ', I2)
0059      IF (IFILE .GE. 4) GO TO 4000
0061      IFILE = IFILE + 1
0062      GO TO 5
      C
      C
0063 2000  WRITE(6, 100) (ICHAR(INDEX), INDEX=1, 40)
0064 100    FORMAT(' ???? WRITE ERROR, OUTPUT AS FOLLOWS'/40A2)
0065      GO TO 10
0066 3000  WRITE(6, 110) (ICHAR(INDEX), INDEX=1, 40)
0067 110    FORMAT(' ???? DECODE ERROR, INPUT AS FOLLOWS'/40A2)
0068      GO TO 140
      C
      C --> REWIND TAPE IN PREP. FOR SECOND TAPE READ
      C
0069 200    WRITE(6, 210) IBLOCK
0070 210    FORMAT(' HAVE FINISHED READING BLOCK #', I4/ ' START '
      * 'PROCESSING EEG DATA')

```

APPENDIX C

CONVERSION OF GRAY SCALE DISPLAY TO COLOR DISPLAY

Conversion of the current gray scale display to a color display involves several changes in the subroutine DISPLA. Instead of two display channels, three must be used—one for each of the primary colors: red, blue and green. Each eight bit data byte will carry six mask bits, two for each channel, in the low order positions, allowing the display of one image point. Note that the two high order bit positions are not used and that the data bytes are arranged in descending order. The use of three display channels provides for up to 64 different colors. Mapping of the 16 gray levels into the 64 colors should be done so as to allow for a maximum of differentiation. This might well be done by assigning each gray level to every fourth color combination. Simplification of the assembler program may be achieved by performing this mapping prior to execution of the display program.

VITA

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