



November 2008

The effect of heterogeneous infectious period and contagiousness on the dynamics of Salmonella transmission in dairy cattle

Cristina Lanzas
Cornell, clanzas@utk.edu

S Brien

R Ivanek

Y Lo

P P. Chapagain

See next page for additional authors

Follow this and additional works at: http://trace.tennessee.edu/utk_compmedpubs

 Part of the [Animal Diseases Commons](#), [Disease Modeling Commons](#), and the [Veterinary Preventive Medicine, Epidemiology, and Public Health Commons](#)

Recommended Citation

Lanzas, Cristina; Brien, S; Ivanek, R; Lo, Y; Chapagain, P P.; Ray, K A.; Ayscue, P; Warnick, L D.; and Grohn, Y T., "The effect of heterogeneous infectious period and contagiousness on the dynamics of Salmonella transmission in dairy cattle" (2008). *Faculty Publications and Other Works -- Biomedical and Diagnostic Sciences*.
http://trace.tennessee.edu/utk_compmedpubs/34

This Article is brought to you for free and open access by the Veterinary Medicine -- Faculty Publications and Other Works at Trace: Tennessee Research and Creative Exchange. It has been accepted for inclusion in Faculty Publications and Other Works -- Biomedical and Diagnostic Sciences by an authorized administrator of Trace: Tennessee Research and Creative Exchange. For more information, please contact trace@utk.edu.

Authors

Cristina Lanzas, S Brien, R Ivanek, Y Lo, P P. Chapagain, K A. Ray, P Ayscue, L D. Warnick, and Y T. Grohn

The effect of heterogeneous infectious period and contagiousness on the dynamics of *Salmonella* transmission in dairy cattle

C. LANZAS^{1*}, S. BRIEN¹, R. IVANEK¹, Y. LO¹, P. P. CHAPAGAIN^{1,2}, K. A. RAY¹,
P. AYSCUE¹, L. D. WARNICK¹ AND Y. T. GRÖHN¹

¹ Department of Population Medicine and Diagnostic Science, College of Veterinary Medicine, Cornell University, Ithaca, NY, USA

² Department of Physics, Florida International University, Miami, FL, USA

(Accepted 7 November 2007; first published online 16 January 2008)

SUMMARY

The objective of this study was to address the impact of heterogeneity of infectious period and contagiousness on *Salmonella* transmission dynamics in dairy cattle populations. We developed three deterministic SIR-type models with two basic infected stages (clinically and subclinically infected). In addition, model 2 included long-term shedders, which were defined as individuals with low contagiousness but long infectious period, and model 3 included super-shedders (individuals with high contagiousness and long infectious period). The simulated dynamics, basic reproduction number (R_0) and critical vaccination threshold were studied. Clinically infected individuals were the main force of infection transmission for models 1 and 2. Long-term shedders had a small impact on the transmission of the infection and on the estimated vaccination thresholds. The presence of super-shedders increases R_0 and decreases the effectiveness of population-wise strategies to reduce infection, making necessary the application of strategies that target this specific group.

INTRODUCTION

Non-typhoidal strains of *Salmonella enterica* are a major cause of foodborne illness in humans. In the United States alone, *Salmonella* accounts for an estimated 1·4 million cases of illness, 16 000 hospitalizations and 600 deaths annually [1]. Cattle are recognized as an important source of *Salmonella* causing human illness, particularly for antimicrobial-resistant strains. Transmission from cattle to humans has been described via contaminated meat [2], milk [3], dairy products [4] and also by direct contact with sick animals and their environment [5]. Recently,

the emergence of several multidrug-resistant (MDR) strains of *Salmonella*, notably MDR Typhimurium DT104 and Newport, has complicated treatment and control of clinical disease in humans; humans infected with MDR strains are at greater risk of bacteraemia, hospitalization and death compared to patients infected with susceptible strains [6, 7].

Prevention of human salmonellosis depends on decreasing the prevalence of infections in livestock hosts as well as identifying and intervening along key transmission routes. Controlling the spread of *Salmonella* at farm level and through the food chain has proven difficult [8]; partly because of the large variation observed in the epidemiological characteristics of *Salmonella* infection at herd level, which range from large clinical outbreaks to endemic persistence without clinical cases [9, 10]. Elucidation of

* Author for correspondence: Dr C. Lanzas, Department of Population Medicine and Diagnostic Science, College of Veterinary Medicine, Cornell University, Ithaca, NY 14853, USA.
(Email: cl272@cornell.edu)

effective control strategies requires, therefore, an improved understanding of the dynamics of infections within host populations and the causes of such a wide range of outcomes in the host–pathogen interaction [11]; including interactions among immunity of the host, infectious dose and virulence of the serotype, and environmental factors [12].

Mathematical models of disease dynamics provide a comprehensive framework in which our current understanding of disease transmission can be summarized, and the impact of intervention strategies can be evaluated [12]. There are only three existing mathematical models of *Salmonella* transmission dynamics in dairy herds. Xiao and colleagues developed theoretical deterministic [13] and stochastic [14] models of *Salmonella* infections. These authors investigated the effects of demographic (e.g. culling rate) and epidemiological (e.g. pathogen-induced mortality) factors on epidemic behaviour and threshold for invasion, while Chapagain *et al.* developed a mathematical model to describe an outbreak of *S. Cerro* in a dairy herd [15].

Heterogeneity in host–pathogen interaction (such as heterogeneous infectious period and contagiousness) may play an important role in determining the outcome of a *Salmonella* infection. Cattle with clinical salmonellosis, which can shed up to 10^{10} c.f.u./g faeces [16], may be responsible for amplifying environmental contamination and therefore raising the challenge exposure enough to cause large outbreaks in the herd [10]. On the other hand, long-term persistence of *Salmonella* in herds has been attributed to the presence of a few individuals that persistently excrete the organism, and thus, removing those individuals has been proposed as a control measure [11]. Heterogeneity in infection transmission has not been addressed in previous models [13, 15].

The overall objective of this study was to assess how heterogeneity in infectious period and contagiousness affect transmission dynamics of *Salmonella* infection in dairy herds. In particular we addressed the following questions: (1) What is the relative importance of clinical and subclinical cases in the transmission of the infection? (2) What is the role of long-term shedders? (3) How can heterogeneity in host infectiousness impact the efficiency of control strategies such as vaccination? To address these questions we developed a series of state transition models (i.e. SIR models) in which different infectious states representing current knowledge were included.

MATERIAL AND METHODS

Models formulation

We developed three deterministic SIR models of *Salmonella* transmission within cattle group. In an SIR-type model, the host population is categorized according to infection status into susceptible (*S*), infected (*I*), and recovered (*R*) classes [12]. A latent state was not included in the models as the latent period in *Salmonella* infections is thought to be very short (24–48 h), and therefore it has little impact on the infection dynamics [12]. Infection with *Salmonella* can result in clinical or subclinical disease [17]. For subclinically infected animals, the duration of faecal shedding can be highly variable [11, 18]. To account for these differences, several *I* stages were included in the models. Each of the *I* stages differ in several parameter values, including infectious period and ‘transmission coefficient’, also known and defined here as ‘ β ’, describing the rate at which susceptible hosts are ‘converted’ into infected hosts by their contact with infectious material (defined as in [19]). An assumption in assigning β for each infected stage is that bacterial load is the only factor that varies among infected stages, and thus other factors that determine the probability of successful transmission are identical.

The following assumptions are common to all three models:

- (1) The population size is constant as the recruitment rate is equal to the exit rate. This reflects the tendency of dairy farms to maintain a constant herd size.
- (2) All newly introduced animals are susceptible. In reality, a replacement animal could be infected and actually serve as a vehicle for introduction of new infection into the herd. However, the purpose of this study was not to evaluate sources for *Salmonella* infection into the herd and a simplifying assumption was accepted.
- (3) Direct transmission is the only route of new infection (i.e. vertical and indirect transmission were not considered). Although the main route of transmission is faecal–oral, and therefore infection is mostly acquired through contact with bacteria shed in the environment (i.e. an indirect exposure), an environment compartment is not explicitly included in the model. We instead assume one common environment in which environmental proliferation is rather limited.

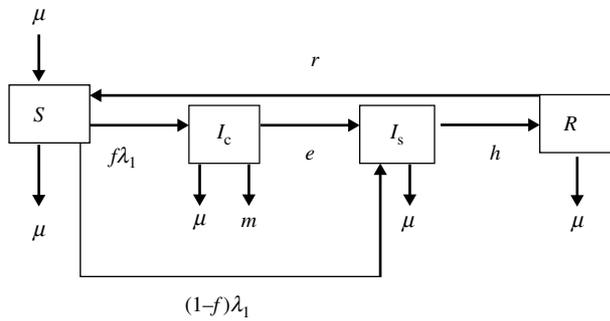


Fig. 1. Flow diagram representing model 1. Four transition states are included: susceptible (S), clinically infected (I_c), subclinically infected (I_s) and recovered (R). Animals move from S to I_c at rate $f\lambda_1$ and from S to I_s at rate $(1-f)\lambda_1$, where f is the proportion of infected animals that develop clinical disease. Clinically infected animals progress to I_s at rate e . Animals in I_s acquire immunity at rate h . The immunity of recovered animals wanes at rate r . Exit for all compartments and replacement for compartment S takes place at rate μ . Animals in I_c also exit the compartment at rate m .

In addition, the main objective is to assess the relative contribution of different types of infected animals to transmission, which would remain unchanged whether or not we include indirect route of infection. The potential for vertical transmission was not included because it is thought to be less important than other routes of infection [20] and also because we modelled an adult cow population.

We selected the transmission term to be ‘density-dependent’, and thus the force of infection (λ) is represented by βI . This form was favoured because increased prevalence of *Salmonella* infection has been reported with increasing herd size [21, 22].

The ordinary differential equations describing the three models are presented in Appendix 1. Two I states were included in model 1: clinically infected (I_c) and subclinically infected (I_s) (Fig. 1); a fraction of the infected animals was assumed to become I_s immediately following infection, and all I_c were assumed to become I_s before full recovery. These states reflect the biological reality that not all infected animals develop clinical salmonellosis [17], and cattle that have recovered from clinical disease can continue to shed *Salmonella* [23, 24]. Exposure to cattle with clinical salmonellosis has been described as a risk factor for development of salmonellosis [22, 25], as I_c may shed larger quantities of c.f.u. than do I_s . Therefore, it was assumed that the transmission coefficient for I_c was greater than for I_s .

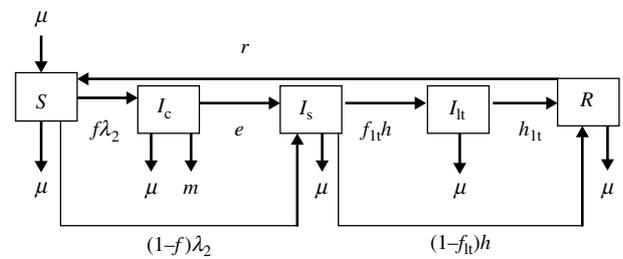


Fig. 2. Flow diagram representing model 2. Five transition states are included: susceptible (S), clinically infected (I_c), subclinically infected (I_s), long-term shedders (I_{st}) and recovered (R). Animals move from S to I_c at rate $f\lambda_2$ and from S to I_s at rate $(1-f)\lambda_2$, where f is the proportion of infected animals that develop clinical disease. Clinically infected animals progress to I_s at rate e . Animals in I_s either acquire immunity at rate $(1-f_1)h$ or become I_{st} at rate f_1h , where f_1 is the proportion of I_s that become I_{st} . The immunity of recovered animals wanes at rate r . Exit for all compartments and replacement for compartment S takes place at rate μ . Animals in I_c also exit the compartment at rate m .

A third infected stage, termed long-term shedders (I_{st}), was included in addition to the I_c and I_s states in model 2 (Fig. 2). Long-term persistence of *Salmonella* at farm level has been observed for several serotypes, including MDR *S. Newport* [11] and *S. Dublin* [9]. On farms with persistent *Salmonella*, few animals without clinical signs were reported to shed *Salmonella* persistently or intermittently. Because animals at the I_{st} stage do not present clinical signs, their transmission coefficient was assumed to be equivalent to the transmission coefficient for I_s .

In model 3, an alternate third infected stage, termed super-shedders (I_{ss}), was included in addition to the I_c and I_s states (Fig. 3). For other bacteria within the family Enterobacteriaceae, the term super-shedder has been used to describe those animals that harbour and shed bacteria at high levels [26]. Super-shedders have a significant impact on the transmission dynamics of *E. coli* O157, and thus removal of high-shedding individuals has been proposed as a control measure [27]. For *Salmonella*, we hypothesized that a fraction of the animals, after recovering from clinical signs of disease, would continue to shed high numbers of *Salmonella* for a long period of time. It is assumed that the transmission coefficient for I_{ss} is equal to the transmission coefficient for I_c .

Model parameters

Model parameters are defined in Table 1 and mean values and observed range are presented. Data from a longitudinal study to determine the incidence of

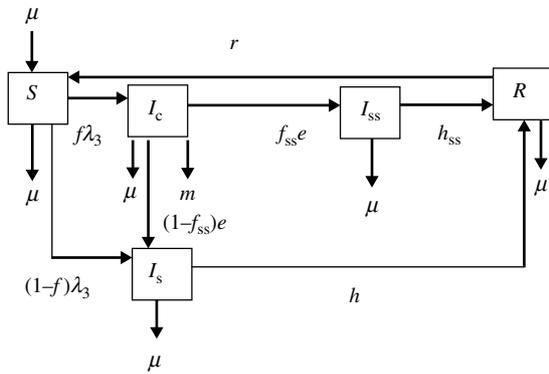


Fig. 3. Flow diagram representing model 3. Five transition states are included: susceptible (S), clinically infected (I_c), subclinically infected (I_s), super-shedders (I_{ss}) and recovered (R). Animals move from S to I_c at rate $f\lambda_3$ and from S to I_s at rate $(1-f)\lambda_3$, where f is the proportion of infected animals that develop clinical disease. Clinically infected animals progress to I_s at rate $(1-f_{ss})e$ and to I_{ss} at rate $f_{ss}e$, where f_{ss} is the proportion of I_c that become I_{ss} . Animals in I_s acquire immunity at rate h and I_{ss} acquire immunity at rate h_{ss} . The immunity of recovered animals wanes at rate r . Exit for all compartments and replacement for compartment S takes place at rate μ . Animals in I_c also exit the compartment at rate m .

salmonellosis in dairy cattle in the Northeastern United States was used to estimate some of the parameters [28]. Of 34 herds enrolled in the study, 22 farms with at least two laboratory-confirmed cases of salmonellosis and on-farm individual cow milk records were enrolled in a prospective follow-up study to determine the duration of faecal shedding following clinical salmonellosis. Diagnostic was established by bacteriological culture of faecal samples. Faecal samples from dairy cattle exhibiting clinical signs of salmonellosis were collected at around monthly intervals until three consecutive negative samples were obtained or the animal was lost to follow-up [24, 28]. Because no serological or faecal diagnostic tests were available for all apparently healthy animals, the actual size for all the compartments could not be determined, and therefore the transmission coefficient could not be calculated directly from the data.

The reciprocal of the duration of the clinical signs was assigned as recovery rate for I_c . The mean duration of clinical signs was estimated to be 4 days based on the literature [20] and by interviewing veterinarians experienced in bovine medicine (T. Divers, C. Guard, L. Warnick, personal communication). Data from the two enrolled herds with the largest outbreaks were used to estimate the remaining recovery rates, fraction of long-term shedders (f_{it}) and super-shedders (f_{ss})

and diseased induced mortality rates. Recovery rates for I_s , I_{ss} , and I_{it} were estimated from the available *Salmonella* faecal shedding data. Duration of *Salmonella* shedding was estimated by the Kaplan–Meier life-test method; animals without three consecutive negative samples after the last positive sample were right-censored [24]. The proportion of animals shedding after clinical salmonellosis follows a decay curve. To obtain the recovery rates for each model, it was assumed that the decay curve was the result of one or two populations (depending on the model) shedding at given rates, and an exponential compartmental model based on the model structure was fitted to the data:

- (1) For model 1, since all infected animals after I_c become I_s , the proportion of animals shedding at time t ($P(t)$) was fitted to one single exponential decay curve,

$$P(t) = e^{-ht}. \quad (1)$$

- (2) In model 2, there are two populations of animals shedding sequentially. All animals in I_s shed at rate h , and a fraction of I_s (f_{it}) continues to shed at a rate h_{it} . Solving the corresponding system of differential equations analytically gives the following sequential irreversible compartmental model,

$$P(t) = \left(1 - \frac{h}{h-h_{it}}f_{it}\right)e^{-ht} + \frac{h}{h-h_{it}}f_{it}e^{-h_{it}t}. \quad (2)$$

- (3) In model 3, there are two populations of animals shedding simultaneously (I_s and I_{ss}), and therefore the decay curve is the sum of two exponential decay curves,

$$P(t) = (1-f_{ss})e^{-ht} + f_{ss}e^{-h_{ss}t} \quad (3)$$

The decay functions were fitted to the data by non-linear regression, using the NLIN procedure of SAS (SAS Institute, Cary, NC, USA). The Levenberg–Marquard algorithm was used.

Salmonella-induced mortality rate was calculated as the number of deaths which reported *Salmonella* as the cause divided by the number of days at risk of death times the number of cows at risk, where cows at risk were defined as the animals with clinical signs and days at risk of death were the mean duration of clinical signs.

Models analysis and simulations

Both numerical and analytical techniques were used to analyse and compare the models. For the numerical

Table 1. *List of parameters*

Symbol	Parameter definition (units)	Mean value*	Estimated range	Models	Sources
μ	Replacement and exit rate (day^{-1})	0.0011	0.00078–0.0018	1, 2, 3	Data†
β_c	Transmission coefficient for clinical animals ($\text{animal}^{-1} \text{day}^{-1}$)	0.0016	—	1, 2, 3	Assumed‡
β_s	Transmission coefficient for subclinical animals ($\text{animal}^{-1} \text{day}^{-1}$)	0.00006	—	1, 2, 3	Assumed‡
β_{lt}	Transmission coefficient for long term shedders ($\text{animal}^{-1} \text{day}^{-1}$)	0.00006	—	2	Assumed‡
β_{ss}	Transmission coefficient for super-shedders ($\text{animal}^{-1} \text{day}^{-1}$)	0.0016	—	3	Assumed‡
f	Proportion of infected animals that develop clinical disease (dimensionless)	0.50	—	1, 2, 3	Assumed
f_{lt}	Proportion of subclinical cases that become long term shedders (dimensionless)	0.12	0.05–0.26	2	Outbreak data
f_{ss}	Proportion of clinical cases that become super-shedders (dimensionless)	0.14	0.04–0.23	3	Outbreak data
e	Rate of clinical cases that become subclinical (day^{-1})	0.25	0.14–0.50	1, 2, 3	[20]/experts
h	Recovery rate for subclinical cases (day^{-1})	0.041§ (0.057)	0.0411–0.0419 (0.047–0.093)	1, 2, 3	Outbreak data
h_{lt}	Recovery rate for long-term shedders (day^{-1})	0.01	0.006–0.012	2	Outbreak data
h_{ss}	Recovery rate for super-shedders (day^{-1})	0.01	0.0059–0.012	3	Outbreak data
m	Disease induced mortality rate (day^{-1})	0.011	0.006–0.016¶	1, 2, 3	Outbreak data
r	Immunity loss rate (day^{-1})	0.01	0.007–0.015	1, 2, 3	[39]

* Value used when parameter was not varied in a simulation.

† Based on average lactating cows longevity in a convenience sample of New York herds (from Ambulatory and Production Medicine Services, Cornell University).

‡ Based on iterative fitting of the model output to the available outbreak data.

§ Estimated value for model 1. Estimated values for models 2 and 3 in parentheses.

|| Faecal shedding data were fitted to equations (1), (2), and (3).

¶ Lower range value was estimated from an outbreak of *Salmonella* group C; Upper value was estimated from an outbreak of *Salmonella* group B.

simulations, the median of the census of lactating cows in farms with at least two clinical cases in the longitudinal study [28] was used as the value for the total population ($N=345$). Simulations started with a complete susceptible population and the introduction of one clinically infected animal. The models were implemented and simulated with Vensim professional version 5.0a (Ventana Systems Inc., Harvard, MA, USA). A fourth-order Runge–Kutta method was used for integration. We assessed the effect of changing the proportion of the different infected stages on the pattern of prevalence of infection and clinical disease and the relative contribution of each stage to new infections. We tested values for the fractions f , f_{it} and f_{ss} greater than the range used on the sensitivity analyses ($\pm 25\%$ from the mean) in order to explore range of patterns of prevalence simulated by each model. For model 1, we simulated the model with the following arbitrarily chosen f values, 0.15 and 0.85. For models 2 and 3, we used the values 0.05 and 0.25 for f_{it} and f_{ss} .

The basic reproduction number (R_0) is the average number of secondary infections produced when one infected individual is introduced into a wholly susceptible host population and is the threshold quantity that determines when an infection can invade and persist in a new host population [29]. If $R_0 < 1$, an infected individual produces less than one newly infected individual on average over the course of its infectious period, and therefore the infection cannot invade or persist [29]. For a SIR model with one category of infected individuals, R_0 is the product of the infection rate and the mean duration of the infectious period. Because our models have several categories of infected individuals (e.g. clinically and subclinically infected individuals), the next-generation method was used to obtain R_0 expressions [29, 30]; Appendix 2 contains the derivation of R_0 . To assess the potential impact of the heterogeneity of infectiousness on a vaccination programme, the critical proportion of the population to be immunized in order to decrease R_0 to below 1 (p_c) was estimated for each model. The efficacy for *Salmonella* vaccinations is highly variable [31, 32], therefore p_c was calculated for different vaccination efficacies (Φ). In a population with homogenous mixing, and with a vaccine that is equally effective across all infectious stages, p_c is given by the expression [12],

$$p_c = \frac{1}{\phi} \left(1 - \frac{1}{R_0} \right), \quad (4)$$

R_0 can be expressed as the sum of the contribution of the clinical stage (R_{0c}) and the contribution of the other infected stages ($R_{0c'}$), i.e.

$$R_0 = R_{0c} + R_{0c'}. \quad (5)$$

The eradication criterion in a homogeneously mixed population is [12]

$$(1 - p_c)R_{0c} + (1 - p_{c'})R_{0c'}. \quad (6)$$

If we assume that the vaccines that attenuate the severity of the clinical cases but do not prevent infection only reduce the transmission due to clinically infected animals (i.e. $p_{c'}=0$), then p_c is given by the expression,

$$p_c = \frac{1}{\phi} \left(1 - \frac{1 - R_{0c'}}{R_{0c}} \right). \quad (7)$$

If $R_{0c'} > 1$, then the reduction of the transmission from the clinically infected individuals would not be enough to prevent an epidemic or eliminate an endemic infection.

Because the parameters were obtained either from only two outbreaks or were assumed, we tested the sensitivity of the predicted endemic prevalence of infection and R_0 to the parameters' uncertainties. We performed a global sensitivity analysis in which all parameters tested were varied simultaneously using Monte Carlo techniques [33]. Parameters were described by uniform distribution with $\pm 25\%$ from the mean as the minimum and maximum values. The sampling technique chosen for drawing the samples from the distributions was the Latin Hypercube [34]. In order to relate the variation in the model outputs to the parameters, a stepwise regression analysis was used. Standard regression coefficients (SRC) were used to rank the parameters. When models are linear or moderately nonlinear ($R^2 > 0.70$), SRC provide a measure of importance of each parameter based on the effect of moving each parameter away from its mean value by a fixed fraction of its standard deviation while retaining all the other parameters at their mean value [33]. For all the models, the R^2 for the stepwise regression was > 0.95 . Monte Carlo simulations (200 iterations) were carried out in Vensim professional version 5.0a (Ventana Systems Inc.) and the REG procedure of SAS was used for the stepwise regressions (SAS Institute, Cary, NC, USA).

RESULTS

Epidemic and endemic behaviour

The simulated prevalence of infection at the peak of the epidemics and at the endemic stage using the mean

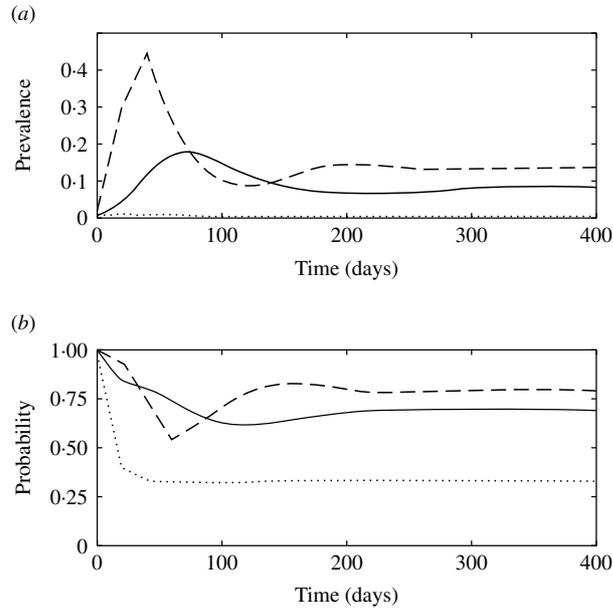


Fig. 4. (a) Simulated prevalence of infection with model 1 when the fraction of clinically infected animals (f) is 0.15 (·····), 0.5 (—) and 0.85 (---). (b) Probability that a newly infected case arises from contact with a clinically infected animal in model 1 when f is 0.15 (·····), 0.5 (—) and 0.85 (---).

parameter values from Table 1 were 0.18 and 0.08 for model 1, 0.16 and 0.10 for model 2 and 0.32 and 0.17 for model 3, respectively. Figure 4 shows the simulated total prevalence of infection when the fraction of newly infected individuals that develop clinical diseases (f) was varied for model 1. When f was low (0.15), subclinically infected animals were not able to maintain the infection, and an outbreak did not take place (predicted $R_0 < 1$). On the other hand, large f ($f = 0.85$) resulted in well-defined epidemics that peaked early and were followed by damped oscillations before reaching a steady state. Predicted endemic prevalence was greater for large f . High β for clinically infected animals and a faster recovery rate for subclinically infected animals had a similar impact to large f on the pattern of infection (results not shown).

When the fraction of subclinically infected individuals that become long-term shedders (f_{lt}) was varied in model 2 (Fig. 5), the early stages of epidemics remained similar (< 100 days) as the early contribution of long-term shedders is relatively low (Fig. 5b). High f_{lt} resulted in patterns in which prevalence of infection increased almost monotonically until it reached equilibrium; the prevalence of infection at the peak and the prevalence at equilibrium were very close (Fig. 5a).

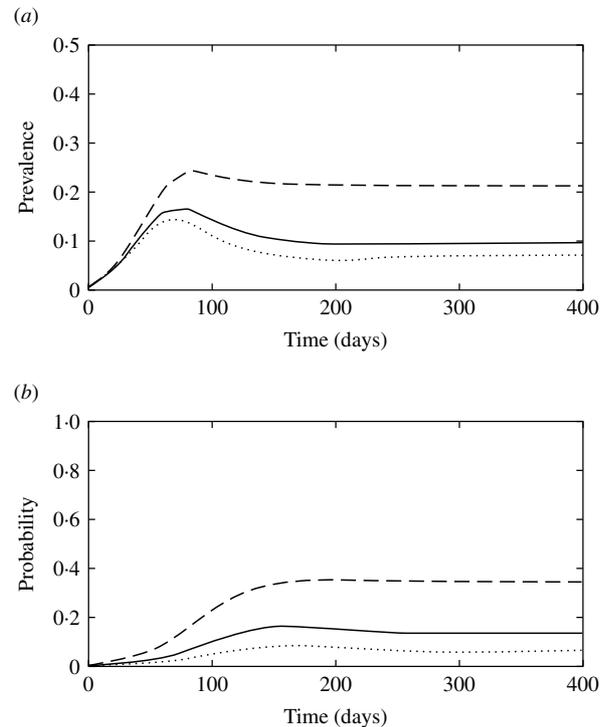


Fig. 5. (a) Simulated prevalence of infection with model 2 when the fraction of subclinically infected animals that become long-term shedders (f_{lt}) is 0.05 (·····), 0.12 (—) and 0.25 (---). (b) Probability that a newly infected case arises from contact with a long-term shedder in model 2 when f_{lt} is 0.05 (·····), 0.12 (—) and 0.25 (---).

The presence of super-shedders impacted both the short-term epidemic dynamics and the endemic stage fixed point (Fig. 6a), as a result of their high contribution to transmission (Fig. 6b). When the fraction of clinically infected animals that become super-shedders (f_{ss}) was 0.25, the probability that a new infection was transmitted by a super-shedder increased to 0.81 (Fig. 6b).

The relationship between population size and predicted endemic prevalence was highly nonlinear (Fig. 7). Models 1 and 2 had similar population size threshold values ($N \sim 215$), while in model 3 the presence of super-shedders decreased the threshold value to 75 (Fig. 7). At large population size, the three models predicted similar prevalence.

The impact of the parameter uncertainty on the prevalence of infection at equilibrium was assessed (Fig. 8). Models 1 and 2 behaved very similarly. The standard deviation around the mean predicted prevalence was the same, and the five parameters ranked as most influential (β_c , e , f , h , r) were the same, with similar SRC. On the other hand, model 3 predictions were also very sensitive to the parameters

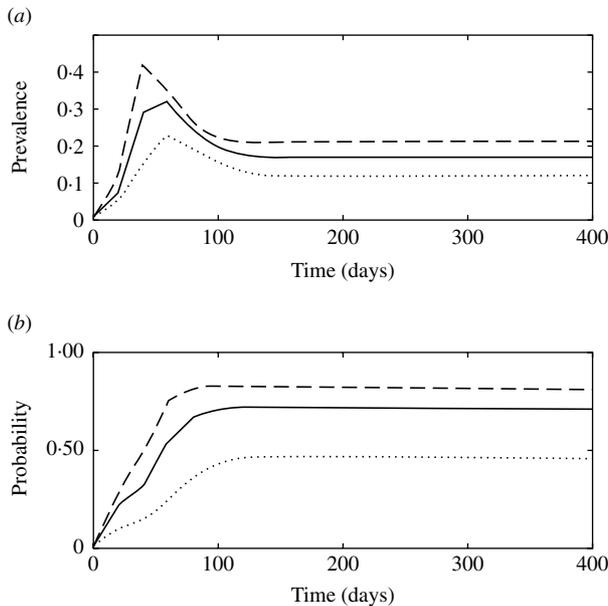


Fig. 6. (a) Simulated prevalence of infection with model 3 when the fraction of subclinically infected animals that become super-shedders (f_{ss}) is 0.05 (·····), 0.14 (—) and 0.25 (---). (b) Probability that a newly infected case arises from contact with a super-shedder in model 3 when f_{ss} is 0.05 (·····), 0.14 (—) and 0.25 (---).

related to super-shedders (β_{ss} , f_{ss} , h_{ss}). All three models were sensitive to the duration of immunity for *Salmonella* (r).

Basic reproduction number and critical vaccination thresholds

For models with several stages of infection such as the ones presented in this paper, the i terms that make up R_0 expressions can be interpreted as the number of new infections produced by a ‘typical’ individual during the time it spends in the i th infectious stage. For model 1, the three terms of R_0 expression represent the newly infected individuals produced by the ‘typical’ infected individual while clinically symptomatic [first term, R_{0c} in equation (5)], subclinically infected (second term), and subclinically infected after clinical recovery (third term) [equation (A 2.1)]. The sum of the second and third terms represents R_{0c} in equation (5). Using the mean parameter estimates from Table 1, the three terms for model 1 were 1.05, 0.25, 0.23 and thus the estimated R_0 was 1.53; the mean predicted R_0 values were greater for model 2 ($R_0 = 1.62$) and model 3 ($R_0 = 4.7$). In model 2, the contribution of the long-term shedder stage to the newly infected cases was 0.21 cases, while for model 3, the contribution of the super-shedders was 3.32 new cases.

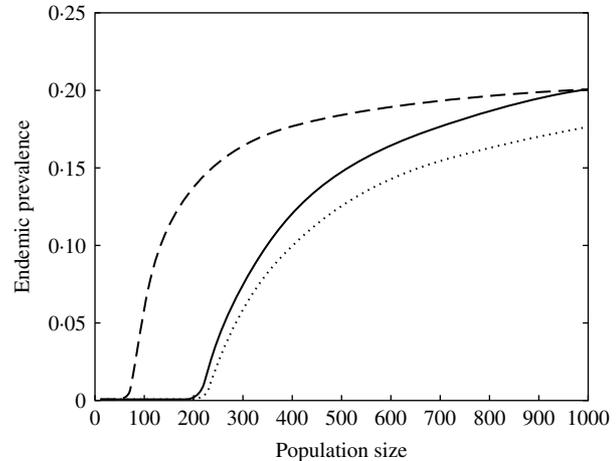


Fig. 7. Effect of population size on the predicted endemic prevalence for model 1 (·····), model 2 (—), and model 3 (---).

The sensitivity of R_0 to the model parameters was also explored (Fig. 9). The contribution of I_c to R_0 was the same for the three models (see Appendix 2). Therefore altering β_c resulted in an identical marginal increase of R_0 in the three models (with a R_0 change of 0.66 units with each change of 10^{-4} units of β_c). However, β_c rankings differed in the SRC analysis; for model 1, β_c was the second most influential parameter (SRC = 0.50), first most influential parameter (SRC = 0.55) for model 2, and fifth for model 3 (SRC = 0.09) (Fig. 9). The predicted R_0 for model 3 had a more skewed distribution when uncertainty on the parameters was included (Fig. 9). Model 3 was very sensitive to β_{ss} , f_{ss} , and h_{ss} .

The critical vaccination thresholds [equations (4) and (7)] were estimated for different scenarios (Table 2). When low vaccine efficacy ($\phi < 0.50$) was assumed, vaccination was inefficient in preventing an epidemic or eliminating an endemic infection, particularly if the vaccine is assumed to reduce only transmission from clinically ill animals. When the vaccine efficacy was > 0.75 , vaccination was a feasible control strategy for models 1 and 2. However, the presence of super-shedders would complicate the eradication of the infection. For model 3, only vaccinations that reduced transmission from all infected animals and had perfect efficacy were able to reduce R_0 to < 1 .

DISCUSSION

The overall objective of this study was to address the impact of heterogeneity of contagiousness and

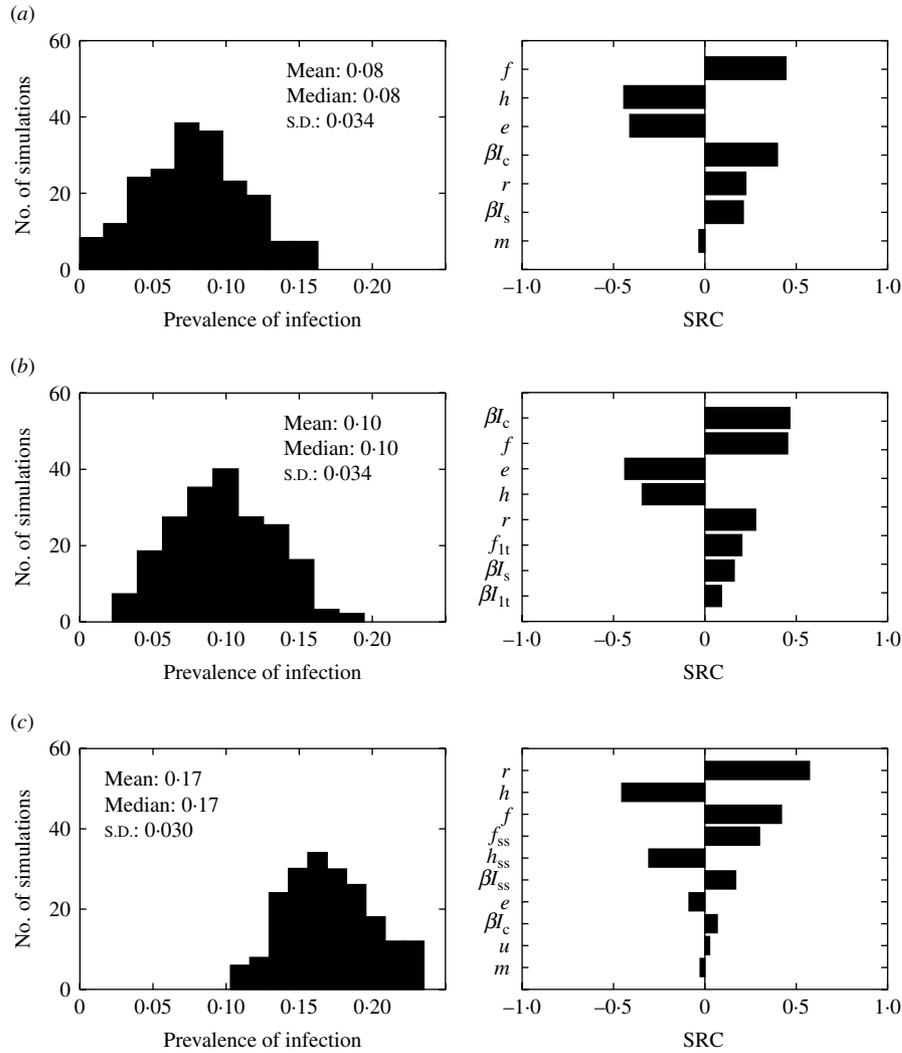


Fig. 8. Histograms of predicted endemic prevalence of infection when parameters were varied $\pm 25\%$ and standard regression coefficients (SRC) for the parameters ranked as the most influential for (a) model 1, (b) model 2 and (c) model 3. Parameters are defined in Table 1.

infectious period. Our approach consisted in the development of deterministic compartment models, in which heterogeneity was added by postulating different homogenous infected subgroups. The dynamics displayed by the models and threshold quantities were studied.

Importance of the different infection stages on *Salmonella* transmission

The three models exhibited different qualitative dynamic patterns. Model 1 was more prone to damped oscillations, especially with a high fraction of clinically infected animals, high transmission coefficients or fast recovery rates. Model 2 tended to increase the prevalence of infection until it reached the endemic

prevalence, with a less defined epidemic curve. Model 3 simulated an epidemic with a well-defined peak followed by high prevalence at equilibrium. All these dynamic patterns are plausible for *Salmonella*, whose epidemic behaviour at herd level range from large clinical outbreaks to endemic persistence without clinical cases. The range of prevalence of faecal shedding and clinical disease reported in the literature for *Salmonella* is also wide. The prevalence of faecal shedding for MDR *S. Newport* in post-parturient cows was 0.23 and 0.09 in two dairy farms with a history of clinical disease [11]. Huston *et al.* [18] reported prevalence of faecal shedding in adult cows as high as 0.87 without clinical signs for farms infected mostly with *S. Kentucky* and *S. Cerro*. This suggests that the presence of different infected states is the

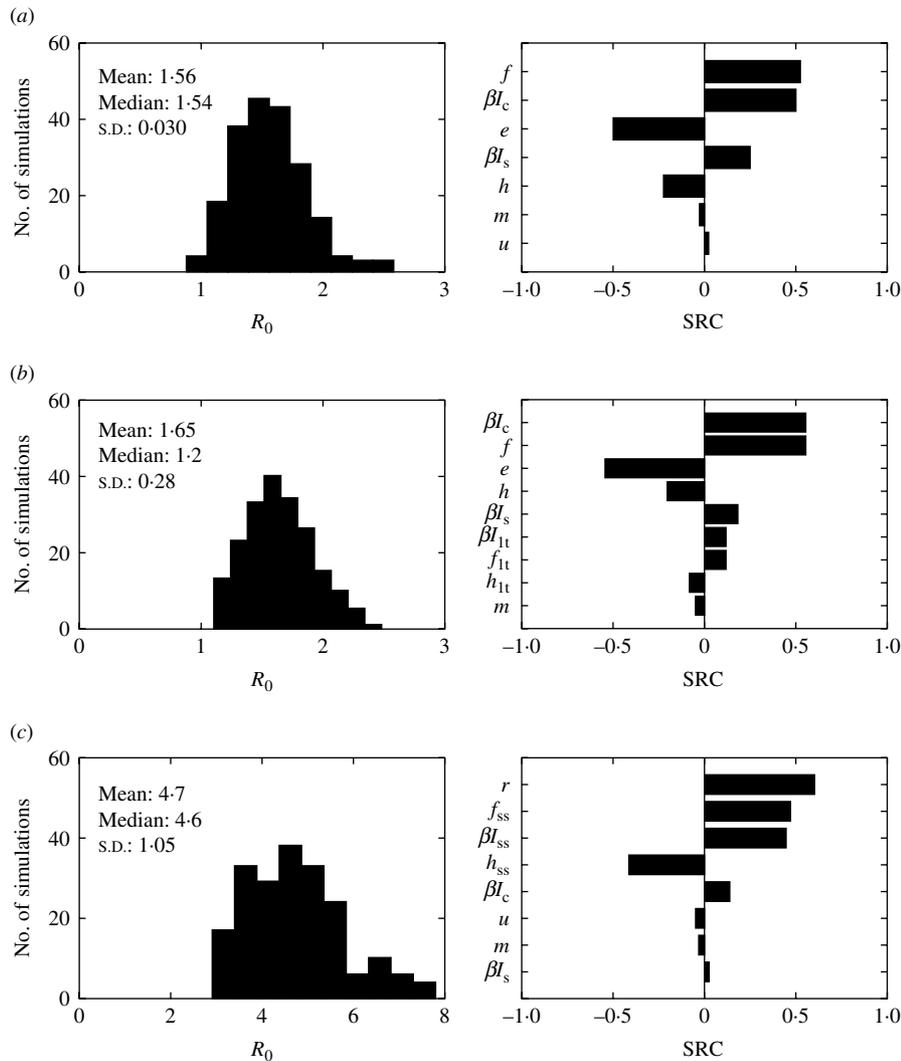


Fig. 9. Histograms for predicted basic reproduction number (R_0) when parameters were varied $\pm 25\%$ and standard regression coefficients (SRC) for the parameters ranked as the most influential for (a) model 1, (b) model 2 and (c) model 3. Parameters are defined in Table 1.

result of the combined effect of host immunity, herd and serotype characteristics.

Clinically infected animals were the main force of transmission for models 1 and 2. Increasing the number of clinically infected individuals resulted in larger outbreaks and higher prevalence at the endemic stage. The relevance of clinical cases on *Salmonella* persistence has been outlined in previous studies. In a case study, the prevalence was higher for the two herds that had a previous history of clinical salmonellosis [10]. Exposure to cattle with clinical salmonellosis has been described as a risk factor for both salmonellosis and *Salmonella* shedding [22, 25]. Diarrhoeic animals can shed *Salmonella* in a range of 10^8 – 10^{10} c.f.u./g faeces [16], which overlaps with the order of magnitude of the reported oral challenge

doses for adult cattle (10^9 – 10^{11}) [20]. In order to simulate the high prevalence of subclinical infection displayed by some serotypes (e.g. *S. Cerro*) in the absence of clinically infected animals ($f=0$), slower recovery rates for subclinically infected animals and long-term shedders than the values reported in Table 1 were necessary in our study.

Although heterogeneity in transmission has not been previously addressed for *Salmonella*, extensive work has been undertaken to investigate sources of heterogeneity for *Escherichia coli* O157 [27, 35]. The distribution of prevalence for *E. coli* O157 is over-dispersed; most of the farms have low prevalence, while a small proportion demonstrate high prevalence of infection [35]. Matthews *et al.* [35] evaluated several stochastic SIS models that included different sources

Table 2. Critical vaccination thresholds when vaccination is equally effective across all infectious stages (p_c) or only transmission from clinically infected animals is reduced ($p_c(\text{cl})$) for the three models assuming different vaccination efficacies (Φ) and group sizes (N)

	Φ							
	0.25		0.5		0.75		1	
	p_c	$p_c(\text{cl})$	p_c	$p_c(\text{cl})$	p_c	$p_c(\text{cl})$	p_c	$p_c(\text{cl})$
$N=200$								
Model 1	$R_0 < 1$	$R_0 < 1$						
Model 2	$R_0 < 1$	$R_0 < 1$						
Model 3	n.f.	n.f.	n.f.	n.f.	0.84	n.f.	0.63	n.f.
$N=345$								
Model 1	n.f.	n.f.	0.70	n.f.	0.46	0.68	0.35	0.51
Model 2	n.f.	n.f.	0.76	n.f.	0.51	0.78	0.38	0.58
Model 3	n.f.	n.f.	n.f.	n.f.	n.f.	n.f.	0.79	n.f.
$N=450$								
Model 1	n.f.	n.f.	1	n.f.	0.67	0.97	0.50	0.73
Model 2	n.f.	n.f.	n.f.	n.f.	0.70	n.f.	0.53	0.81
Model 3	n.f.	n.f.	n.f.	n.f.	n.f.	n.f.	0.84	n.f.

n.f., Non-feasible, $p_c > 1$.

of heterogeneity. Models that included between-animal variability in infectious period failed to reproduce the observed data. Similarly, simulations with model 2 showed that only when long-term shedders ($f_{\text{it}}=0.12$) had very slow recovery rates (i.e. duration of shedding longer than 2 years), were they able to maintain $R_0 > 1$, suggesting that the role a few individuals with unusually long infectious period but low contagiousness have on the persistence and transmission of the infection may be overestimated. On the other hand, models that incorporated either farm or animal variability in transmission rates improved the fit to the *E. coli* O157 prevalence data [35]. It was estimated that the fraction of animals with higher transmission rates (50 times higher) was 0.05 [35] for *E. coli* O157. In model 3, we included the super-shedder stage; based on our parameter estimates from field data and model assumptions, those super-shedders had both greater transmission rates (26.7 times higher than I_s) and longer infectious periods (5.7 times longer than I_s). It is reasonable to assume that animals that shed *Salmonella* in greater counts do so for a longer period of time. As has been shown before [27, 36], those individuals would have an important impact on the dynamics of transmission, being responsible for $\sim 80\%$ of the transmission (Fig. 6*b*). Sensitivity analysis indicated that the assumed high β_{ss} made model 3 very sensitive to the recovery rate for I_{ss} . (Figs 8, 9). In fitting the shedding

data, continuous shedding of *Salmonella* was assumed. However, intermittent shedding of *Salmonella* can also take place [17, 27], in which case, the total duration of shedding would be shorter and therefore recovery rates would be higher than the values reported in Table 1.

Impact of heterogeneity on vaccination programmes for *Salmonella*

An important implication of the presence of heterogeneity on the transmission of disease is that individual-specific control measures designed to target the most infectious individuals (e.g. isolation) are more efficient at eradicating disease than are population-wide control measures (e.g. random vaccination) [36, 37]. However, targeting specific subgroups to control *Salmonella* in a farm environment may prove very challenging. There are difficulties in identifying persistently infected individuals without clinical signs. For example, in the case of *S. Dublin*, the reported sensitivity of ELISA and bacterial culture from faeces may be as low as 21–50% and 6–14%, respectively in animals without clinical symptoms [38]. Further, ill-conceived intervention strategies may actually increase the prevalence of infection; the isolation of clinically ill animals in joint hospital and maternity pens has been reported to favour *Salmonella* persistence [11]. Therefore, we

focused on evaluating the impact that heterogeneity has on population-wide control measures such as vaccination when the objective of vaccination is to eradicate an endemic *Salmonella* infection or prevent its introduction in a completely susceptible population.

The proportion of individuals that must be vaccinated to eliminate the infection is related to both R_0 and vaccine efficacy. The objective of the simulated scenarios (Table 2) was to compare models rather than provide absolute vaccination threshold values. Results indicated that vaccines with low efficacy would be rather ineffective at providing protection against persistent or invasive *Salmonella* infection. High efficacy vaccines that either reduce transmission from clinically ill animals or from all infective individuals were predicted to aid in eradicating infection for models 1 and 2. In one study comparing the efficacy of a *Salmonella* bacterin and a modified live *Salmonella* vaccine for adult cattle on a commercial dairy, the bacterin did not have any effect on faecal shedding; while the modified live vaccine was able to reduced the frequency of faecal shedding for the same serogroup by 25% [31]. This would not reach the efficacy thresholds needed to eliminate infection as predicted for models 1 and 2. However, we cannot give a general recommendation regarding *Salmonella* vaccination because our study did not address economic factors such as vaccine costs and benefits other than elimination of infection. In addition, key data such as vaccine efficacy for current vaccines are not available.

The presence of super-shedders decreases the effectiveness of population-wide strategies, making necessary the application of strategies that target this specific group. The onset of large clinical outbreaks may be associated with the presence of concurrent diseases (e.g. metabolic diseases) or nutritional stress [10, 17]. It is plausible that the super-shedder stage of *Salmonella* could be associated with herd-level characteristics that induce a generalized decrease on the immunological resistance to *Salmonella*. In that case, further work examining the factors that predispose a herd to immunological incompetence against *Salmonella* are a necessary step to design appropriate control measures.

We demonstrated the impact of individual heterogeneity on *Salmonella* transmission dynamics and eradication thresholds. Infected individuals with clinical signs were the main force of infection and transmission for models 1 and 2, thus demonstrating

that reducing transmission from I_c could be an effective way to reduce *Salmonella* prevalence. Long-term shedders had a small impact on the transmission of the infection and on the estimated vaccination thresholds, while the presence of super-shedders increased R_0 and decreased the effectiveness of population-wide strategies to reduce infection, making necessary the application of strategies that target this specific group. The question of which model is more appropriate to describe *Salmonella* transmission under various conditions remains contingent upon future findings. Data on *Salmonella* counts for clinically infected animals and apparently healthy animals in *Salmonella* outbreaks would help to elucidate the relative contribution of the infected stages to transmission. In addition, because farms are small populations, large fluctuations on the prevalence can occur by chance, and therefore, stochastic approaches will be necessary to move modelling efforts forward to determine the presence of heterogeneity in *Salmonella* transmission.

APPENDIX 1

List of the differential equations for the state transition models

Model 1

$$\frac{dS}{dt} = \mu N + rR - (\beta_c I_c + \beta_s I_s + \mu)S, \quad (A1.1)$$

$$\frac{dI_c}{dt} = f(\beta_c I_c + \beta_s I_s)S - (e + m + \mu)I_c, \quad (A1.2)$$

$$\frac{dI_s}{dt} = (1-f)(\beta_c I_c + \beta_s I_s)S + eI_c - (h + \mu)I_s, \quad (A1.3)$$

$$\frac{dR}{dt} = hI_s - (r + \mu)R. \quad (A1.4)$$

Model 2

$$\frac{dS}{dt} = \mu N + rR - (\beta_c I_c + \beta_s I_s + \beta_{It} I_{It} + \mu)S, \quad (A1.5)$$

$$\frac{dI_c}{dt} = f(\beta_c I_c + \beta_s I_s + \beta_{It} I_{It})S - (e + m + \mu)I_c, \quad (A1.6)$$

$$\frac{dI_s}{dt} = (1-f)(\beta_c I_c + \beta_s I_s + \beta_{It} I_{It})S + eI_c - (h + \mu)I_s, \quad (A1.7)$$

$$\frac{dI_{It}}{dt} = f_{It} h I_s - (h_{It} + \mu)I_{It}, \quad (A1.8)$$

$$\frac{dR}{dt} = (1 - f_{II})hI_s + h_{II}I_{II} - (r + \mu)R. \tag{A1.9}$$

$$\frac{dI_s}{dt} = (1 - f)(\beta_c I_c + \beta_s I_s + \beta_{ss} I_{ss})S + (1 - f_{ss})eI_c - (h + \mu)I_s, \tag{A1.12}$$

Model 3

$$\frac{dS}{dt} = \mu N + rR - (\beta_c I_c + \beta_s I_s + \beta_{ss} I_{ss} + \mu)S, \tag{A1.10}$$

$$\frac{dI_{ss}}{dt} = f_{ss}eI_c - (h_{ss} + \mu)I_{ss}, \tag{A1.13}$$

$$\frac{dI_c}{dt} = f(\beta_c I_c + \beta_s I_s + \beta_{ss} I_{ss})S - (e + m + \mu)I_c, \tag{A1.11}$$

$$\frac{dR}{dt} = hI_s + h_{ss}I_{ss} - (r + \mu)R. \tag{A1.14}$$

APPENDIX 2

The R_0 expressions were obtained by using the next-generation matrix method [29, 30]. R_0 is defined as the spectral radius (dominant eigenvalue) of the next-generation matrix. To construct the next-generation matrix (FV^{-1}), we define the matrices F and V as follows:

$$F = \left[\frac{\partial F_i(x)}{\partial x_j} \right]_{x=x_0} \quad \text{and} \quad V = \left[\frac{\partial V_i(x)}{\partial x_j} \right]_{x=x_0},$$

where the (i, j) entry of F is the rate at which infected individuals in compartment j produce new infections in compartment i and the (i, j) entry of V is the net rate of change of animals in compartment i by any other means. The rates are evaluated at the disease-free equilibrium $x = x_0$. For model 1, F and V matrices are:

$$F = \begin{bmatrix} f\beta_c S_0 & f\beta_s S_0 \\ (1-f)\beta_c S_0 & (1-f)\beta_s S_0 \end{bmatrix}$$

$$V = \begin{bmatrix} e + \mu + m & 0 \\ -e & h + \mu \end{bmatrix}.$$

The next-generation matrix is then given by the product $FV^{-1} \cdot V^{-1}$, which indicates the average time that an individual spends in compartment i during its lifetime, is:

$$V^{-1} = \begin{bmatrix} \frac{1}{e + \mu + m} & 0 \\ \frac{e}{(e + \mu + m)(h + \mu)} & \frac{1}{h + \mu} \end{bmatrix},$$

and thus

$$FV^{-1} = \begin{bmatrix} \frac{f\beta_c S_0}{e + \mu + m} + \frac{fe\beta_s S_0}{(e + \mu + m)(h + \mu)} & \frac{f\beta_s S_0}{h + \mu} \\ \frac{(1-f)\beta_c S_0}{(e + \mu + m)} + \frac{(1-f)e\beta_s S_0}{(e + \mu + m)(h + \mu)} & \frac{(1-f)\beta_s S_0}{h + \mu} \end{bmatrix}.$$

The dominant eigenvalue of the matrix FV^{-1} gives R_0 , which is obtained by solving the characteristic equation $(FV^{-1})I - \Lambda I = 0$ where Λ is the eigenvalue and I is the identity matrix. The characteristic equation is given by

$$\left(\frac{f\beta_c S_0}{e + \mu + m} + \frac{(1-f)\beta_s S_0}{h + \mu} + \frac{fe\beta_s S_0}{(e + \mu + m)(h + \mu)} - \Lambda \right) \Lambda = 0.$$

Thus the dominant eigenvalue is given by

$$\Lambda_{\max} = R_0 = \frac{f\beta_c S_0}{e + \mu + m} + \frac{(1-f)\beta_s S_0}{h + \mu} + \frac{fe\beta_s S_0}{(e + \mu + m)(h + \mu)}. \tag{A2.1}$$

For model 2, F and V matrices are:

$$F = \begin{pmatrix} f\beta_c S_0 & f\beta_s S_0 & f\beta_{II} S_0 \\ (1-f)\beta_c S_0 & (1-f)\beta_s S_0 & (1-f)\beta_{II} S_0 \\ 0 & 0 & 0 \end{pmatrix}$$

$$V = \begin{pmatrix} e + \mu + m & 0 & 0 \\ -e & h + \mu & 0 \\ 0 & -f_{lt}h & h_{lt} + \mu \end{pmatrix}.$$

The next-generation matrix is then given by the product FV^{-1} . The characteristic equation for FV^{-1} is then given by

$$\left(\frac{f\beta_c S_0}{e + \mu + m} + \frac{fe\beta_s S_0}{(e + \mu + m)(h + \mu)} + \frac{fef_{lt}h\beta_{lt} S_0}{(e + \mu + m)(h + \mu)(h_{lt} + \mu)} + \frac{(1-f)\beta_s S_0}{h + \mu} + \frac{(1-f)f_{lt}h\beta_{lt} S_0}{(h + \mu)(h_{lt} + \mu)} - \Lambda \right) \Lambda^2 = 0.$$

Thus the dominant eigenvalue is given by

$$\Lambda_{\max} = R_0 = \frac{f\beta_c S_0}{e + \mu + m} + \frac{(1-f)\beta_s S_0}{h + \mu} + \frac{fe\beta_s S_0}{(e + \mu + m)(h + \mu)} + \frac{(1-f)f_{lt}h\beta_{lt} S_0}{(h + \mu)(h_{lt} + \mu)} + \frac{fef_{lt}h\beta_{lt} S_0}{(e + \mu + m)(h + \mu)(h_{lt} + \mu)}. \quad (A2.2)$$

For model 3, F and V matrices are:

$$F = \begin{pmatrix} f\beta_c S_0 & f\beta_s S_0 & f\beta_{ss} S_0 \\ (1-f)\beta_c S_0 & (1-f)\beta_s S_0 & (1-f)\beta_{ss} S_0 \\ 0 & 0 & 0 \end{pmatrix}$$

$$V = \begin{pmatrix} e + \mu + m & 0 & 0 \\ -(1-f_{ss})e & h + \mu & 0 \\ -f_{ss}e & 0 & h_{ss} + \mu \end{pmatrix}.$$

The characteristic equation for the next-generation matrix FV^{-1} is given by

$$\left(\frac{f\beta_c S_0}{e + \mu + m} + \frac{(1-f)\beta_s S_0}{h + \mu} + \frac{f(1-f_{ss})e\beta_s S_0}{(e + \mu + m)(h + \mu)} + \frac{eff_{ss}\beta_{ss} S_0}{(e + \mu + m)(h_{ss} + \mu)} - \Lambda \right) \Lambda^2 = 0$$

Thus the dominant eigenvalue is given by

$$\Lambda_{\max} = R_0 = \frac{f\beta_c S_0}{e + \mu + m} + \frac{(1-f)\beta_s S_0}{h + \mu} + \frac{f(1-f_{ss})e\beta_s S_0}{(e + \mu + m)(h + \mu)} + \frac{eff_{ss}\beta_{ss} S_0}{(e + \mu + m)(h_{ss} + \mu)}. \quad (A2.3)$$

ACKNOWLEDGEMENTS

This project has been funded with Federal funds from the National Institute of Allergy and Infectious Diseases, National Institute of Health, Department of Health and Human Services, under Contract no. NO1-AI-30054.

DECLARATION OF INTEREST

None.

REFERENCES

1. Mead PS, et al. Food-related illness and death in the United States. *Emerging Infectious Diseases* 1999; **5**: 607–625.
2. Dechet AM, et al. Outbreak of multidrug-resistant *Salmonella enterica* serotype Typhimurium definitive type 104 infection linked to commercial ground beef, northeastern United States, 2003–2004. *Clinical Infectious Diseases* 2006; **42**: 747–752.
3. Olsen SJ, et al. Multidrug-resistant *Salmonella typhimurium* infection from milk contaminated after pasteurization. *Emerging Infectious Diseases* 2004; **10**: 932–935.
4. Cody SH, et al. Two outbreaks of multidrug-resistant *Salmonella* serotype Typhimurium DT104 infections linked to raw-milk cheese in northern California. *Journal of the American Medical Association* 1999; **281**: 1805–1810.
5. Gupta A, et al. Emergence of multidrug-resistant *Salmonella enterica* serotype Newport infections resistant to expanded-spectrum cephalosporins in the United States. *Journal of Infectious Diseases* 2003; **188**: 1707–1716.
6. Helms M, et al. Excess mortality associated with antimicrobial drug-resistant *Salmonella typhimurium*. *Emerging Infectious Diseases* 2002; **8**: 490–495.
7. Martin LJ, et al. Increased burden of illness associated with antimicrobial-resistant *Salmonella enterica* serotype Typhimurium infections. *Journal of Infectious Diseases* 2004; **189**: 377–384.
8. Humphrey T. Science and society – *Salmonella*, stress responses and food safety. *Nature Reviews Microbiology* 2004; **2**: 504–509.

9. **Wray C, et al.** A three-year study of *Salmonella dublin* infection in a closed dairy herd. *Veterinary Record* 1989; **124**: 532–537.
10. **Anderson RJ, et al.** Epidemiologic and biological characteristics of salmonellosis in three dairy herds. *Journal of the American Veterinary Medical Association* 2001; **219**: 310–322.
11. **Cobbold RN, et al.** Long-term persistence of multi-drug-resistant *Salmonella enterica* serovar Newport in two dairy herds. *Journal of the American Veterinary Medical Association* 2006; **228**: 585–591.
12. **Anderson RM, May RM.** *Infectious Diseases of Humans: Dynamics and Control*. Oxford, UK: Oxford University Press, 1992.
13. **Xiao YN, et al.** Understanding the dynamics of *Salmonella* infections in dairy herds: a modelling approach. *Journal of Theoretical Biology* 2005; **233**: 159–175.
14. **Xiao Y, et al.** A semi-stochastic model for *Salmonella* infection in a multi-group herd. *Mathematical Biosciences* 2006; **200**: 214–233.
15. **Chapagain PP, et al.** A mathematical model of the dynamics of *Salmonella* Cerro infection in a US dairy herd. *Epidemiology and Infection*. Published online: 20 April 2007. doi:10.1017/S0950268807008400.
16. **De Jong H, Ekdahl MO.** Salmonellosis in calves – the effect of dose rate and other factors on transmission. *New Zealand Veterinary Journal* 1965; **13**: 59–67.
17. **Wray C, Davies RH.** *Salmonella* infections in cattle. In: Wray C, Wray A, eds. *Salmonella in Domestic Animals*. Wallingford, UK: CABI Publishing, 2000, pp. 169–190.
18. **Huston CL, Wittum TE, Love BC.** Persistent fecal *Salmonella* shedding in five dairy herds. *Journal of the American Veterinary Medical Association* 2002; **220**: 650–655.
19. **Begon M, et al.** A clarification of transmission terms in host-microparasite models: numbers, densities and areas. *Epidemiology and Infection* 2002; **129**: 147–153.
20. **Jones PW, Watson PR, Wallis TS.** Salmonellosis. In: Andrews AH, et al., eds. *Bovine Medicine: Disease and Husbandry of Cattle* Oxford, UK: Blackwell Publishing, 2004, pp. 215–230.
21. **Kabagambe EK, et al.** Risk factors for fecal shedding of *Salmonella* in 91 US dairy herds in 1996. *Preventive Veterinary Medicine* 2000; **43**: 177–194.
22. **Warnick LD, et al.** Effect of previous antimicrobial treatment on fecal shedding of *Salmonella enterica* subsp *enterica* serogroup B in New York dairy herds with recent clinical salmonellosis. *Preventive Veterinary Medicine* 2003; **56**: 285–297.
23. **Wray C, Sojka WJ.** Experimental *Salmonella typhimurium* infection in calves. *Research in Veterinary Science* 1978; **25**: 139–143.
24. **Warnick LD, et al.** Duration of fecal shedding following clinical salmonellosis in dairy cattle. In: *International Symposium on Veterinary Epidemiology and Economics*. Cairns, Australia, 2006.
25. **Fossler CP, et al.** Herd-level factors associated with isolation of *Salmonella* in a multi-state study of conventional and organic dairy farms – I. *Salmonella* shedding in cows. *Preventive Veterinary Medicine* 2005; **70**: 257–277.
26. **Low JC, et al.** Rectal carriage of enterohemorrhagic *Escherichia coli* O157 in slaughtered cattle. *Applied and environmental microbiology* 2005; **71**: 93–97.
27. **Matthews L, et al.** Heterogeneous shedding of *Escherichia coli* O157 in cattle and its implications for control. *Proceedings of the National Academy of Sciences USA* 2006; **103**: 547–552.
28. **Ray KA.** Epidemiology of antimicrobial resistant *Salmonella* on dairy farms in the northeast and midwest USA (Dissertation). Ithaca, NY: Cornell University, 2007, 225 pp.
29. **Diekmann O, Heesterbeek JAP.** *Mathematical Epidemiology of Infectious Diseases: Model Building, Analysis and Interpretation*. Chichester, UK: John Wiley & Sons, 2000.
30. **van den Driessche P, Watmough J.** Reproduction numbers and sub-threshold endemic equilibria for compartmental models of disease transmission. *Mathematical Biosciences* 2002; **180**: 29–48.
31. **House JK, et al.** Evaluation of an autogenous *Salmonella* bacterin and a modified live *Salmonella* serotype choleraesuis vaccine on a commercial dairy farm. *American Journal of Veterinary Research* 2001; **62**: 1897–1902.
32. **Robertsson JA, et al.** *Salmonella typhimurium* infection in calves – protection and survival of virulent challenge bacteria after immunization with live or inactivated vaccines. *Infection and Immunity* 1983; **41**: 742–750.
33. **Helton JC, Davis FJ.** Illustration of sampling-based methods for uncertainty and sensitivity analysis. *Risk Analysis* 2002; **22**: 591–622.
34. **Helton JC, Davis FJ.** Latin hypercube sampling and the propagation of uncertainty in analyses of complex systems. *Reliability Engineering & System Safety* 2003; **81**: 23–69.
35. **Matthews L, et al.** Super-shedding cattle and the transmission dynamics of *Escherichia coli* O157. *Epidemiology and Infection* 2006; **134**: 131–142.
36. **Lloyd-Smith JO, et al.** Superspreading and the effect of individual variation on disease emergence. *Nature* 2005; **438**: 355–359.
37. **Woolhouse MEJ, et al.** Heterogeneities in the transmission of infectious agents: implications for the design of control programs. *Proceedings of the National Academy of Sciences USA* 1997; **94**: 338–342.
38. **Nielsen LR, Toft N, Ersboll AK.** Evaluation of an indirect serum ELISA and a bacteriological faecal culture test for diagnosis of *Salmonella* serotype *dublin* in cattle using latent class models. *Journal of Applied Microbiology* 2004; **96**: 311–319.
39. **Mastroeni P, et al.** *Salmonella*: immune responses and vaccines. *Veterinary Journal* 2001; **161**: 132–164.